

1. d.

$$X = \begin{bmatrix} -2 \\ 0 \\ 2 \end{bmatrix} \quad y = \begin{bmatrix} -1 \\ 1 \\ -1 \end{bmatrix} \quad \phi(X) = \begin{bmatrix} 1 & -2 & 4 \\ 1 & 0 & 0 \\ 1 & 2 & 4 \end{bmatrix}$$

$$\begin{aligned} 2w_1 - 4w_2 - b &\geq 1 & 4w_1 &\geq 0 & -4w_2 &\geq 2 \\ b &\geq 1 & w_1 &\geq 0 & w_2 &\geq -\frac{1}{2} \\ -2w_1 - 4w_2 - b &\geq 1 \end{aligned}$$

2. b.

$$\frac{1}{\|w\|} = \frac{1}{\sqrt{w_1^2 + w_2^2}} = \frac{1}{\sqrt{\frac{1}{4}}} = 2 \quad \#$$

3. e

$$-\frac{1}{2} \left( \begin{array}{c} \leftarrow \quad \rightarrow \\ x_n \quad x_{n+1} \end{array} \right) + \frac{1}{2} (x_{n+1} - x_n)$$

5. c

$$\frac{1}{2} w^T w + \sum \partial_n (\rho - \gamma_n (w^T z_n + b)) \quad \frac{\partial L(b, w, \partial)}{\partial b} = 0 = -\sum \gamma_n \partial_n$$

$$\frac{1}{2} w^T w + \sum \partial_n (\rho - \gamma_n (w^T z_n)) \quad \gamma_n (w^T z_n + b) \geq \rho$$

$$\begin{aligned} -\frac{1}{2} \sum \|\partial_n \gamma_n z_n\|^2 + \sum \rho \partial_n & \quad \frac{\partial L(b, w, \partial)}{\partial w} = 0 = w_i - \sum \partial_n \gamma_n z_n \\ w &= \sum \partial_n \gamma_n z_n \end{aligned}$$

$$\min \frac{1}{2} \sum \|\partial_n \gamma_n z_n\|^2 - \sum \rho \partial_n$$

6. a.

$$\lambda \begin{cases} w = \sum \partial_n \gamma_n z_n \\ b = \gamma_n - w^T z_n \end{cases}$$

7. d.

$\log_2 K(x, x')$  非半正定矩陣

10. C

$$W_{t+1} \leftarrow \partial_t \phi(x) + \gamma \phi(x)$$

$$W_{t+1} \leftarrow \phi(x)(\partial_t + \gamma)$$

11. C

$$W \phi(x)$$

$$= \partial_n \gamma_n \phi(x) \phi(x)$$

$$= \gamma_n \partial_n K(x_n, x)$$

12. a.

$$\partial_n = C$$

$$\partial_n \underbrace{(1 - \xi - \gamma_n (w^T z_n + b))}_{=0} = 0$$

$$(C - \partial_n) \xi = 0$$

$$\xi = 1 - \gamma_n (w^T z_n + b) \rightarrow \text{violation amount}$$

15~20 X b e d b a

Read data

```
def read_data(file):
    f = open(file)
    data = f.read()
    f.close()

    all_data = []
    all_label = []
    for line in data.split("\n"):
        i = 0
        line_data = []
        for sub_line in line.split(" "):
            for value in sub_line.split(":"):
                if i == 0:
                    if value != "":
                        all_label.append(int(value))
                elif i != 0 and i % 2 == 0:
                    if value != "":
                        line_data.append(float(value))
                i += 1
            if line_data != []:
                all_data.append(line_data)
    return all_data, all_label

def redefine_label(label, class_number):
    new_label = []
    for i in range(len(label)):
        if label[i] == class_number:
            new_label.append(1)
        else:
            new_label.append(-1)
    return new_label

train_data, train_label = read_data("./train.txt")
test_data, test_label = read_data("./test.txt")
```

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```
train_label = redefine_label(train_label, 2)
test_label = redefine_label(test_label, 2)
m = svm_train(train_label, train_data, "-c 10 -t 1 -
d 2")
p_label, p_acc, p_val = svm_predict(train_label, train_
data, m)
```

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```
best_Eout = 100
best_c = 0
Cs = [0.01, 0.1, 1, 10, 100]
train_label = redefine_label(train_label, 6)
test_label = redefine_label(test_label, 6)
for c in Cs:
    m = svm_train(train_label, train_data, "-c %f -
t 2 -g 10" % c)
    p_label, p_acc, p_val = svm_predict(test_label, tes
t_data, m)
    print(p_acc[0])
    if 100 - p_acc[0] < best_Eout:
        best_Eout = 100 - p_acc[0]
        best_c = c
print("best:", best_Eout, best_c)
```

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```
best_Eout = 100
best_gamma = 10000
gammas = [0.1, 1, 10, 100, 1000]
train_label = redefine_label(train_label, 6)
test_label = redefine_label(test_label, 6)
for gamma in gammas:
    m = svm_train(train_label, train_data, "-c 0.1 -
t 2 -g %f" % gamma)
    p_label, p_acc, p_val = svm_predict(test_label, tes
t_data, m)
    print(p_acc[0])
    if 100 - p_acc[0] < best_Eout:
        best_Eout = 100 - p_acc[0]
        best_gamma = gamma
```

```
print("best:", best_Eout, best_gamma)
```

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```
def train_val_split(data, label, val_index):  
    train_data = []  
    train_label = []  
    val_data = []  
    val_label = []  
    for i in range(len(data)):  
        if i in val_index:  
            val_data.append(data[i])  
            val_label.append(label[i])  
        else:  
            train_data.append(data[i])  
            train_label.append(label[i])  
    return train_data, train_label, val_data, val_label
```

```
train_label = redefine_label(train_label, 6)  
test_label = redefine_label(test_label, 6)  
all_index = np.arange(0, len(train_data))  
val_index = random.sample(range(0, len(train_data)), 20  
0)  
train_data, train_label, val_data, val_label = train_val_split(  
    train_data, train_label, val_index)
```

```
gammas = [0.1, 1, 10, 100, 1000]  
smallest_gamma = []
```

```
best_Eout = 100  
best_gamma = 10000  
for epoch in range(10):  
    print(epoch)  
    for gamma in gammas:  
        m = svm_train(train_label, train_data, "-  
c 0.1 -t 2 -g %f" % gamma)  
        p_label, p_acc, p_val = svm_predict(val_label,  
val_data, m)  
        if 100 - p_acc[0] <= best_Eout:
```

```
        if gamma < best_gamma:
            best_gamma = gamma
        smallest_gamma.append(best_gamma)
print(smallest_gamma)
counts = np.bincount(smallest_gamma)
print(np.argmax(counts))
```