

**Theorem 3** Let  $(A_0, A_1, \dots, A_m)$  be a fitness partition of a finite state space  $\mathcal{X}$ . Let  $T := \min\{2t\lambda \mid |P_t \cap A_m| > 0\}$  be the first point in time that the elements of  $A_m$  appear in  $P_t$  of the 2-tournament EA with noisy function  $f^n(x)$  and mutation rate  $\chi/n$ . If there exist  $h_0, h_1, \dots, h_{m-1}$  and  $\theta \in (0, 1/2]$ , and where  $\chi \in (0, \ln(1 + 2\theta\zeta))$  for an arbitrary constant  $\zeta \in (0, 1)$ , such that, for an arbitrary constant  $\xi \in (0, 1/16)$ ,

(C1) for all  $j \in [0..m-1]$ ,  $\Pr(y \in A_{\geq j+1} \mid z \in A_j) \geq h_j$ ,

(C2) for all  $j \in [0..m-2]$ , and all search points  $x_1 \in A_{\geq j+1}$  and  $x_2 \in A_{\leq j}$ , it follows  $\Pr(f^n(x_1) > f^n(x_2)) + \frac{1}{2} \Pr(f^n(x_1) = f^n(x_2)) \geq \frac{1}{2} + \theta$ ,

(C3) and the population size  $\lambda \in \mathbb{N}$  satisfies

$$\lambda > \frac{4(1+o(1))}{\theta^2 \xi (1-\zeta)^4} \ln \left( \frac{128(m+1)}{\theta^2 \xi (1-\zeta)^4 \min\{h_j\}} \right),$$

then  $E[T] < \frac{16(1+o(1))}{\theta^2 \xi (1-\zeta)^2} \sum_{j=0}^{m-1} \left( \lambda \ln \left( \frac{6}{\xi (1-\zeta)^2 h_j} \right) + \frac{1}{\xi (1-\zeta)^2 h_j} \right)$ .