## NLAST

# 几乎已能

99.99 %

SFG

完全理解

拉曼奈斯

### NLAST

z 向非完美匹配时,

> 99.99 %

$$\mathcal{F}\left[E_3\left(x,y,z\right)\right] \approx \frac{\chi_{\text{eff}}\omega_3^2}{c^2} \cdot \sum_{l_z=-\infty}^{+\infty} C_{l_z} \cdot \left[$$

$$\frac{\mathcal{F}\left[M_{\text{eff}}\left(x,y\right)\cdot E_{1}\left(\mathbf{r}\right)E_{2}\left(\mathbf{r}\right)\right]\cdot e^{ig_{l_{z}}z}-\mathcal{F}\left[M_{\text{eff}}\left(x,y\right)\cdot E_{10}E_{20}\right]\cdot e^{ik_{3z}z}}{\left(\overline{k_{1z}}+\overline{k_{2z}}+g_{l_{z}}\right)^{2}-k_{3z}^{2}}$$

$$\frac{\overline{k_{1z}}}{\overline{k_{1z}}} = \sum_{k_{1x}, k_{1y}} \frac{\mathcal{F}\left[E_{10}\right]^{2}}{\sum_{k_{1x}, k_{1y}} \mathcal{F}\left[E_{10}\right]^{2}} k_{1z}$$

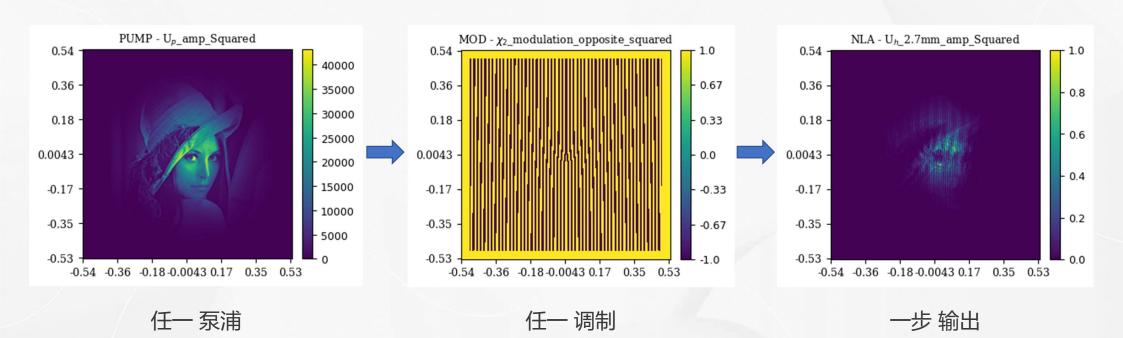
$$\overline{k_{2z}} = \sum_{k_{2x}, k_{2y}} \frac{\mathcal{F}\left[E_{20}\right]^{2}}{\sum_{k_{2x}, k_{2y}} \mathcal{F}\left[E_{20}\right]^{2}} k_{2z}$$

SFG

$$\mathcal{F}\left[E_{3}\left(x,y,z\right)\right] \approx \frac{\chi_{\text{eff}}\omega_{3}^{2}}{c^{2}} \cdot \sum_{l_{z}=-\infty}^{+\infty} C_{l_{z}} \cdot \left[\begin{array}{c} \frac{\mathcal{F}\left[M_{\text{eff}}\left(x,y\right) \cdot E_{1}\left(r\right)E_{2}\left(r\right)\right] \cdot e^{ig_{l_{z}}z} - \mathcal{F}\left[M_{\text{eff}}\left(x,y\right) \cdot E_{10}E_{20}\right] \cdot e^{ik_{3z}z}}{\left(\overline{k_{1z}} + \overline{k_{2z}} + g_{l_{z}}\right)^{2} - k_{3z}^{2}} \end{array}\right]$$

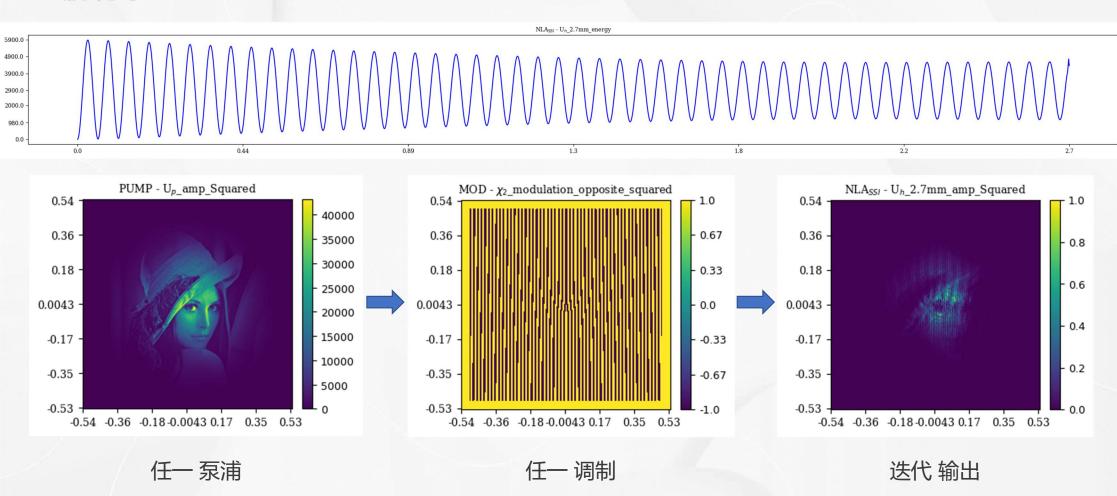
新公式, 无视 晶体长度, 一步到位

#### 耗时 < 1 s

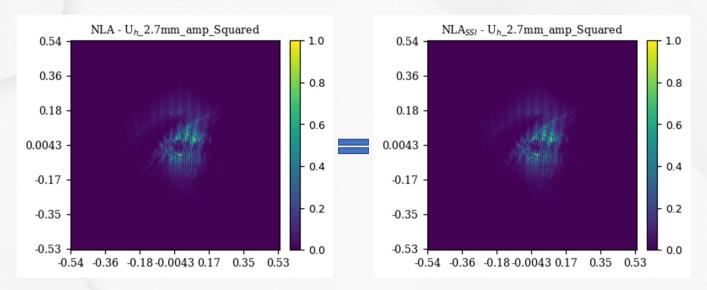


旧公式, 只能迭代 一般 耗时 > 100 s

$$\mathcal{F}\left[E_{3}(x,y,z)\right] = \frac{\omega_{3}^{2}}{c^{2}} \cdot \frac{1 - e^{-ik_{3z}dz}}{k_{3z}^{2}} \cdot \sum_{j=1}^{z/dz} Q_{3,z-j\cdot dz} \cdot e^{ik_{3z}\cdot j\cdot dz}$$



$$\mathcal{F}\left[E_{3}\left(x,y,z\right)\right] \approx \frac{\chi_{\text{eff}}\omega_{3}^{2}}{c^{2}} \cdot \sum_{l_{z}=-\infty}^{+\infty} C_{l_{z}} \cdot \left[\frac{\mathcal{F}\left[M_{\text{eff}}\left(x,y\right) \cdot E_{1}\left(\boldsymbol{r}\right)E_{2}\left(\boldsymbol{r}\right)\right] \cdot e^{ig_{l_{z}}z} - \mathcal{F}\left[M_{\text{eff}}\left(x,y\right) \cdot E_{10}E_{20}\right] \cdot e^{ik_{3z}z}}{\left(\overline{k_{1z}} + \overline{k_{2z}} + g_{l_{z}}\right)^{2} - k_{3z}^{2}}\right]$$



一步 输出

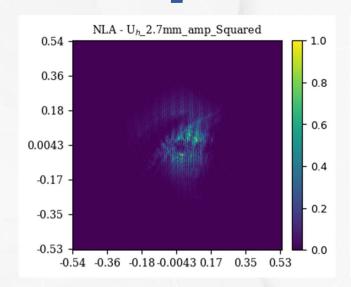
迭代 输出

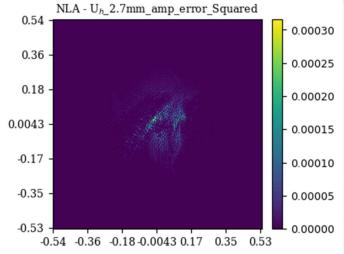
$$\mathcal{F}\left[E_{3}(x,y,z)\right] = \frac{\omega_{3}^{2}}{c^{2}} \cdot \frac{1 - e^{-ik_{3z}dz}}{k_{3z}^{2}} \cdot \sum_{j=1}^{z/dz} Q_{3,z-j\cdot dz} \cdot e^{ik_{3z}\cdot j\cdot dz}$$

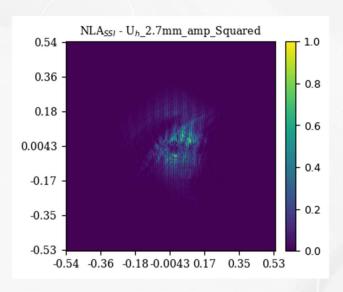
$$\mathcal{F}\left[E_{3}\left(x,y,z\right)\right] \approx \frac{\chi_{\text{eff}}\omega_{3}^{2}}{c^{2}} \cdot \sum_{l_{z}=-\infty}^{+\infty} C_{l_{z}} \cdot \left[\frac{\mathcal{F}\left[M_{\text{eff}}\left(x,y\right) \cdot E_{1}\left(\boldsymbol{r}\right)E_{2}\left(\boldsymbol{r}\right)\right] \cdot e^{ig_{l_{z}}z} - \mathcal{F}\left[M_{\text{eff}}\left(x,y\right) \cdot E_{10}E_{20}\right] \cdot e^{ik_{3z}z}}{\left(\overline{k_{1z}} + \overline{k_{2z}} + g_{l_{z}}\right)^{2} - k_{3z}^{2}}\right]\right]$$

U NonZero size=0.9, w0=0.3, LO Crystal=2.66, zo structu lam1=1.064, is air pump=0,

deff=30, is fft=1, fft mode







一步 输出

二者 之差 ~ 0.01 %

迭代 输出

Tx=18.769, Ty=20, Tz=6.2, mx=1, my=0, mz=1, is stripe=0, is NLAST=1,

真·随机参数 
$$\mathcal{F}\left[E_{3}(x,y,z)\right] = \frac{\omega_{3}^{2}}{c^{2}} \cdot \frac{1 - e^{-ik_{3z}dz}}{k_{3z}^{2}} \cdot \sum_{j=1}^{z/dz} Q_{3,z-j\cdot dz} \cdot e^{ik_{3z}\cdot j\cdot dz}$$

(但 T, 得远离 2 l。)

U\_NonZero\_size=0.9, w0=0.1, z0=10,

lam1=1.064, is\_air\_pump=0, is\_a
deff=30, is\_fft=1, fft\_mode=0,

Tx=10, Ty=10, Tz=3, mx=1, my=0, mz=0,

$$\mathcal{F}\left[E_{3}\left(x,y,z\right)\right] \approx \frac{\chi_{\text{eff}}\omega_{3}^{2}}{c^{2}} \cdot \sum_{l_{z}=-\infty}^{+\infty} C_{l_{z}} \cdot \left[\frac{\mathcal{F}\left[M_{\text{eff}}\left(x,y\right) \cdot E_{1}\left(\boldsymbol{r}\right)E_{2}\left(\boldsymbol{r}\right)\right] \cdot e^{ig_{l_{z}}z} - \mathcal{F}\left[M_{\text{eff}}\left(x,y\right) \cdot E_{10}E_{20}\right] \cdot e^{ik_{3z}z}}{\left(\overline{k_{1z}} + \overline{k_{2z}} + g_{l_{z}}\right)^{2} - k_{3z}^{2}}\right]$$



$$E_{3}(x,y,z) \approx \frac{\chi_{\text{eff}}\omega_{3}^{2}}{c^{2}} \cdot \sum_{l_{z}=-\infty}^{+\infty} C_{l_{z}} \cdot \left\{ \mathcal{F}^{-1} \left[ \frac{\mathcal{F}\left[M_{\text{eff}}(x,y) \cdot E_{1}(\mathbf{r}) E_{2}(\mathbf{r})\right] \cdot e^{ig_{l_{z}}z}}{\left(\overline{k_{1z}} + \overline{k_{2z}} + g_{l_{z}}\right)^{2} - k_{3z}^{2}} \right] \right\}$$

$$\left[ \mathcal{F}^{-1} \left[ \frac{\mathcal{F} \left[ M_{\text{eff}} \left( x, y \right) \cdot E_{10} E_{20} \right] \cdot e^{ik_{3z}z}}{\left( \overline{k_{1z}} + \overline{k_{2z}} + g_{l_z} \right)^2 - k_{3z}^2} \right] \right]$$

正空间 【

晶体内) 正向 传播

斜向 传播



0.54

0.36 -

0.18 -

0.0043

-0.17 -

-0.35 -

-0.53 -

#### 拉曼 奈斯 远场

-0.54 -0.36 -0.18-0.0043 0.17 0.35 0.53

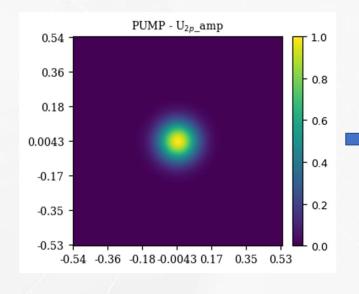
NLA - G<sub>2h</sub>\_10.0mm\_amp

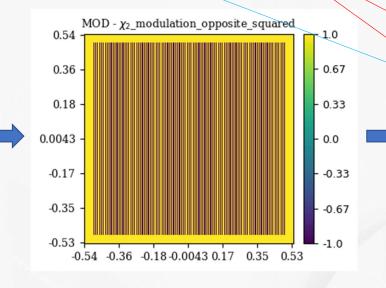
0.004

0.003

0.001

0.000

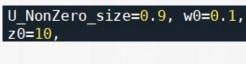




高斯入射

1维光栅

拉曼 奈斯 近场



lam1=1.064, is air pump=0, is ai deff=30, is fft=1, fft mode=1,

Tx=10, Ty=10, Tz=3, mx=1, my=0, mz=0,

$$\mathcal{F}\left[E_3\left(x,y,z\right)\right] \approx \frac{\chi_{\text{eff}}\omega_3^2}{c^2} \cdot \sum_{l_x,l_y,l_z=-\infty}^{+\infty} C_{l_x,l_y,l_z}$$

$$\left[\begin{array}{c} \mathcal{F}\left[rac{E}{E}
ight]$$

$$\mathcal{F}\left[E_{3}\left(x,y,z\right)\right] \approx \frac{\chi_{\text{eff}}\omega_{3}^{2}}{c^{2}} \cdot \sum_{l_{x},l_{y},l_{z}=-\infty}^{+\infty} C_{l_{x},l_{y},l_{z}} \left[ \frac{\mathcal{F}\left[E_{1}\left(r\right)E_{2}\left(r\right)\right]\Big|_{k_{3x}-g_{x},k_{3y}-g_{y}} \cdot e^{ig_{l_{z}}z} - \mathcal{F}\left[E_{10}E_{20}\right]\Big|_{k_{3x}-g_{x},k_{3y}-g_{y}} \cdot e^{ik_{3z}z}}{\left(\overline{k_{1z}} + \overline{k_{2z}} + g_{l_{z}}\right)^{2} - k_{3z}^{2}} \right]$$



$$E_{3}(x,y,z) \approx \frac{\chi_{\text{eff}}\omega_{3}^{2}}{c^{2}} \cdot \sum_{l_{x},l_{y},l_{z}=-\infty}^{+\infty} C_{l_{x},l_{y},l_{z}} \cdot \left\{ \mathcal{F}^{-1} \left[ \frac{\mathcal{F}\left[E_{1}(\mathbf{r})\right]}{\left(\overline{k_{1z}}\right)} \right] \right\}$$

$$\mathcal{F}^{-1} \left[ \frac{\mathcal{F} \left[ \underline{E}_{1}(\mathbf{r}) \underline{E}_{2}(\mathbf{r}) \right] \Big|_{k_{3x} - g_{x}, k_{3y} - g_{y}} \cdot e^{ig_{l_{z}}z}}{\left( \overline{k}_{1z} + \overline{k}_{2z} + g_{l_{z}} \right)^{2} - k_{3z}^{2}} \right]$$

$$\mathcal{F}^{-1} \left[ \frac{\mathcal{F} \left[ E_{10} E_{20} \right] \Big|_{k_{3x} - g_x, k_{3y} - g_y} \cdot e^{ik_{3z}z}}{\left( \overline{k_{1z}} + \overline{k_{2z}} + g_{l_z} \right)^2 - k_{3z}^2} \right] \right]$$



正向 传播

斜向 传播



0.54

0.36 -

0.18 -

0.0043 -

-0.17 -

-0.35 -

-0.53 -

#### 拉曼 奈斯 远场

-0.54 -0.36 -0.18-0.0043 0.17 0.35 0.53

NLA - G2h\_10.0mm\_amp

0.014

0.012

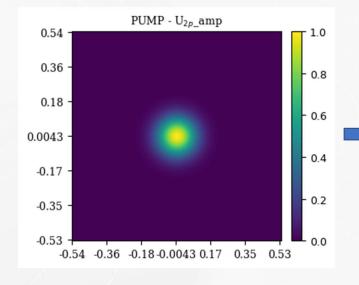
0.010 0.008

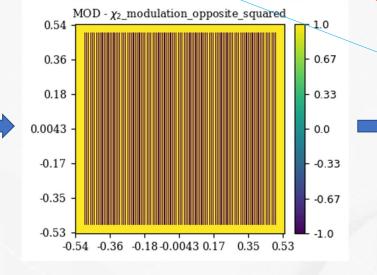
0.006

0.004

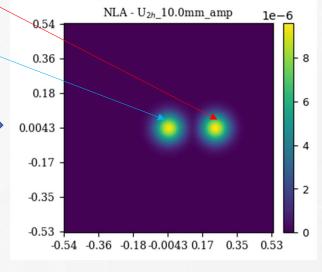
0.002

0.000





1维光栅



拉曼 奈斯 近场

高斯入射

