Network Homework 6

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Part I Background

In this project, we are going to use dynamic network model to simulate data and analysis. The network that can change over time (or we can say the network have multi-status) can be seen as dynamic network. It is based on the ERGMs and it can grow or shrink (in terms of nodes).

Also, the package we are going to use in this project is RSiena. The package can be used to deal with longtitude network data. There is a basic network variable and also there is a behavior variable that is a dependent variable. It is a node characteristic that changes over time, the evolution of which may considered in a co-evolutionary model.

By using the simulated model and data, we can get two models and analysis those results and statistics. And if the t-ratio is smaller than 0.1 (absolute value), it should be converge and 0.15 is reasonable. Four significant, we divide the estimation by standard error and the result should be larger than four, so it should be significant.

Part II Question I

At first, we extracted four period network data from whole data.

```
fr_w1=Coevolve$fr_w1
fr_w2=Coevolve$fr_w2
fr_w3=Coevolve$fr_w3
fr_w4=Coevolve$fr_w4
```

Then we operated them into another network data by using sienaDependent.

```
w1 <- cbind(get.edgelist(fr_w1), 1)
w2 <- cbind(get.edgelist(fr_w2), 1)
w3 <- cbind(get.edgelist(fr_w3), 1)
w4 <- cbind(get.edgelist(fr_w4), 1)
w1s <- spMatrix(37, 37, w1[,1], w1[,2], w1[,3])
w2s <- spMatrix(37, 37, w2[,1], w2[,2], w2[,3])
w3s <- spMatrix(37, 37, w3[,1], w3[,2], w3[,3])
w4s <- spMatrix(37, 37, w4[,1], w4[,2], w4[,3])
fr4wav2 <- sienaDependent(list(w1s,w2s,w3s,w4s))
fr4wav2</pre>
```

```
smoke <- array(
   c(V(fr_w1)$smoke, V(fr_w2)$smoke,
      V(fr_w3)$smoke, V(fr_w4)$smoke),
   dim=c(37,4))
smokebeh <- sienaDependent(smoke,
   type = "behavior")
smokebeh</pre>
```

```
· ```{r}
friend <- sienaDataCreate(fr4wav,smokebeh,gender)</pre>
friend
 Dependent variables: fr4wav, smokebeh
 Number of observations: 4
 Nodeset
                            Actors
 Number of nodes
                                37
 Dependent variable fr4wav
 Type
                     oneMode
 Observations
 Nodeset
                     Actors
 Densities
                     0.13 0.13 0.13 0.13
 Dependent variable smokebeh
 Type
                     behavior
 Observations
 Nodeset
                     Actors
                     0 - 1
 Range
```

So we get the data friend

```
```{r}
frndeff <- getEffects(friend)</pre>
frndeff
 include fix
 effectName
 test initialValue parm
 name
1 fr4wav constant fr4wav rate (period 1) TRUE FALSE FALSE
 2.00405
2 fr4wav constant fr4wav rate (period 2) TRUE
 FALSE FALSE
 2.00405
 0
3 fr4wav constant fr4wav rate (period 3) TRUE
 FALSE FALSE 2.00405
 0
4 fr4wav outdegree (density)
 TRUE
 FALSE FALSE -0.80750 0
 FALSE FALSE
5 fr4wav reciprocity
 0.00000
 TRUE
6 smokebeh rate smokebeh (period 1)
 FALSE FALSE
 0.20811
 TRUE
 FALSE FALSE
7 smokebeh rate smokebeh (period 2)
 TRUE
 0.20811
 0
8 smokebeh rate smokebeh (period 3)
 0
 0.20811
 TRUE
 FALSE FALSE
9 smokebeh smokebeh linear shape
 TRUE
 FALSE FALSE
 0.56173
 0
```

Here is the original effect table based on friend data. And then we can add kinds of effects to it.

```
frndeff1 <- includeEffects(frndeff1,sameX,</pre>
interaction1="gender",name="fr4wav")
frndeff1 <- includeEffects(frndeff1,egoX,</pre>
interaction1="gender",name="fr4wav")
frndeff1 <- includeEffects(frndeff1,altx,</pre>
interaction1="gender",name="fr4wav")
frndeff1 <- includeEffects(frndeff1,egoX,</pre>
interaction1="smokebeh",name="fr4wav")
frndeff1 <- includeEffects(frndeff1,altx,</pre>
interaction1="smokebeh",name="fr4wav")
frndeff1 <- includeEffects(frndeff1,sameX,</pre>
interaction1="smokebeh",name="fr4wav")
frndeff1 <- includeEffects(frndeff1,avSim,</pre>
interaction1="fr4wav",name="smokebeh")
frndeff1 <- includeEffects(frndeff1.totSim.</pre>
interaction1="fr4wav",name="smokebeh")
```

And I got the following result.

```
{r}
frndeff1
 include fix
 initial Value parm
 effectName
 name
 test
1
 fr4wav
 constant fr4wav rate (period 1) TRUE
 2.00405
 FALSE FALSE
 0
 constant fr4wav rate (period 2) TRUE
2
 fr4wav
 2.00405
 FALSE FALSE
 0
3
 fr4wav
 constant fr4wav rate (period 3)
 2.00405
 0
 TRUE
 FALSE FALSE
4
 fr4wav
 outdegree (density)
 FALSE FALSE
 -0.80750
 0
 TRUE
5
 fr4wav
 reciprocity
 0.00000
 0
 TRUE
 FALSE FALSE
6
 fr4wav
 transitive triplets
 TRUE
 FALSE FALSE
 0.00000
 0
7
 fr4wav
 FALSE FALSE
 gender alter
 TRUE
 0.00000
 0
8
 fr4wav
 gender ego
 0.00000
 0
 TRUE
 FALSE FALSE
9
 fr4wav
 same gender
 0.00000
 TRUE
 FALSE FALSE
 0
10 fr4wav
 smokebeh alter
 FALSE FALSE
 0.00000
 0
 TRUE
11 fr4wav
 smokebeh ego
 FALSE FALSE
 0.00000
 0
 TRUE
12 fr4wav
 same smokebeh
 TRUE
 FALSE FALSE
 0.00000
 0
13 smokebeh rate smokebeh (period 1)
 TRUE
 FALSE FALSE
 0.20811
 0
14 smokebeh rate smokebeh (period 2)
 TRUE
 FALSE FALSE
 0.20811
 0
15 smokebeh rate smokebeh (period 3)
 0.20811
 0
 FALSE FALSE
 TRUE
16 smokebeh smokebeh linear shape
 0.56173
 0
 TRUE
 FALSE FALSE
17 smokebeh smokebeh average similarity
 FALSE FALSE
 0.00000
 0
 TRUE
18 smokebeh smokebeh total similarity
 TRUE
 FALSE FALSE
 0.00000
 0
```

### Part III Question II

```
Question 2

"{r}

myalgorithm <- sienaAlgorithmCreate(projname='coevolve')

RSmod1<-siena07(myalgorithm, data=friend, effects=frndeff, batch=T, verbose = F, useCluster = T, initC = T, nbrNodes = 3, returnDeps=TRUE)

siena07 will create an output file coevolve.txt .

start phase 0
theta: 2.004 2.004 2.004 -0.808 0.000 0.208 0.208 0.208 0.562

Start phase 1
Phase 1 Iteration 1 Progress: 0%
Phase 1 Iteration 4 Progress: 0%
Phase 1 Iteration 10 Progress: 0%
Phase 1 Iteration 25 Progress: 0%
Phase 1 Iteration 25 Progress: 0%
```

Here is the model we built.

Estimates, standard errors and convergence t-ratios

	Estimate	Standard Error	Convergence t-ratio
Network Dynamics		LITOI	c racio
1. rate constant fr4wav rate (period 1)	1.1474	( 0.2344 )	0.0279
<ol><li>rate constant fr4wav rate (period 2)</li></ol>	1.1202	( 0.2057)	-0.0958
<ol><li>rate constant fr4wav rate (period 3)</li></ol>	1.1387	( 0.2122 )	-0.0203
<ol><li>eval outdegree (density)</li></ol>	-3.1799	•	
<ol><li>eval reciprocity</li></ol>	0.8095	•	
<ol><li>6. eval transitive triplets</li></ol>	0.0863	•	-0.0697
7. eval gender alter	-0.3091	•	
8. eval gender ego	0.2890	•	
9. eval same gender	1.2786	•	
10. eval smokebeh alter	0.7442	•	
11. eval smokebeh ego	-0.0466	( 0.2997)	0.0335
12. eval same smokebeh	1.2390	( 1.3380)	-0.0176
Behavior Dynamics			
13. rate rate smokebeh (period 1)	0.2970	( 0.1637)	0.1129
<ol><li>rate rate smokebeh (period 2)</li></ol>	0.3161	( 0.1782 )	0.0554
<ol><li>rate rate smokebeh (period 3)</li></ol>	0.3072	( 0.3177)	-0.0104
16. eval smokebeh linear shape	13.6460	( 1061.5170 )	0.0761
17. eval smokebeh average similarity	122.1568	( 14378.4129 )	-0.2900
18. eval smokebeh total similarity	-15.4698	( 1903.4595 )	-0.1361

Overall maximum convergence ratio: 1.2624

And here is the summary of the model from where we can get a lot of statistics.

# **Part IV Question III**

```
Question 3
```{r}
ell <- RSmod1$sims[[1]][[1]][[1]]
sb1 <- RSmod1$sims[[1]][[1]][[2]]
el2 <- RSmod1$sims[[1]][[1]][[1]]
sb2 <- RSmod1$sims[[1]][[1]][[2]]
el3 <- RSmod1$sims[[1]][[1]][[1]][[3]]
sb3 <- RSmod1$sims[[1]][[1]][[2]][[3]]
sim1 <- graph.data.frame(el1,directed = TRUE)</pre>
sim2 <- graph.data.frame(el2,directed = TRUE)</pre>
sim3 <- graph.data.frame(el3,directed = TRUE)</pre>
w2s=spMatrix(37,37,el1[,1],el1[,2],el1[,3])
w3s = spMatrix(37, 37, e12[,1], e12[,2], e12[,3])
w4s = spMatrix(37, 37, e13[,1], e13[,2], e13[,3])
fr4wav4=sienaDependent(list(w1s,w2s,w3s,w4s))
smoke\_sim=array(c(V(fr\_w1)\$smoke,sb1,sb2,sb3),dim=c(37,4))
smoke_beh_sim=sienaDependent(smoke_sim,type="behavior")
friend_sim=sienaDataCreate(fr4wav4,smoke_beh_sim,gender)
```

By following the method shown in the PowerPoint Lecture 9, we can re-simulate data based on the RSmod1. And after adding effects to it, we can use these two to get two corresponding models.

Here are the statistics about model 1.

Estimates, standard errors and convergence t-ratios

	Estimate	Standard Error	Convergence t-ratio
Network Dynamics			
 rate constant fr4wav4 rate (period 1) 	1.1464	(0.2167)	0.0118
rate constant fr4wav4 rate (period 2)	4.1290	(0.5047)	-0.0169
rate constant fr4wav4 rate (period 3)	3.2824	(0.4344)	-0.0010
eval outdegree (density)	-3.0690	(0.3475)	-0.0156
eval reciprocity	0.9207	(0.1477)	-0.0233
eval transitive triplets	0.0922	(0.0461)	-0.0025
7. eval gender alter	-0.1430	(0.2353)	-0.0026
8. eval gender ego	0.2226	(0.2288)	0.0192
9. eval same gender	1.5052	(0.2601)	-0.0015
10. eval smoke_beh_sim alter	0.1661	(0.2491)	0.0077
 eval smoke_beh_sim ego 	0.1664	(0.2465)	-0.0448
12. eval same smoke_beh_sim	0.6941	(0.3721	-0.0366
Behavior Dynamics			
rate rate smoke_beh_sim (period 1)	0.3217	(0.1690)	0.0943
<pre>14. rate rate smoke_beh_sim (period 2)</pre>	0.7774	(0.3720)	0.0333
<pre>15. rate rate smoke_beh_sim (period 3)</pre>	1.1094	(0.4726)	-0.0122
16. eval smoke_beh_sim linear shape	0.4258	(0.5195)	0.0066
17. eval smoke_beh_sim average similarity	1.0252	(7.3823)	0.0143
18. eval smoke_beh_sim total similarity	0.2900	(1.5820	0.0147

Overall maximum convergence ratio: 0.1599

From the result, we can get that for all convergence t-ratio are good and they can be excellent convergence (abs value smaller than 0.1). And overall convergence ratio is reasonable. And based on both estimation and standard error, we can calculate approximately that item 6, 7, 8, 10, 11, 12, 13, 14, 15, 16, 17, 18 are not significant (not larger than 4).

And here is the result of model 2.

Estimates, standard errors and convergence t-ratios Estimate Standard Convergence Error t-ratio Network Dynamics rate constant fr4wav4 rate (period 1) 1.1200 (0.1907 -0.0490 (0.4960 rate constant fr4wav4 rate (period 2) 4.0578 -0.0220 3. rate constant fr4wav4 rate (period 3) 3.2307 (0.3978 -0.03774. eval outdegree (density) -2.9046 (0.2900) 0.0286 1.0000 (0.1538 5. eval reciprocity) 0.0570 6. eval same gender 1.6615 (0.2266 0.0250 7. eval same smoke_beh_sim 0.5444 (0.2639 0.0431 Behavior Dynamics 8. rate rate smoke_beh_sim (period 1) 0.2600 (0.1500 -0.0230 9. rate rate smoke_beh_sim (period 2) (0.2715) 0.5135 -0.0052(0.3681 10. rate rate smoke_beh_sim (period 3) 0.9391 0.0200 11. eval smoke_beh_sim linear shape -0.1664 (0.4302) 0.0091 Overall maximum convergence ratio: 0.1044

All t-ratio are good and they can be convergence (abs value smaller than 0.1) and max convergence ratio is good. In terms of significance, item 7, 8, 9, 10, 11 are not significant (not larger than 4).

So, based on the results above, we can say that the model two is better as the ratio is smaller so it can be more possible to converge and less non-significant variables.

Part V Appendix

title: "Network_HW6"

author: "Chenrui Xu"

date: "2021/3/28"

output: html_document

```
library(igraph)
library(UserNetR)
library(RSiena)
library(Matrix)
data(Coevolve)
set.seed(999)
•••
```{r}
fr_w1=Coevolve$fr_w1
fr_w2=Coevolve$fr_w2
fr_w3=Coevolve$fr_w3
fr_w4=Coevolve$fr_w4
•••
```{r}
matw1 <- as.matrix(get.adjacency(fr_w1))
matw2 <- as.matrix(get.adjacency(fr_w2))</pre>
matw3 <- as.matrix(get.adjacency(fr_w3))</pre>
matw4 <- as.matrix(get.adjacency(fr_w4))
```{r}
fr4wav<-sienaDependent(
```

```
array(c(matw1,matw2,matw3,matw4),
 dim=c(37,37,4)), sparse=FALSE)
class(fr4wav)
fr4wav
...
```{r}
w1 <- cbind(get.edgelist(fr w1), 1)
w2 <- cbind(get.edgelist(fr_w2), 1)
w3 <- cbind(get.edgelist(fr_w3), 1)
w4 <- cbind(get.edgelist(fr_w4), 1)
w1s <- spMatrix(37, 37, w1[,1], w1[,2], w1[,3])
w2s <- spMatrix(37, 37, w2[,1], w2[,2], w2[,3])
w3s <- spMatrix(37, 37, w3[,1], w3[,2], w3[,3])
w4s <- spMatrix(37, 37, w4[,1], w4[,2], w4[,3])
fr4wav2 <- sienaDependent(list(w1s,w2s,w3s,w4s))
fr4wav2
```{r}
gender_vect <- V(fr_w1)$gender
table(gender_vect)
gender <- coCovar(gender vect)</pre>
gender
```

```
```{r}
smoke <- array(</pre>
   c(V(fr_w1)$smoke, V(fr_w2)$smoke,
      V(fr_w3)$smoke, V(fr_w4)$smoke),
   dim=c(37,4))
smokebeh <- sienaDependent(smoke,</pre>
   type = "behavior")
smokebeh
```{r}
friend <- sienaDataCreate(fr4wav,smokebeh,gender)
friend
```{r}
frndeff <- getEffects(friend)</pre>
frndeff
```{r}
```

effectsDocumentation(frndeff)

```
•••
```

```
```{r}
frndeff <- getEffects(friend)</pre>
frndeff1 <- getEffects(friend)
#frndeff2 <- getEffects(friend)
# frndeff2 <- includeEffects(frndeff2,sameX,
# interaction1="gender",name="fr4wav")
#
# frndeff2 <- includeEffects(frndeff2,sameX,
# interaction1="smokebeh",name="fr4wav")
frndeff1 <- includeEffects(frndeff1,sameX,</pre>
interaction1="gender",name="fr4wav")
frndeff1 <- includeEffects(frndeff1,egoX,</pre>
interaction1="gender",name="fr4wav")
frndeff1 <- includeEffects(frndeff1,altX,
interaction1="gender",name="fr4wav")
frndeff1 <- includeEffects(frndeff1,egoX,
```

```
interaction1="smokebeh",name="fr4wav")
frndeff1 <- includeEffects(frndeff1,altX,
interaction1="smokebeh",name="fr4wav")
frndeff1 <- includeEffects(frndeff1,sameX,
interaction1="smokebeh",name="fr4wav")
frndeff1 <- includeEffects(frndeff1,avSim,
interaction1="fr4wav",name="smokebeh")
frndeff1 <- includeEffects(frndeff1,totSim,</pre>
interaction1="fr4wav",name="smokebeh")
frndeff1 <- includeEffects(frndeff1,recip,transTrip,</pre>
name="fr4wav")
```{r}
frndeff
```{r}
frndeff1
```

```
Question 2
```{r}
myalgorithm <- sienaAlgorithmCreate(projname='coevolve')
RSmod1<-siena07(myalgorithm,data=friend,effects=frndeff1,batch=T,verbose
= F,useCluster = T,initC = T,nbrNodes = 3,returnDeps=TRUE)
```{r}
RSmod1
```{r}
RSmod1$sims[[1]]
```{r}
summary(RSmod1)
```{r}
myalgorithm <- sienaAlgorithmCreate(projname='coevolve')</pre>
```

```
RSmod2<-siena07(myalgorithm,data=friend,effects=
#
 S
 frndeff2,batch=T,verbose = F,useCluster = T,initC =
#
T,nbrNodes = 3,returnDeps=TRUE)
#RSmod2
Question 3
```{r}
el1 <- RSmod1$sims[[1]][[1]][[1]]
sb1 <- RSmod1$sims[[1]][[1]][[2]][[1]]
el2 <- RSmod1$sims[[1]][[1]][[1]][[2]]
sb2 <- RSmod1$sims[[1]][[1]][[2]][[2]]
el3 <- RSmod1$sims[[1]][[1]][[1]][[3]]
sb3 <- RSmod1$sims[[1]][[1]][[2]][[3]]
sim1 <- graph.data.frame(el1,directed = TRUE)
sim2 <- graph.data.frame(el2,directed = TRUE)
sim3 <- graph.data.frame(el3,directed = TRUE)
w1 <- cbind(get.edgelist(fr_w1), 1)
w1s <- spMatrix(37, 37, w1[,1], w1[,2], w1[,3])
w2s_sim=spMatrix(37,37,el1[,1],el1[,2],el1[,3])
w3s sim=spMatrix(37,37,el2[,1],el2[,2],el2[,3])
```

```
fr4wav4=sienaDependent(list(w1s,w2s_sim,w3s_sim,w4s_sim))
smoke_sim=array(c(V(fr_w1)$smoke,sb1,sb2,sb3),dim=c(37,4))
smoke_beh_sim=sienaDependent(smoke_sim,type="behavior")
friend_sim=sienaDataCreate(fr4wav4,smoke_beh_sim,gender)
# V(sim1)$smoke <- sb1
# V(sim1)$gender <- V(fr_w4)$gender
#sim1
#
# matsim1=as.matrix(get.adjacency(sim1))
# simwav1=sienaDependent(matsim1,sparse=F)
# simgender vect1=V(sim1)$gender
# gender1 <- coCovar(simgender vect1)
#
# smoke1 <- array(V(sim1)$smoke,dim=c(37,1))</pre>
# smokebeh1 <- sienaDependent(c(smoke1),type = "behavior")
# smokebeh1
#
#
# w1 <- cbind(get.edgelist(fr w1), 1)
# w1s <- spMatrix(37, 37, w1[,1], w1[,2], w1[,3])
```

w4s_sim=spMatrix(37,37,el3[,1],el3[,2],el3[,3])

```
```{r}
friend_sim
```{r}
frndeff1_sim <- getEffects(friend_sim)</pre>
frndeff2_sim <- getEffects(friend_sim)</pre>
frndeff2_sim <- includeEffects(frndeff2_sim,sameX,
interaction1="gender",name="fr4wav4")
frndeff2_sim <- includeEffects(frndeff2_sim,sameX,
interaction1="smoke beh sim",name="fr4wav4")
frndeff1_sim <- includeEffects(frndeff1_sim,sameX,</pre>
interaction1="gender",name="fr4wav4")
frndeff1_sim <- includeEffects(frndeff1_sim,egoX,
interaction1="gender",name="fr4wav4")
```

frndeff1_sim <- includeEffects(frndeff1_sim,altX,

```
interaction1="gender",name="fr4wav4")
frndeff1 sim <- includeEffects(frndeff1 sim,egoX,
interaction1="smoke_beh_sim",name="fr4wav4")
frndeff1_sim <- includeEffects(frndeff1_sim,altX,
interaction1="smoke beh sim",name="fr4wav4")
frndeff1_sim <- includeEffects(frndeff1_sim,sameX,
interaction1="smoke beh sim",name="fr4wav4")
frndeff1_sim <- includeEffects(frndeff1_sim,avSim,
interaction1="fr4wav4",name="smoke_beh_sim")
frndeff1 sim <- includeEffects(frndeff1 sim,totSim,
interaction1="fr4wav4",name="smoke beh sim")
frndeff1_sim <- includeEffects(frndeff1_sim,recip,transTrip,
name="fr4wav4")
```{r}
RSmod1 sim<-
siena07(myalgorithm,data=friend sim,effects=frndeff1 simZ,batch=T,verbose
```

```
= F,useCluster = T,initC = T,nbrNodes = 3,returnDeps=TRUE)
```{r}
RSmod2_sim<-
siena07(myalgorithm,data=friend_sim,effects=frndeff2_sim,batch=T,verbose =
F,useCluster = T,initC = T,nbrNodes = 3,returnDeps=TRUE)
```{r}
summary(RSmod1_sim)
•••
```{r}
summary(RSmod2_sim)
```