各 NLAST 的 误差 E(Δ U)	Mismatch 版	Sinc 版	Σ Cos 版	M ⊕ Σ Cos 版
完全 失配	10-7	10-2	10-1	₹ 10 ⁻⁷ \$
部分 匹配	10-1	10-1	10-4	(10-4)
完全 匹配	1	10-2	10-6	₹ 10-6 \$



$$M \oplus \Sigma \text{ Cos} - \text{NLAST:} \qquad \text{np.where} \left(\left| \frac{\Delta k_z z}{2} \right| \le (J+1)\pi, \mathcal{F}[E_{3z}] \right|_{\Sigma \text{Cos}}, 0 \right) + \text{np.where} \left(\left| \frac{\Delta k_z z}{2} \right| > (J+1)\pi, \mathcal{F}[E_{3z}] \right|_{\text{Mismatch}}, 0 \right)$$

$$\begin{split} \mathcal{E} & \text{Cos} - \text{NLAST:} \quad \mathcal{F}[E_{3z}] \Big|_{\Sigma \text{Cos}} \approx \frac{\chi_{\text{eff}} \omega_{3}^{2}}{2c^{2}} \cdot \sum_{j} a_{j} \mathcal{F} \Bigg[\mathcal{F}_{z} \Big[M_{\text{eff}} \big(r \big) \Big] \cdot \underbrace{\frac{e^{ig_{z}} \frac{b_{j} \pm 1}{2b_{j}} z}{\overline{k_{1z}} + \overline{k_{2z}} + g_{z} + k_{3z}}} \cdot \text{d}g_{z} \cdot e^{ik_{3z} \frac{b_{j} \mp 1}{2b_{j}} z} \cdot iz \end{split}$$

$$& \text{ ψ $\Rightarrow $ \mathcal{E}[E_{3z}] \Big|_{\text{Mismatch}} \approx \frac{\chi_{\text{eff}} \omega_{3}^{2}}{c^{2}} \cdot \mathcal{F} \underbrace{\mathcal{F}[\mathcal{F}_{z} \Big[M_{\text{eff}} \big(r \big) \Big] \cdot E_{1z} E_{2z} \Big] \cdot e^{ig_{z}z} - \mathcal{F}[\mathcal{F}_{z} \Big[M_{\text{eff}} \big(r \big) \Big] \cdot E_{10} E_{20} \Big] \cdot e^{ik_{3z}z}} \cdot \text{d}g_{z} } \cdot dg_{z}$$

失配解 - NLAST:
$$\mathcal{F}[E_{3z}]\Big|_{\text{Mismatch}} \approx \frac{\chi_{\text{eff}} \omega_{3}^{2}}{c^{2}} \cdot \int \frac{\mathcal{F}[\mathcal{F}_{z}[M_{\text{eff}}(\mathbf{r})] \cdot E_{1z}E_{2z}] \cdot e^{ig_{z}z} - \mathcal{F}[\mathcal{F}_{z}[M_{\text{eff}}(\mathbf{r})] \cdot E_{10}E_{20}] \cdot e^{ik_{3z}z}}{\left(\overline{k_{1z}} + \overline{k_{2z}} + g_{z}\right)^{2} - k_{3z}^{2}} \cdot dg_{z}$$