

LinearSys

- 1) Basic Parameter setting
Var: params -- struct
[1] P48

.tStart initial time t0 (default value 0)

.tFinal final time tf

.R0 initial set X0 specified by one of the set representations

.U input set U specified as an object of class zonotope

etc.
- 2) Reachability Settings
Var: options -- struct
[1] P56
only for linearSys

.linAlg string specifying the reachability algorithm that is used — **** important**

.timeStep time step size required for all algorithms

.taylorTerms number of Taylor terms for the computation of the exponential matrix $e^{(A*\delta_t)}$ — **** determine the accuracy**

.zonotopeOrder upper bound for the zonotope order p

.error upper bound for the error containing over-approximative terms — only for adaptive mode

3) Define systems — linearSys -- inherit from contDynamics
[1] P56

- 4) Reachability analysis

(1) Preprocessing options — autofill the missing elements in options

(2) Do reachability analysis in different modes
 - standard
 - wrapping free
 - adaptive
 - etc.

Var: uTrans|uTransVec -- input set U and input vector

Ref:
[1] CORA document
[2] PhD thesis from Prof. Althoff
[3] Reachable Set Computation for Uncertain Time-Varying Linear Systems

Important value:
Rfirst.tp -- time point
Rfirst.ti -- time interval

- Standard RA

(1) Func: initReach_Euclidean
get the initial reachable set

Func: exponential [3] P4 — compute $e^{(A*\delta_t)}$ with the error term W — Important value: obj.taylor.power -- value; obj.taylor.error -- error

Func: tie [2] P34 — compute the correction matrix; to make sure that all the trajectory from the initial set can be detected. — Important value: F

Func: inputSolution [2] P35
 - compute reachable set due to input
 - Asum and Vsum all come from [2] P36 (3.7)
 - overall solution [2] P36 — compute the constant solution (Asum) and solution with 0-contained set (Vsum)
 - inputTie — compute the input time interval error

Func: enclose [2]

Func: reduce [2]

(2) Func: initOutputEquation
initialize parameter for the output equation

(3) Loop: — using the previous step to compute the next solution, the results are stored into Rout

Important value:
RV (inputSolV): overall solution
eAtInt: solution due to constant input
inputF: F of input
inputCorr: input correction
Rtrans (inputSolVtrans): solution due to constant input

- wrapping-free

warpping effect [2] P37 — The over-approximation error is propagated through the computations at later time steps

(1) Func: initReach_Euclidean
get the initial reachable set — same

(2) using algorithm 2 in [2] P37 to compute reachable set