



Technical Specification and Study Report

[Perceptron Learning, Pocket, Logistic Regression, and Linear Regression Algorithms]

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0.9	11/4/2016	Jianfa Lin	First draft release
1.0	11/5/2016	Jianfa Lin	First release

Related documents

Document	Description
NeuralNetwork.py	The implementation of Neural Network algorithm by Python 3.5
downgesture_train.list	List of training data sets for Neural Network algorithm.
downgesture_test.list	List of testing data sets for Neural Network algorithm.
gestures	Folder of training data sets and testing data sets.

Contribution

Name	USC ID	Labour
Cheng-Lin Li	9799716705	Implement the code
Jianfa Lin	6950769029	Write the document.

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1 INTRODUCTION

1.1 Objectives

Implement the Back Propagation algorithm for Feed Forward Neural Networks to learn down gestures from training images available in **downgesture_train.list**. After the training, use the trained network to predict the labels for the gestures in the test images available in **downgesture_test.list**.

The result should print out whether the prediction is correct for “down” gesture, the prediction result and the accuracy of prediction.

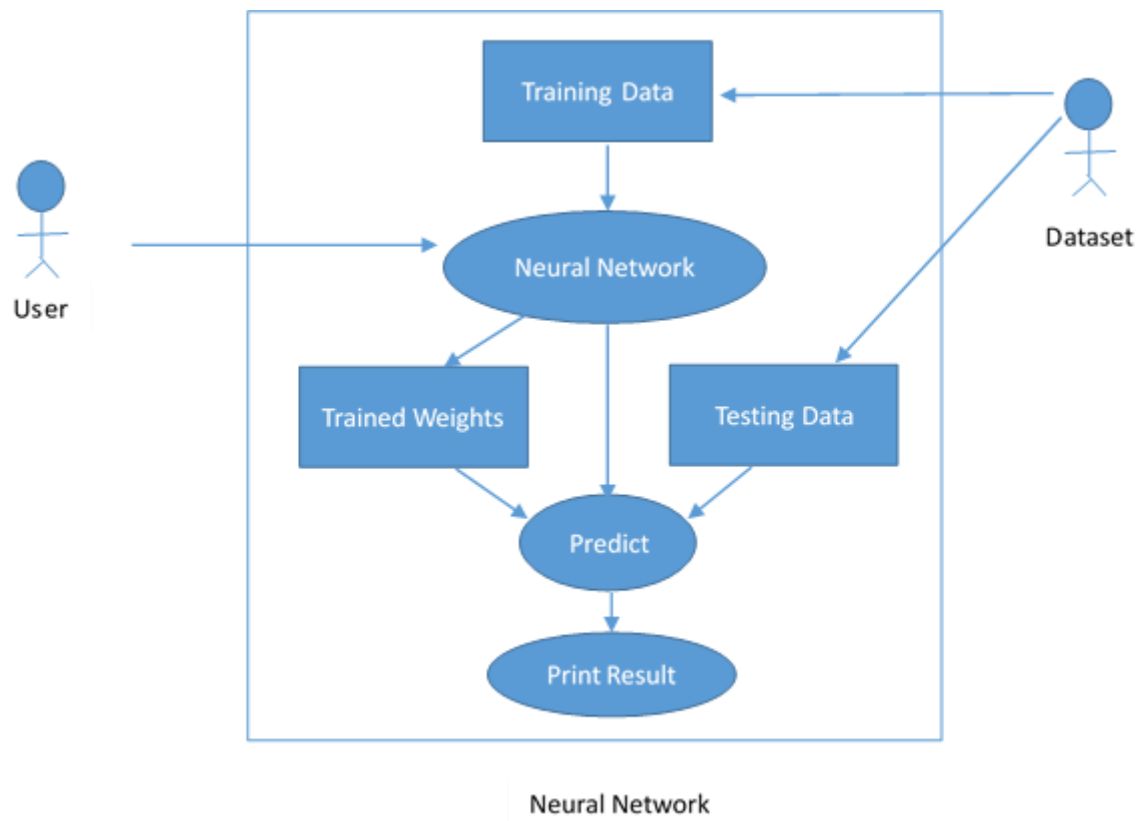
There are 184 training data sets in downgesture_train.list and 83 testing data sets in downgesture_test.list. The training data sets and testing data sets are PGM image, which is a special to present grayscale graphic image.

2 Functionality [\[1\]](#)

2.1 Description: Neural Network Algorithm

1. Input the dataset and signal the data with 1 or 0.
2. Assign the parameters.
3. Get an initial weight vector with [[Weights of level-01], [Weights of level-12], ..., [Weights of level-(L-1)(L)]], in which each value in the assigned range.
4. Compute $X_j^{(l)}$ in the forward direction with one random training data set.
5. Compute $\delta_j^{(l)}$ in the backward direction with corresponding result in step 4.
6. Update weight vectors $w_{ij}^{(l)}$ by $w_{ij}^{(l)} = w_{ij}^{(l)} - \eta * X_i^{(l-1)} * \delta_j^{(l)}$. Where η is learning rate.
7. Repeat step 4 ~ 6 a certain number of times. (1000 times here)
8. Predict the gesture of testing dataset with trained weights vector, and calculate the correct rate of prediction.

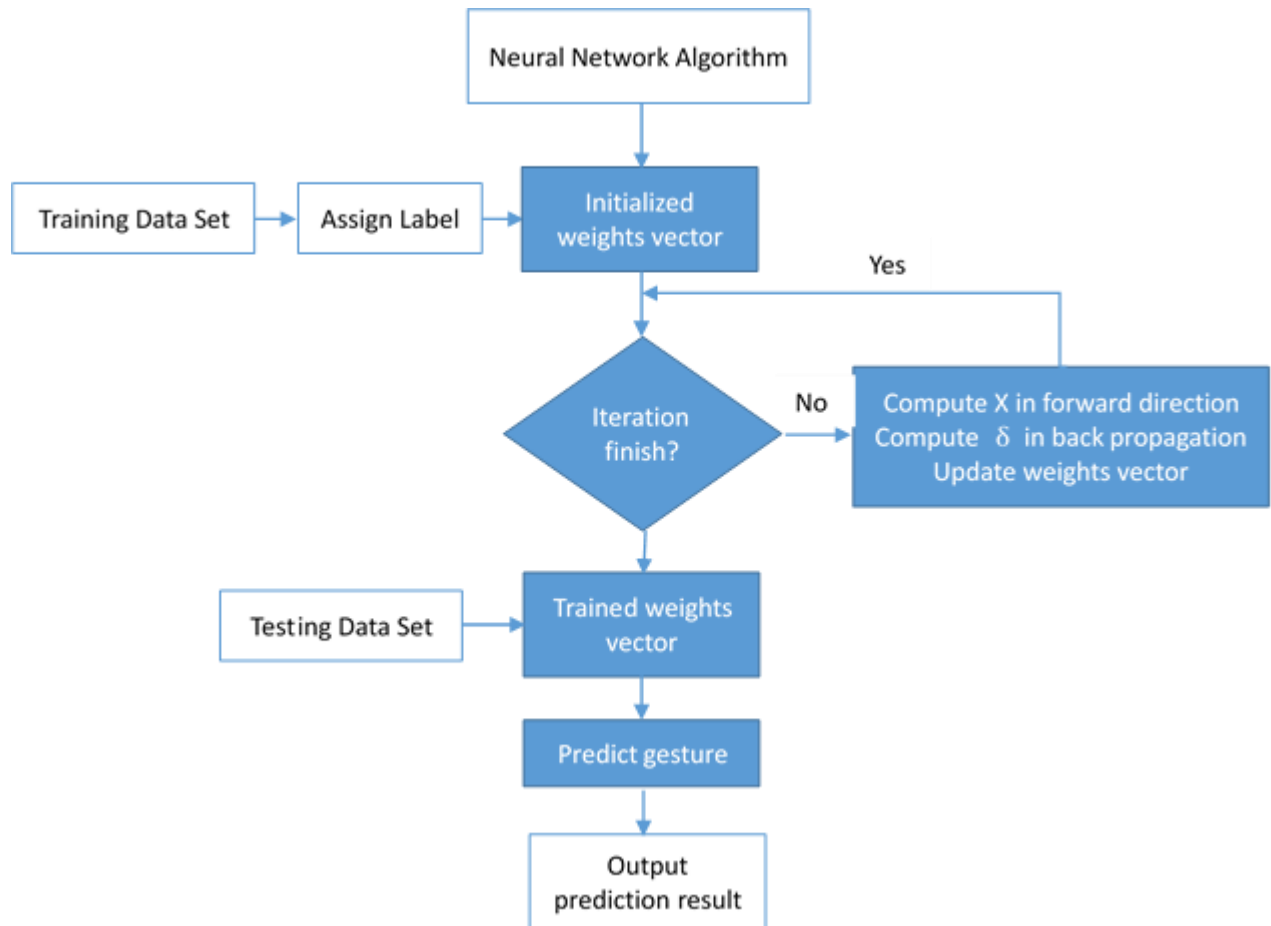
3 Use Case



4 Architecture

4.1 Architecture Overview for Neural Network Algorithms.

Here is the generalized architecture diagram for Neural Network algorithms.



5 Design

5.1 Data Structure

1. Training data and testing data are stored in array like [[data1], [data2], ... , [dataN]]. For [data1] = [value_dimension_1, value_dimension_2, ..., value_dimension_d].
2. Labels of each data set are stored in list.
3. Weights store in an array like [[Weights of level-01], [Weights of level-12], ..., [Weights of level-(L-1)(L)]]]. For [Weights of Level-01]=[[w01, w02, ..., w0d], [w11, w12, ..., w1d], ... [wd1, wd2, ..., wdd]]
4. The layer sizes are store in an array, in which each item corresponds to different layer.
5. Weight vector store in an array/vector.

5.2 Procedures

1. Get input training data sets from files.
2. Assign label to each data set according to its file name. If 'down' exists in file name, the label is 1, otherwise 0.
3. Class constructor initialize the hidden layers array, network layers array, activation function and other parameters according to user's input.
4. Execute algorithm by execute() function.
5. Initialize weights vector randomly with each value between given range.
6. A while-loop trains the neural network with all training data sets and initial weight vector.
 - a. According to Stochastic Learning approach, randomly pick up a data set from all training data sets.
 - b. Compute $X_j^{(l)} = \theta\left(\sum_{i=0}^{d^{(l-1)}} w_{ij}^{(l)} X_i^{(l-1)}\right)$ in the forward direction data set chosen in a. θ is an activation function, which can be both logistic sigmoid and hyperbolic tangent functions as what we set.
 - c. Compute $\delta_j^{(l-1)} = \left(1 - \left(X_i^{(l-1)}\right)^2\right) \sum_{j=1}^{d^{(l)}} W_{ij}^{(l)} \delta_j^{(l)}$ in the backward direction with corresponding result in step b.
 - d. Update weight vectors $w_{ij}^{(l)}$ by $w_{ij}^{(l)} = w_{ij}^{(l)} - \eta * X_i^{(l-1)} * \delta_j^{(l)}$. η is learning rate.
7. The program terminates when the maximum iteration was reached. The default iteration here is 1000.
8. Get input testing data sets from files.
9. Predict the label of each data set with trained neural network. If the prediction finds out the "down" gesture correctly, print "Match(O)", otherwise "Match(X)". Calculate and output the accuracy finally.

5.3 Optimizations and Challenges

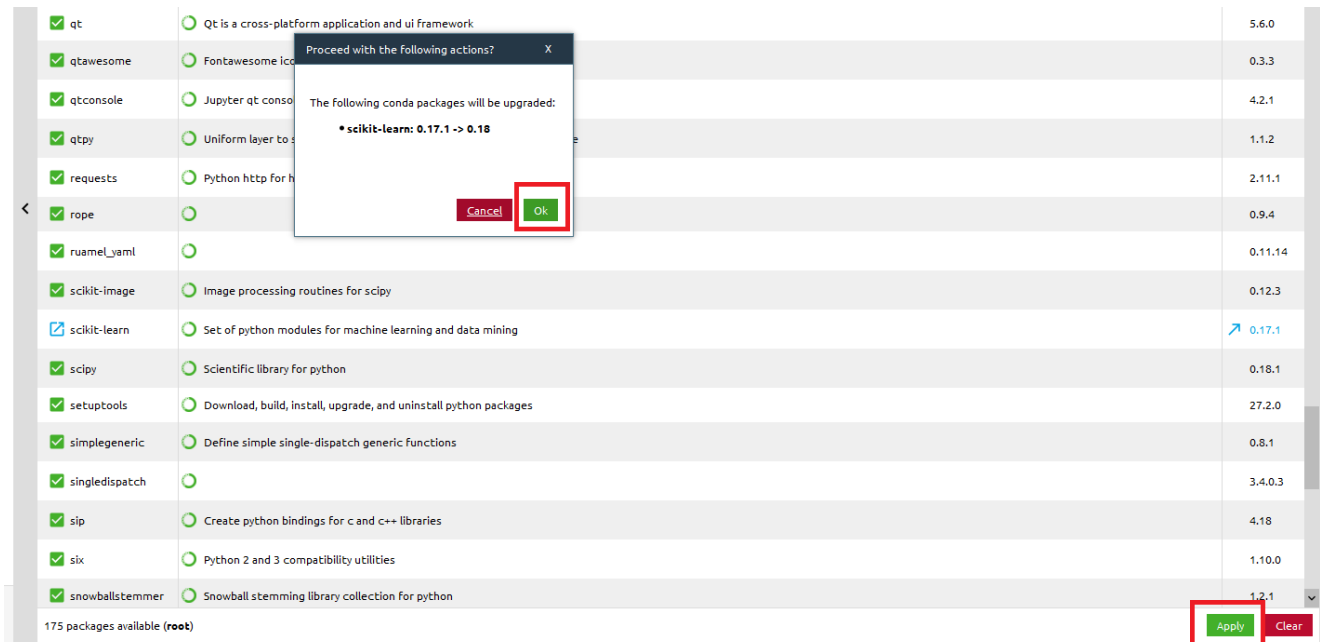
5.3.1 Optimization

- In the training procedure, we pick up the data randomly rather than sequentially from data set in every training epoch. Because we found that if putting in the data sets in sequence and repeating, the neural network would be less well-trained so that the accuracy of prediction would be lower.

- Combine the step 6.c and step 6.d in section 5.2 as mentioned above. During the calculation of $\delta_j^{(l-1)}$, we found that $w_{ij}^{(l)}$ can be updated after being leveraged in calculation, so we update it at the same loop.
- The implementation supports logistic (this assignment) and hyperbolic tangent (professor teach) activation functions with multiple hidden layers.
- The implementation supports binary classification enable or disable feature in logistic activation function. It will help to observe the gap between label and output data for parameters tuning purpose.
- According to our trail, (0,1) is a better range for the weight vectors when applying in our program, which help trained neural network get accuracy as high as 95% at most.

5.3.2 Challenge:

- What is the best initial weight matrix is the most critical for the accuracy, especially in a relative small training iterations.
- It's very confusing when dealing with array and matrix operations, especially for the weights at this time. The weights vector in the hidden layer is very complex.
- How to select and put in training data impacts the results. We choose to randomly pick up data from data sets and get a better result.
- The indexes of each X, weight, and δ are also confusing. It will be easy to make mistake when choosing which value to be calculate during implementation.

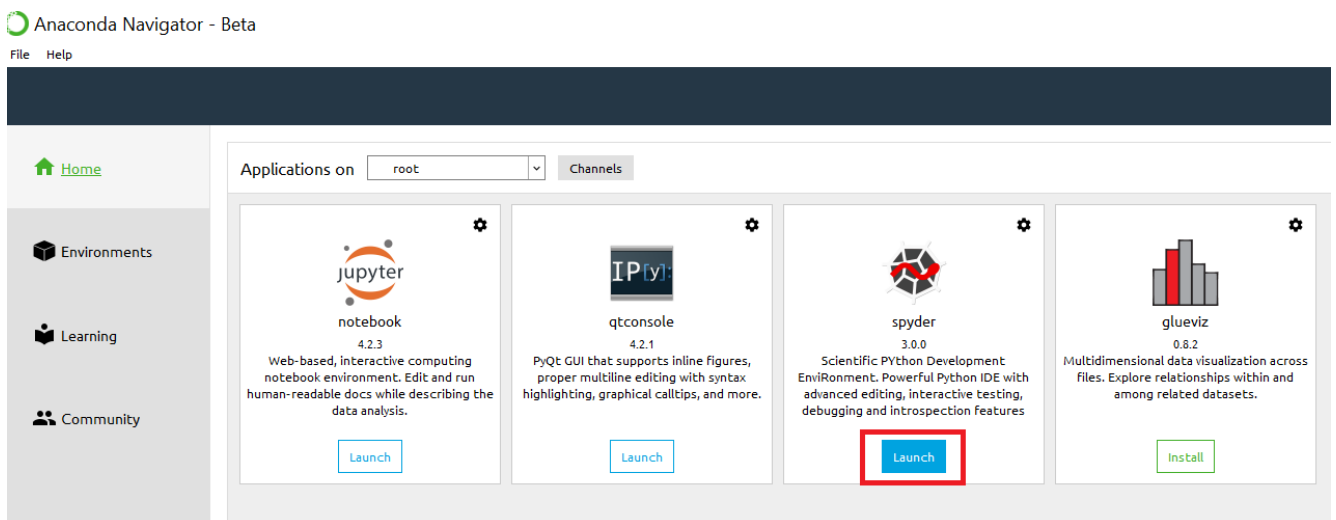


6.2 Script Files and Dataset File in same folder

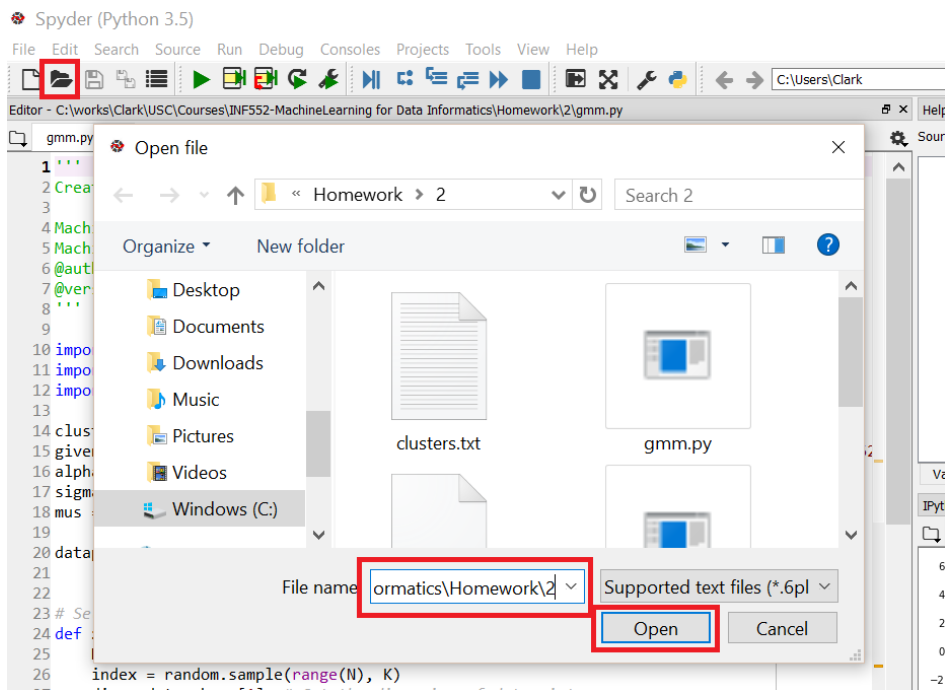
- NeuralNetwork.py (Implementation code)
- downgesture_train.list (List of training data sets for Neural Network algorithm)
- downgesture_test.list (List of testing data sets for Neural Network algorithm)
- gestures (Folder of data set)

6.3 Execution from Spyder version 3.0

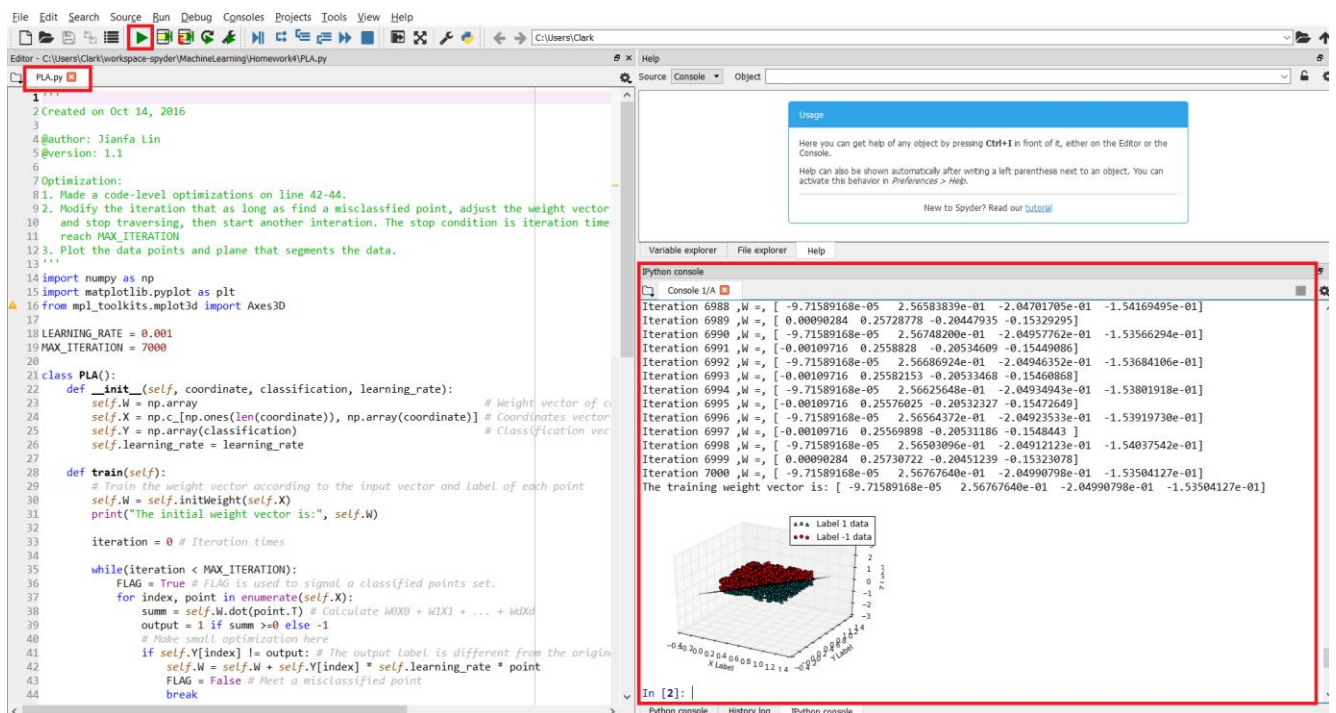
1. Under the “Home” of Anaconda Navigator, Click “Launch” to enable spyder 3.0.0 environment.



2. In Spyder IDE, please select open file icon on tool bar and open implementation and testing files.



3. Please select the implementation code you want to execute, then click the “Run file” icon. The result will show in IPython console window.



6.4 Execution Results

This is the best result we get from our implementation. The accuracy reach around 95%.

Total input numbers= 184

Match(O)=>gestures/A/A_down_1.pgm: Predict=True, Output value=[1.]

Match(O)=>gestures/A/A_down_2.pgm: Predict=True, Output value=[1.]

Match(O)=>gestures/A/A_hold_1.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/A/A_hold_10.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/A/A_stop_1.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/A/A_stop_4.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/A/A_up_1.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/A/A_up_10.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/B/B_down_1.pgm: Predict=True, Output value=[1.]
Match(O)=>gestures/B/B_down_2.pgm: Predict=True, Output value=[1.]
Match(O)=>gestures/B/B_hold_1.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/B/B_hold_2.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/B/B_stop_1.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/B/B_stop_2.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/B/B_up_1.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/B/B_up_4.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/C/C_down_1.pgm: Predict=True, Output value=[1.]
Match(O)=>gestures/C/C_down_2.pgm: Predict=True, Output value=[1.]
Match(O)=>gestures/C/C_hold_1.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/C/C_hold_2.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/C/C_stop_2.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/C/C_stop_3.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/C/C_up_1.pgm: Predict=False, Output value=[0.]
Match(X)=>gestures/D/D_down_1.pgm: Predict=False, Output value=[0.]
Match(X)=>gestures/D/D_down_2.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/D/D_hold_1.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/D/D_hold_2.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/D/D_hold_6.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/D/D_stop_1.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/D/D_stop_2.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/D/D_up_1.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/D/D_up_3.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/E/E_down_1.pgm: Predict=True, Output value=[1.]
Match(O)=>gestures/E/E_hold_1.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/E/E_hold_5.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/E/E_stop_1.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/E/E_stop_2.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/E/E_up_1.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/E/E_up_2.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/F/F_down_1.pgm: Predict=True, Output value=[1.]
Match(O)=>gestures/F/F_down_4.pgm: Predict=True, Output value=[1.]
Match(O)=>gestures/F/F_hold_1.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/F/F_hold_2.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/F/F_stop_2.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/F/F_stop_5.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/G/G_down_2.pgm: Predict=True, Output value=[1.]
Match(X)=>gestures/G/G_down_3.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/G/G_hold_4.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/G/G_stop_2.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/G/G_stop_5.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/G/G_up_2.pgm: Predict=False, Output value=[0.]

Match(O)=>gestures/G/G_up_5.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/H/H_down_2.pgm: Predict=True, Output value=[1.]
Match(O)=>gestures/H/H_hold_10.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/H/H_hold_2.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/H/H_hold_5.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/H/H_stop_5.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/H/H_stop_6.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/H/H_up_5.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/I/I_hold_2.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/I/I_hold_5.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/I/I_down_3.pgm: Predict=True, Output value=[1.]
Match(O)=>gestures/I/I_stop_5.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/I/I_stop_6.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/I/I_up_2.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/I/I_up_3.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/J/J_down_5.pgm: Predict=True, Output value=[1.]
Match(X)=>gestures/J/J_down_6.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/J/J_hold_2.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/J/J_hold_3.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/J/J_stop_7.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/J/J_stop_8.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/J/J_up_1.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/J/J_up_2.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/K/K_down_2.pgm: Predict=True, Output value=[1.]
Match(O)=>gestures/K/K_down_3.pgm: Predict=True, Output value=[1.]
Match(O)=>gestures/K/K_hold_1.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/K/K_hold_2.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/K/K_hold_3.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/K/K_stop_1.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/K/K_stop_2.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/K/K_stop_1.pgm: Predict=False, Output value=[0.]
Match(O)=>gestures/K/K_stop_2.pgm: Predict=False, Output value=[0.]
Accuracy: correct rate: 95.18072289156626%

7 Software Familiarization

7.1 Overview

As previous describe, we find a good data science platform, Anaconda, which includes major open source of Python libraries for data science. The latest version as of Oct., 1, 2016 is 4.2.0. The platform includes IDE (Integrated Development Environment), Python open source library management for developer to build up their own code.

Under this environment, a clustering testing code implements base on Numpy library, scikit-learn library, and matplotlib library as a comparison to our implementations.

7.2 Perceptron algorithm in scikit-learn library

7.2.1 API introduction^[4]

In the linear model, a perceptron algorithm is available for use. *Perceptron* and *SGDClassifier* share the same underlying implementation. In fact, *Perceptron()* is equivalent to *SGDClassifier(loss="perceptron", eta0=1, learning_rate="constant", penalty=None)*.

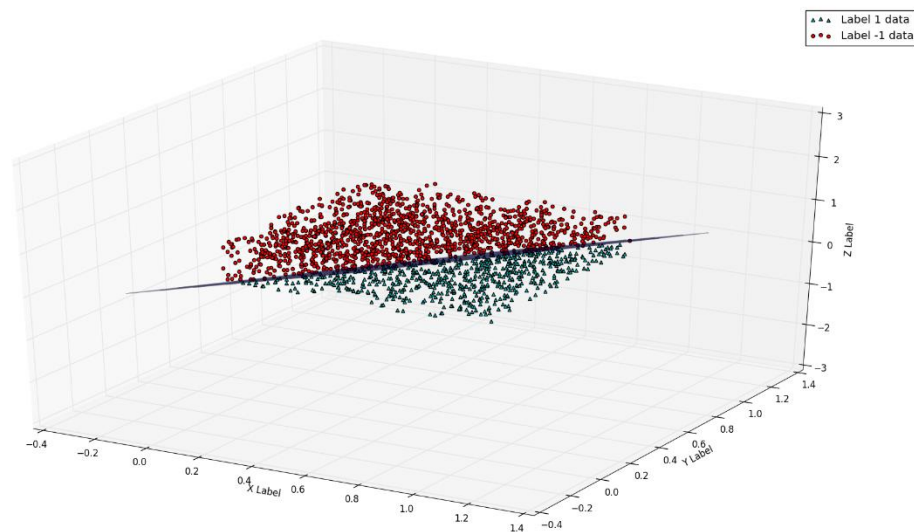
There are several interesting parameters can be assigned into this implementation.

1. "alpha": learning rate, default is 0.0001
2. "n_iter": maximum iteration number can be restricted. Default is 5.
3. "class_weight": the parameter provides user a chance to provide initial weight vector for your data. Default is weight one for all classes.
4. "warm_start": When set to True, reuse the solution of the previous call to fit as initialization. Otherwise, just erase the previous solution.
5. "score()": Returns the mean accuracy on the given test data and labels.

7.2.2 Execution results

The best result after 10 trials as below, the result is the same as the best results of our implementation:

```
{'warm_start': False, 'random_state': 0, 'shuffle': True, 'verbose': 0, 'n_jobs': 1,
'eta0': 1.0, 'penalty': None, 'fit_intercept': True, 'class_weight': None, 'n_iter': 200,
'alpha': 0.0001}
score = 1.0
W= [[ 0.          54.64874766 -43.75947362 -32.77355205]]
```



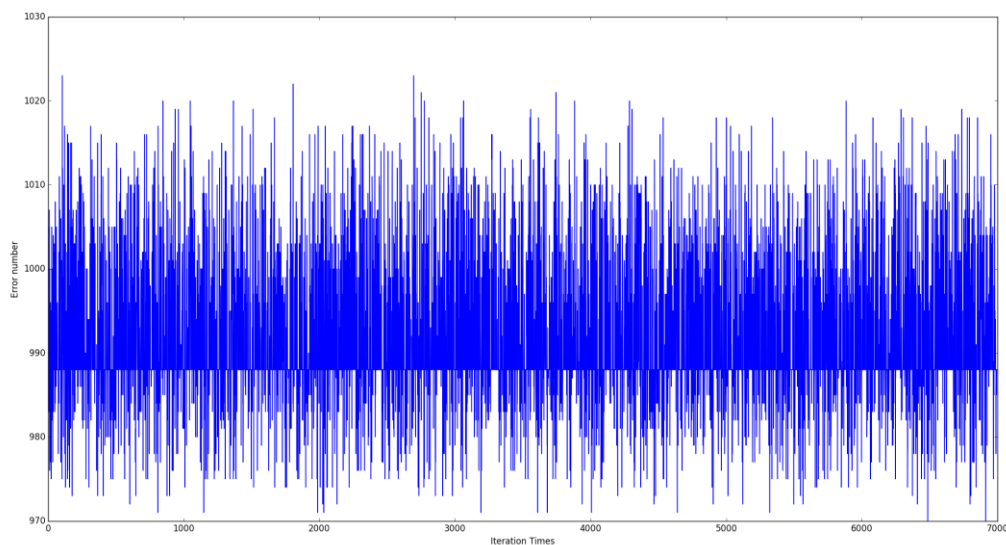
7.3 Pocket algorithm in scikit-learn library

7.3.1 introduction[\[4\]](#)

Due to there is no Pocket algorithm implementation in scikit-learn library. We leverage Perceptron implementation and set the warm_start as True and the n_iter = 1 for 7000 times to calculate error number via score and total data number.

The result as below for reference:

```
{'warm_start': True, 'random_state': 0, 'shuffle': True, 'verbose': 0, 'n_jobs': 1,
'eta0': 1.0, 'penalty': None, 'fit_intercept': True, 'class_weight': None, 'n_iter': 1,
'alpha': 0.0001}
score = 0.515
W= [[-1.          -0.64196622 -0.73630825 -0.63632897]]
```



7.4 Logistic Regression Algorithm in scikit-learn library

7.4.1 API Introduction[\[5\]](#)

There are several interesting parameters can be assigned into this implementation.

1. “tol”: Tolerance for stopping criteria, Default is 1e-4.
2. “solver”: {‘newton-cg’, ‘lbfgs’, ‘liblinear’, ‘sag’}, different algorithm to use in the optimization problem. For small dataset, ‘liblinear’ is good choice, whereas ‘sag’ is faster for large ones. For multiclass problems, only ‘newton-cg’, ‘sag’, and ‘lbfgs’ handle. Default: ‘liblinear’ is limited to one-versus-rest schemes.
3. “max_iter”: maximum iteration number can be restricted. Default is 100.
4. “warm_start”: If warm_start is true; the solution of the last fitting is used as initialization for the next call. It will speed up convergence when developer repeat called several time on similar problems. The default value is False.
5. “n_init”: the number of trials will perform. The best results are kept. Default value is 1.

7.4.2 Execution results

```
{'fit_intercept': True, 'max_iter': 100, 'solver': 'liblinear', 'C': 1.0, 'n_jobs': 1,
'dual': False, 'verbose': 0, 'penalty': 'l2', 'tol': 0.0001, 'class_weight': None,
'warm_start': False, 'intercept_scaling': 1, 'multi_class': 'ovr', 'random_state': None}
score = 0.5295
```

```
W= [[-0.01550526 -0.17376308  0.11159028  0.07474653]]
```

7.5 Linear Regression Algorithm in scikit-learn library

7.5.1 API Introduction[\[6\]](#)

There are several interesting parameters can be assigned into this implementation. But there is no weight vector can be printed by the API, instead, a predict(X) function provides for results prediction and plot the diagram.

6. “fit_intercept”: Boolean, optional. Where to calculate the intercept for this model.
7. “normalize”: Boolean, optional, default is False. If it is True, the regressors X will be normalized before regression. This parameter is ignored when the fit_intercept is set to Faluse.
8. “coef_”: Estimated coefficients for the linear regression problem.
9. “fit(X, y, sample_weight=None)”: X is training data, y is target values, sample_weight can provide by user or not.
10. “predict(X)”: Predict using the linear model
11. “score()”: Returns the coefficient of determination R^2 of the prediction.

7.6 How to improve our implementation

7.6.1 Improvement opportunities on Perceptron Learning and Pocket Algorithms

1. Improve the random point selection. We can improve our code to automatic generate different weight vectors and learning rate to get the best result in different variables combination.

7.6.2 Improvement opportunities on Logistic Regression Algorithm

1. We may implement the coverage function which taught in class and do a comparison between the two different coverage functions and the results.
2. Add an option to user to choose different functions.

7.6.3 Improvement opportunities on Linear Regression Algorithm

3. We may implement the coverage function for singular matrix data input to make the solution more complete.

8 Application

8.1 The applications on Perceptron Learning and Pocket Algorithm.

Except on traditional binary data classification, like credit card application question. Perceptron learning generalizes naturally to multiclass classification. In recent years, perceptron training has become popular in the field of natural language processing for such tasks as text categorization [\[7\]](#).

8.2 The application on Logistic Regression Algorithm.

Logistic regression algorithm is widely applied in business, like measure the success rates of marketing campaigns. An interesting application is in GIS-based application. Especially in regional hazard management, multivariate statistical analysis in the form of logistic regression was used to produce a landslide susceptibility map in specific areas [\[8\]](#), sometimes frequency ratio model is used to compare with logistic regression algorithm [\[9\]](#).

8.3 The applications on Linear Regression Algorithm.

Linear regression algorithm is an important numerical method for linear least squares problem because it is one of the most important types of model in statistics. A lot of business questions like “evaluating trends and sales estimation” or “analysing the impact of price changes and sales”. Biometrical procedure for testing the equality of measurements [\[10\]](#), researcher will use linear regression procedure as a method comparison studies in clinical chemistry.

9 Reference

- [1] Alpaydin E. Introduction to machine learning[M]. MIT press, 2014.
- [2] Andrew Ng, Machine Learning Course Materials. URL <http://cs229.stanford.edu/notes/cs229-notes1.pdf>, page 11~13.
- [3] Chih-Hao's Blog, URL <http://zhihaozhang.github.io/2016/03/17/logisticRegression/>
- [4] scikit-learn, version 0.18, Perceptron, URL http://scikit-learn.org/stable/modules/generated/sklearn.linear_model.Perceptron.html
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- [6] scikit-learn, version 0.18, Linear Regression, URL http://scikit-learn.org/stable/modules/generated/sklearn.linear_model.LinearRegression.html
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