Sovereign Default with Bounded Rationality

[INCOMPLETE AND COMMENTS WELCOME]

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June 11, 2025

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Motivation

Motivation

The Stylized Facts:

- Emerging market sovereign spreads
 high and extremely volatile
- Crises ⇒ sudden spikes in spreads
- Standard models generated spreads ⇒ too low and too smooth

Gap in Literature:

 Most of the papers in this literature assume full rationality

Figure 1: Argentina's Spread (1983-2003)



Data Source: (Arellano, 2008)

A Model with Bounded Rationality

This paper: Relax the full rationality assumption \implies **heterogeneous** Lenders

Boundedly rational agents (Information & Cognitive Costs ⇒ Heuristic decision)

Key Results:

Theoretical: Endogenous price discontinuity

· A new mechanism for sudden crises

Quantitative: Match high average spreads AND

- Extreme spread volatility
- Higher financial fragility (more debt & defaults)

Model

Model Setup

A small open economy with AR(1) potential output stream $\{y_t\}_{t=0}^{\infty}$:

$$\ln(y_{t+1}) = \rho \ln(y_t) + \varepsilon_{t+1}$$
, where $\varepsilon_{t+1} \sim N(0, \sigma_{\varepsilon}^2)$

described by a kernel p(y', y)

The government maximizes:

$$\mathbb{E}_{0}\left[\sum_{t=0}^{\infty}\beta^{t}u\left(c_{t}\right)\right]$$

The government smooth consumption by borrowing from (and lending to) foreign creditors

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Government & Financial Market

The Sovereign Government

Decision: Default or Repay?

- If Default:
 - Output cost: $y \rightarrow h(y) \le y$
 - · Excluded from credit markets
 - Re-entry with probability θ each period
- If Repay:
 - · Honors current debt B
 - Chooses next period's assets B'

Budget Constraint (when repaying):

$$c = y + B - q(B', y)B'$$

The Financial Market

- Lenders: Competitive & Risk-Neutral
- Asset: One-period, non-contingent bond
- The Bond Pricing Equation:

$$q(B', y) = \frac{1 - \delta(B', y)}{1 + r}$$
 (1)

 $\delta(B',y)$: probability of default on the new debt B'

Recursive Government's Problem

The Value of Default, $V^D(y)$

$$V^{D}(y) = u(h(y)) + \beta \mathbb{E}_{y'} \left[\theta V(0, y') + (1 - \theta) V^{D}(y') | y \right]$$
 (2)

The Value of Repayment, $V^R(B, y)$

$$V^{R}(B,y) = \max_{B' > -Z} \left\{ u \left(y + B - q(B',y)B' \right) + \beta \mathbb{E}_{y'}[V(B',y')|y] \right\}$$
 (3)

The Optimal Decision & Overall Value Function, V(B, y)

Defaults if and only if $V^D(y) > V^R(B, y)$

$$V(B,y) = \max \left\{ V^{R}(B,y), V^{D}(y) \right\}$$
 (4)

Default Probability with λ **-Rationality**

Assuming the market consists of two types of lenders:

Fraction λ : Rational Lenders

$$\delta_{r}(B',y) = \mathbb{E}_{y'}\left[\mathbb{I}_{\{V^{D}(y')>V^{R}(B',y')\}}|y\right] = \int \mathbb{I}_{\{\dots\}}p(y,y')dy'$$
(5)

Fraction $(1 - \lambda)$: Boundedly Rational Lenders

Motivation: Information & cognitive costs

$$\delta_{ir}(B',y) = \mathbb{I}_{\{V^D(\mathbb{E}[y'|y]) > V^R(B',\mathbb{E}[y'|y])\}}$$
(6)

Aggregate Market Belief

The weighted average of the two groups' beliefs

$$\delta(\mathbf{B}', \mathbf{y}; \lambda) = \lambda \delta_{\mathbf{r}}(\mathbf{B}', \mathbf{y}) + (1 - \lambda) \delta_{i\mathbf{r}}(\mathbf{B}', \mathbf{y})$$
(7)



The Discontinuous Price Schedule

Bounded rationality \implies "price cliff"

Theorem

With a fraction $(1 - \lambda) > 0$ of boundedly rational lenders, the equilibrium bond price schedule $\mathbf{q}(\mathbf{B}', \mathbf{y}; \lambda)$ has a unique discontinuity at a critical debt threshold $\tilde{\mathbf{B}}'(\mathbf{y})$. Specifically:

The price drop at the threshold

$$\lim_{B'\to \tilde{B}'(y)^+} q(B',y;\lambda) - \lim_{B'\to \tilde{B}'(y)^-} q(B',y;\lambda) = \frac{1-\lambda}{1+r}$$

- For "safe" debt levels (B' > $\tilde{B}'(y)$), $q(B',y;\lambda) \ge q(B',y;1)$
- For "risky" debt levels (B' < $\tilde{B}'(y)$), $q(B',y;\lambda) \le q(B',y;1)$

Intuition: Shift in the beliefs of boundedly rational lenders \implies sudden drop in the market price

Implications & Dynamics

Implication 1: Endogenous Interest Rate Spikes

Corollary

For adverse states (B, y) where $B' < \tilde{B}'(y)$, the resulting interest rate

$$r^{c}(B,y) = \frac{1}{q(B'(B,y),y;\lambda)} - 1$$

is **strictly higher** than in the fully rational benchmark

Implication 2: State-Dependent Financial Fragility

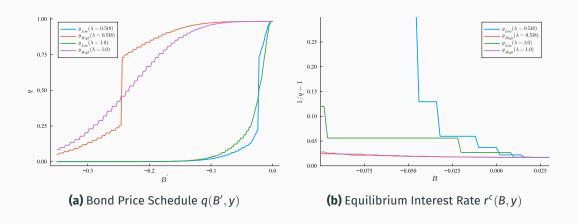
Proposition

The critical debt threshold $\tilde{B}'(y)$ is **decreasing** in y, i.e., $\frac{dB'(y)}{dy} < 0$

Intuition: In good times \implies lenders are more optimistic \implies the government sustain more debt before a crisis is triggered

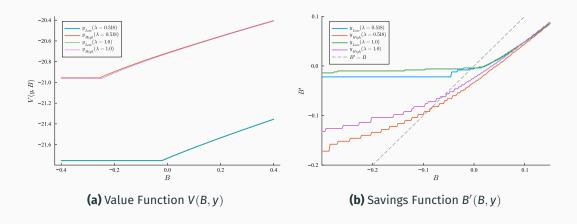


Price Drop & Interest Rate Spike



In adverse states (low y, high initial debt B) \Longrightarrow "forced" over the cliff \Longrightarrow **high** equilibrium interest rates

Equilibrium Policy & Financial Fragility



Negligible "value effect" + the "price effect" dominates \implies more aggressive borrowing \implies endogenously more **fragile**

Recap

Summary & Key Takeaways

A New Mechanism for Sudden Crisis

Heterogeneous lender beliefs \implies both rational and boundedly rational agents

Endogenous "Price Cliff"

Endogenously generates a discontinuous bond price schedule

Resolving the Spread Puzzles

Can match the high average spreads observed in emerging markets

Endogenous Financial Fragility

"Cheap" credit offered by optimistic lenders \implies induced to borrow more aggressively \implies endogenously more fragile