



## Chapter 2: Intro to Relational Model

- **Data model:** a collection of conceptual tools for describing data, data relationships, data semantics, and consistency constraints.
- **Relational Model:** is the most widely used model today.
  - **Main concept:** relation, basically a table with rows and columns.

Database System Concepts, 6<sup>th</sup> Ed.

©Silberschatz, Korth and Sudarshan

See [www.db-book.com](http://www.db-book.com) for conditions on re-use



# Example of a Relation

<i>ID</i>	<i>name</i>	<i>dept_name</i>	<i>salary</i>
10101	Srinivasan	Comp. Sci.	65000
12121	Wu	Finance	90000
15151	Mozart	Music	40000
22222	Einstein	Physics	95000
32343	El Said	History	60000
33456	Gold	Physics	87000
45565	Katz	Comp. Sci.	75000
58583	Califieri	History	62000
76543	Singh	Finance	80000
76766	Crick	Biology	72000
83821	Brandt	Comp. Sci.	92000
98345	Kim	Elec. Eng.	80000

attributes  
(or columns)

tuples  
(or rows)

**Figure 2.1** The *instructor* relation.



# Attribute Domain Types

- The set of allowed values for each attribute is called the **domain** of the attribute
- Attribute values are (normally) required to be **atomic**; that is, indivisible
- The special value ***null*** is a member of every domain
  - The null value causes **complications** in the definition of many operations



# Relation Schema and Instance

## ■ *Relation Schema*

- $A_1, A_2, \dots, A_n$  are *attributes*
- $R = (A_1, A_2, \dots, A_n)$  is a *relation schema*

Example:

*instructor* = (*ID*, *name*, *dept\_name*, *salary*)

## ■ *Relation Instance*

- **Formally**, given sets  $D_1, D_2, \dots, D_n$  . a **relation instance**  $r$  is a subset of  $D_1 \times D_2 \times \dots \times D_n$

Thus, a relation is a set of  $n$ -tuples  $(a_1, a_2, \dots, a_n)$  where each  $a_i \in D_i$

- **relation** vs. **table**

- The current values (**relation instance**) of a relation are specified by a table
- An element  $t$  of  $r$  is a *tuple*, represented by a *row* in a table



# Relations are Unordered

- Order of tuples is irrelevant (tuples may be stored in an arbitrary order)
- Example: *instructor* relation with unordered tuples

ID	name	dept_name	salary
22222	Einstein	Physics	95000
12121	Wu	Finance	90000
32343	El Said	History	60000
45565	Katz	Comp. Sci.	75000
98345	Kim	Elec. Eng.	80000
76766	Crick	Biology	72000
10101	Srinivasan	Comp. Sci.	65000
58583	Califieri	History	62000
83821	Brandt	Comp. Sci.	92000
15151	Mozart	Music	40000
33456	Gold	Physics	87000
76543	Singh	Finance	80000

ID	name	dept_name	salary
10101	Srinivasan	Comp. Sci.	65000
12121	Wu	Finance	90000
15151	Mozart	Music	40000
22222	Einstein	Physics	95000
32343	El Said	History	60000
33456	Gold	Physics	87000
45565	Katz	Comp. Sci.	75000
58583	Califieri	History	62000
76543	Singh	Finance	80000
76766	Crick	Biology	72000
83821	Brandt	Comp. Sci.	92000
98345	Kim	Elec. Eng.	80000



# Database

- A database consists of multiple relations
- 例: Information about an enterprise is broken up into parts

*instructor*

*student*

*advisor*

- **Bad** design:  
*univ (instructor -ID, name, dept\_name, salary, student\_Id, ..)*  
results in

- repetition of information (e.g., two students have the same instructor)
- the need for null values (e.g., represent an student with no advisor)

- Normalization theory (Chapter 7) deals with how to design “good” relational schemas

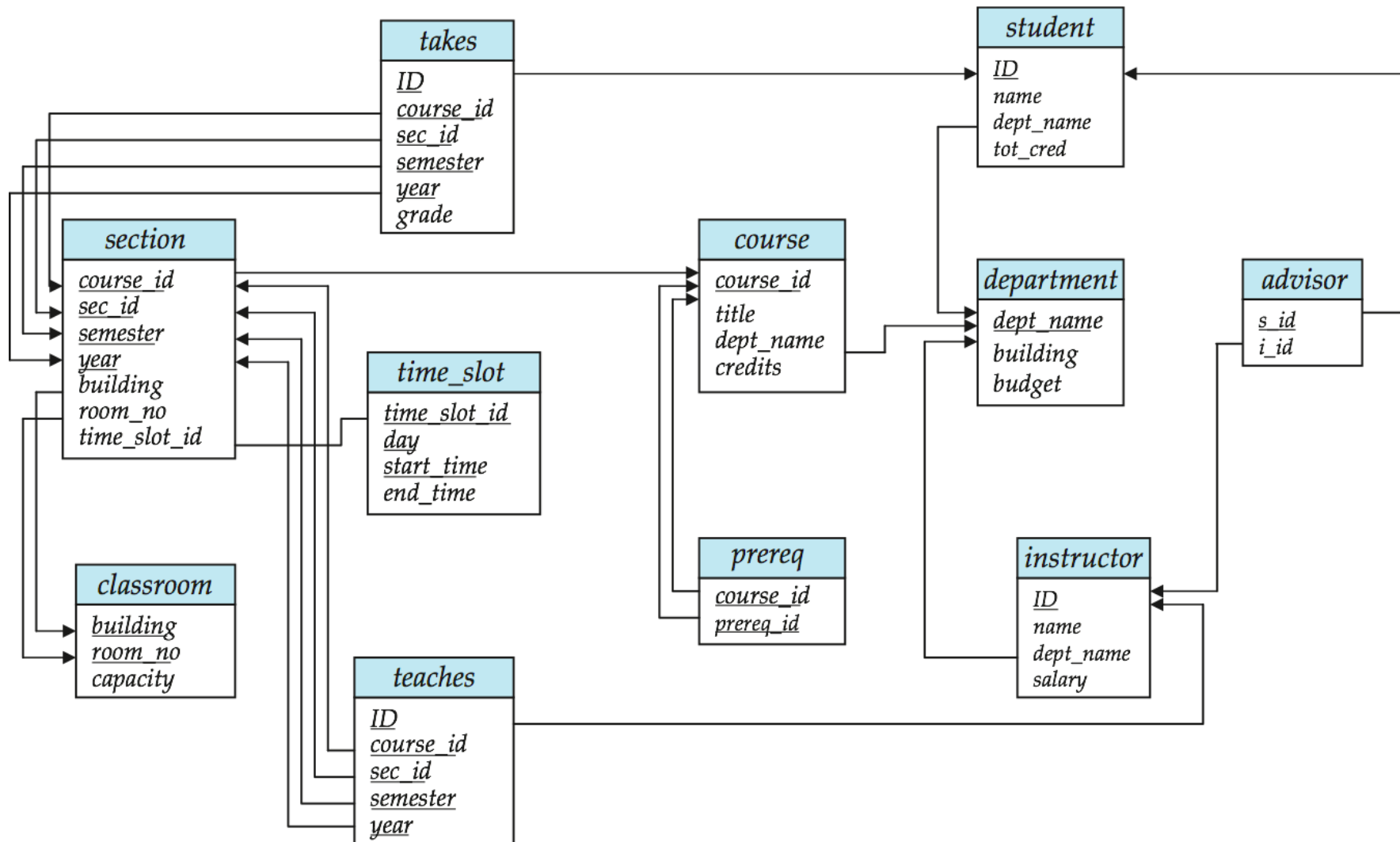


# Keys

- Let  $K \subseteq R$
- $K$  is a **superkey** of  $R$  if values for  $K$  are sufficient to identify a unique tuple of each possible relation  $r(R)$ 
  - Example:  $\{ID\}$  and  $\{ID, name\}$  are both superkeys of *instructor*.
- Superkey  $K$  is a **candidate key** if  $K$  is minimal  
Example:  $\{ID\}$  is a candidate key for *Instructor*
- One of the candidate keys is selected to be the **primary key**.
  - which one?
- **Foreign key** constraint: Value in one relation must appear in another
  - **Referencing** relation
  - **Referenced** relation



# Schema Diagram for University Database







# Relational Query Languages

- Procedural vs. non-procedural, or declarative
  - Query languages **used in practice** include elements of **both the procedural and the nonprocedural** approaches, such as SQL.
- “Pure” languages:
  - Relational algebra
  - Tuple relational calculus
  - Domain relational calculus



# Relational operators

Symbol (Name)	Example of Use
$\sigma$ (Selection)	$\sigma_{\text{salary} \geq 85000}(\text{instructor})$
	Return rows of the input relation that satisfy the predicate.
$\Pi$ (Projection)	$\Pi_{ID, salary}(\text{instructor})$
	Output specified attributes from all rows of the input relation. Remove duplicate tuples from the output.
$\bowtie$ (Natural Join)	$\text{instructor} \bowtie \text{department}$
	Output pairs of rows from the two input relations that have the same value on all attributes that have the same name.
$\times$ (Cartesian Product)	$\text{instructor} \times \text{department}$
	Output all pairs of rows from the two input relations (regardless of whether or not they have the same values on common attributes)
$\cup$ (Union)	$\Pi_{name}(\text{instructor}) \cup \Pi_{name}(\text{student})$
	Output the union of tuples from the two input relations.



# Selection of tuples

- Relation r

A	B	C	D
$\alpha$	$\alpha$	1	7
$\alpha$	$\beta$	5	7
$\beta$	$\beta$	12	3
$\beta$	$\beta$	23	10

- Select tuples with A=B  
and D > 5

- $\sigma_{A=B \text{ and } D > 5}(r)$

A	B	C	D
$\alpha$	$\alpha$	1	7
$\beta$	$\beta$	23	10



# Selection of Columns (Attributes)

- Relation  $r$ :

A	B	C
$\alpha$	10	1
$\alpha$	20	1
$\beta$	30	1
$\beta$	40	2

- Select A and C
  - Projection
  - $\Pi_{A, C}(r)$

A	C
$\alpha$	1
$\alpha$	1
$\beta$	1
$\beta$	2

=

A	C
$\alpha$	1
$\beta$	1
$\beta$	2



# Joining two relations – Cartesian Product

■ Relations  $r, s$ :

$A$	$B$
$\alpha$	1
$\beta$	2

$r$

$C$	$D$	$E$
$\alpha$	10	a
$\beta$	10	a
$\beta$	20	b
$\gamma$	10	b

$s$

■  $r \times s$ :

$A$	$B$	$C$	$D$	$E$
$\alpha$	1	$\alpha$	10	a
$\alpha$	1	$\beta$	10	a
$\alpha$	1	$\beta$	20	b
$\alpha$	1	$\gamma$	10	b
$\beta$	2	$\alpha$	10	a
$\beta$	2	$\beta$	10	a
$\beta$	2	$\beta$	20	b
$\beta$	2	$\gamma$	10	b



# Union of two relations

- Relations  $r, s$ :

$A$	$B$
$\alpha$	1
$\alpha$	2
$\beta$	1

$r$

$A$	$B$
$\alpha$	2
$\beta$	3

$s$

- $r \cup s$ :

$A$	$B$
$\alpha$	1
$\alpha$	2
$\beta$	1
$\beta$	3



# Set difference of two relations

- Relations  $r$ ,  $s$ :

$A$	$B$
$\alpha$	1
$\alpha$	2
$\beta$	1

$r$

$A$	$B$
$\alpha$	2
$\beta$	3

$s$

- $r - s$ :

$A$	$B$
$\alpha$	1
$\beta$	1



# Set Intersection of two relations

- Relation  $r, s$ :

$A$	$B$
$\alpha$	1
$\alpha$	2
$\beta$	1

$r$

$A$	$B$
$\alpha$	2
$\beta$	3

$s$

- $r \cap s$

$A$	$B$
$\alpha$	2





# Joining two relations – Natural Join

- Let  $r$  and  $s$  be relations on schemas  $R$  and  $S$  respectively. Then, the “natural join” of relations  $R$  and  $S$  is a relation on schema  $R \cup S$  obtained as follows:
  - Consider each pair of tuples  $t_r$  from  $r$  and  $t_s$  from  $s$ .
  - If  $t_r$  and  $t_s$  have the same value on each of the attributes in  $R \cap S$ , add a tuple  $t$  to the result, where
    - ▶  $t$  has the same value as  $t_r$  on  $r$
    - ▶  $t$  has the same value as  $t_s$  on  $s$



# Natural Join Example

- Relations  $r$ ,  $s$ :

$A$	$B$	$C$	$D$
$\alpha$	1	$\alpha$	a
$\beta$	2	$\gamma$	a
$\gamma$	4	$\beta$	b
$\alpha$	1	$\gamma$	a
$\delta$	2	$\beta$	b

$r$

$B$	$D$	$E$
1	a	$\alpha$
3	a	$\beta$
1	a	$\gamma$
2	b	$\delta$
3	b	$\epsilon$

$s$

- Natural Join

- $r \bowtie s$

$A$	$B$	$C$	$D$	$E$
$\alpha$	1	$\alpha$	a	$\alpha$
$\alpha$	1	$\alpha$	a	$\gamma$
$\alpha$	1	$\gamma$	a	$\alpha$
$\alpha$	1	$\gamma$	a	$\gamma$
$\delta$	2	$\beta$	b	$\delta$



# End of Chapter 2

**Database System Concepts, 6<sup>th</sup> Ed.**

©Silberschatz, Korth and Sudarshan

See [www.db-book.com](http://www.db-book.com) for conditions on re-use