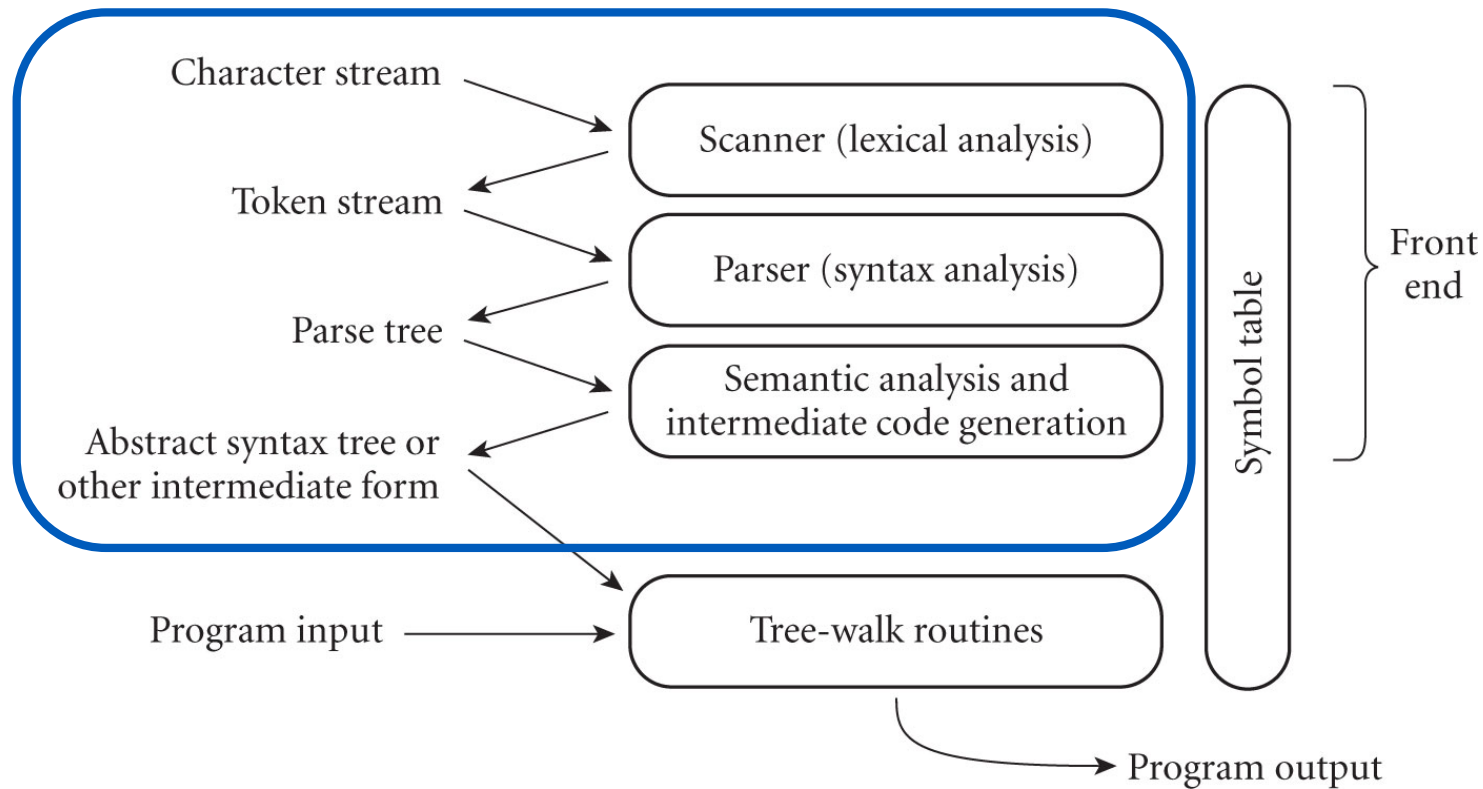


CS 320 : Continuing on Formal Grammars

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Parsing and semantic analysis



Generator vs Recognizer

```
<program> ::= <stmts>
<stmts> ::= <stmt> | <stmt> ; <stmts>
<stmt> ::= <var> = <expr>
<var> ::= a | b | c | d
<expr> ::= <term> + <term> | <term> - <term>
<term> ::= <var> | const
```

Recognize a sentence

```
a = b + const
<var> = b + const
<var> = <var> + const
<var> = <term> + const
<var> = <term> + <term>
<var> = <expr>
<stmt>
<stmts> =:: <program>
```

Generate a sentence

```
<program> ::= <stmts>
               <stmt>
               <var> = <expr>
               a = <expr>
               a = <term> + <term>
               a = <var> + <term>
               a = b + <term>
               a = b + const
```

Some of the challenges:

- There is a (potentially) **infinite number of source programs** that we need to recognize.
 - An infinity of words
 - An infinity of sentences
- There should be **no ambiguity in the way the program is interpreted.**
 - Unique vocabulary,
 - Uniquely determine sentences
- The source program may contain **syntax errors** and the compiler/interpreter has to recognize them.
 - Lexical errors (errors in the choice of words)
 - Grammatical errors (errors in the construction of sentences)

Is a BNF grammar specific enough for an interpreter to execute it?

Here a simple grammar for expressions:

$\langle \text{expr} \rangle ::= \langle \text{expr} \rangle \langle \text{op} \rangle \langle \text{expr} \rangle$

$\langle \text{expr} \rangle ::= 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0$

$\langle \text{op} \rangle ::= + | - | * | /$

How shall the interpreter/compiler **execute** the following expression?

$2 + 3 * 4$

This can be interpreted as

$(2 + 3) * 4$

or as

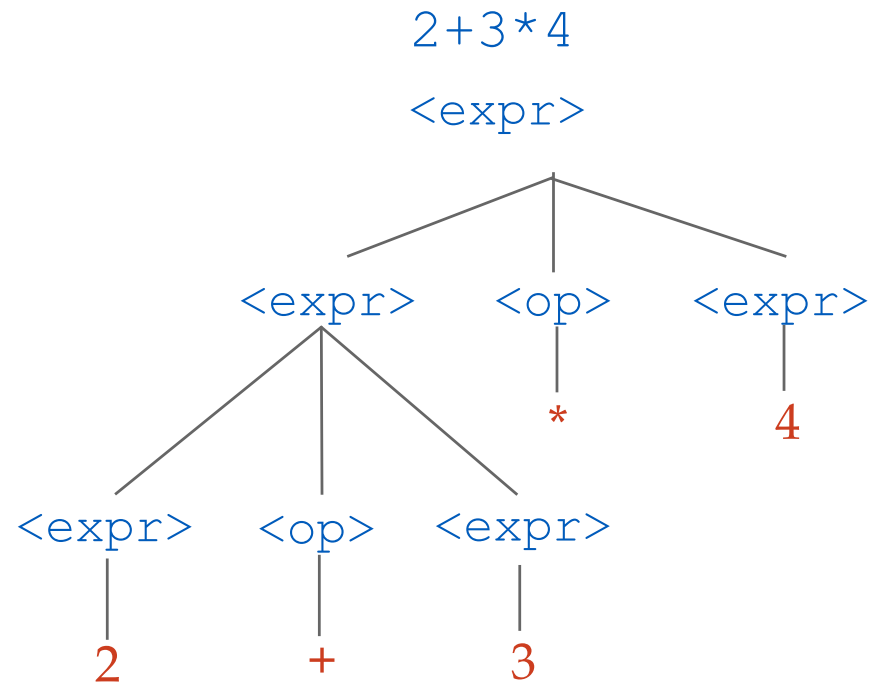
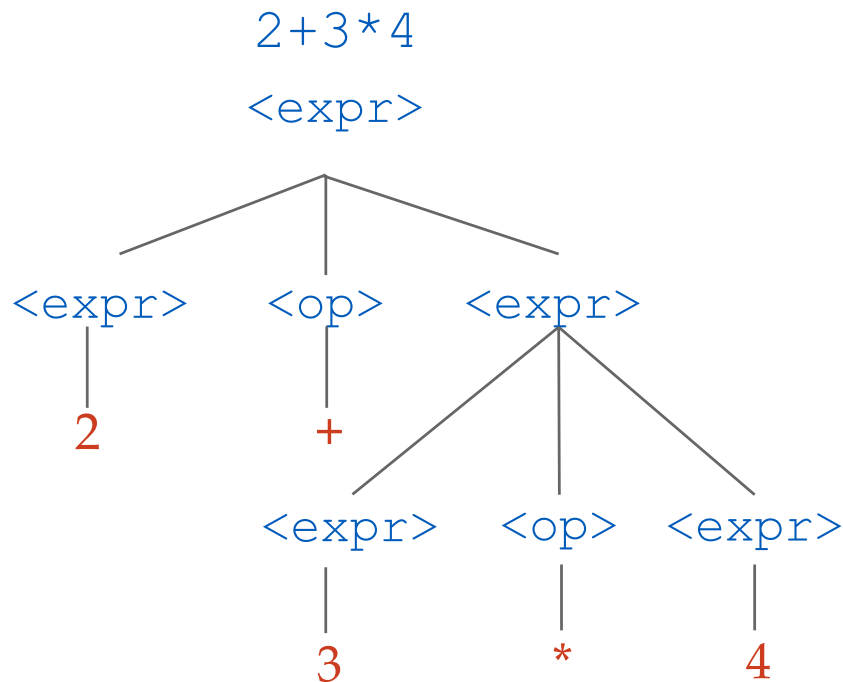
$2 + (3 * 4)$

Note: here the parenthesis are just to show the possible ambiguity, they are not part of the grammar.

Ambiguous Grammars

- A grammar is **ambiguous** if and only if it generates a sentential form that has **two or more distinct parse trees**.

$\langle \text{expr} \rangle$	$::=$	$\langle \text{expr} \rangle \langle \text{op} \rangle \langle \text{expr} \rangle$
$\langle \text{expr} \rangle$	$::=$	$1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9 \mid 0$
$\langle \text{op} \rangle$	$::=$	$+ \mid - \mid * \mid /$



Ambiguous Grammars

Ambiguous grammars are, in general, **undesirable** in formal languages.

Why?

It makes parsing **difficult** – and more **error prone**.

Ambiguity can have **different sources**.

Good news: we can usually **eliminate the ambiguity by revising** the grammar.

Some examples

<funtype> ::= <type> | <funtype> -> <funtype>
<type> ::= int | float | bool

Is this grammar ambiguous? Show why?

Some examples

<prodtype> ::= int * <prodtype> | int

Is this grammar ambiguous? Show why?

Some examples

<expr> ::= <expr> + <expr>

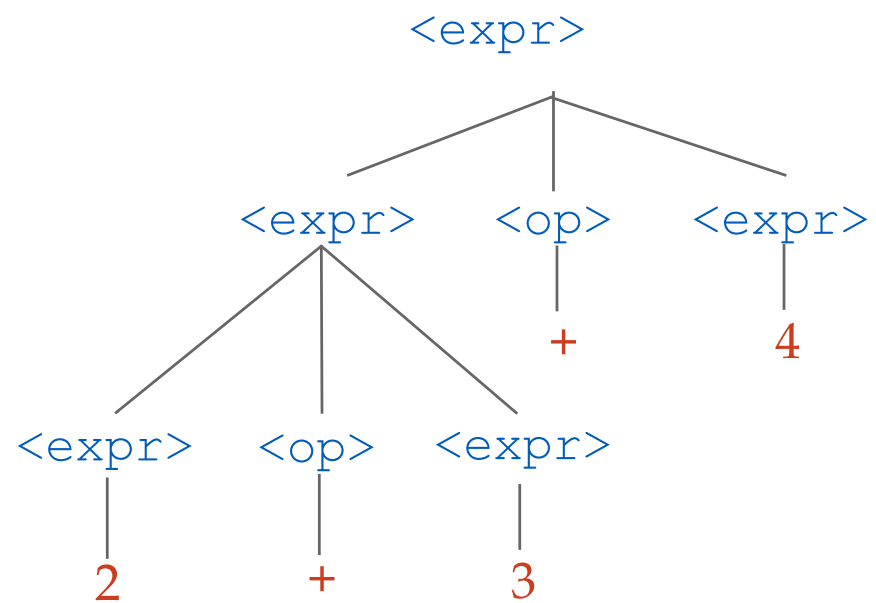
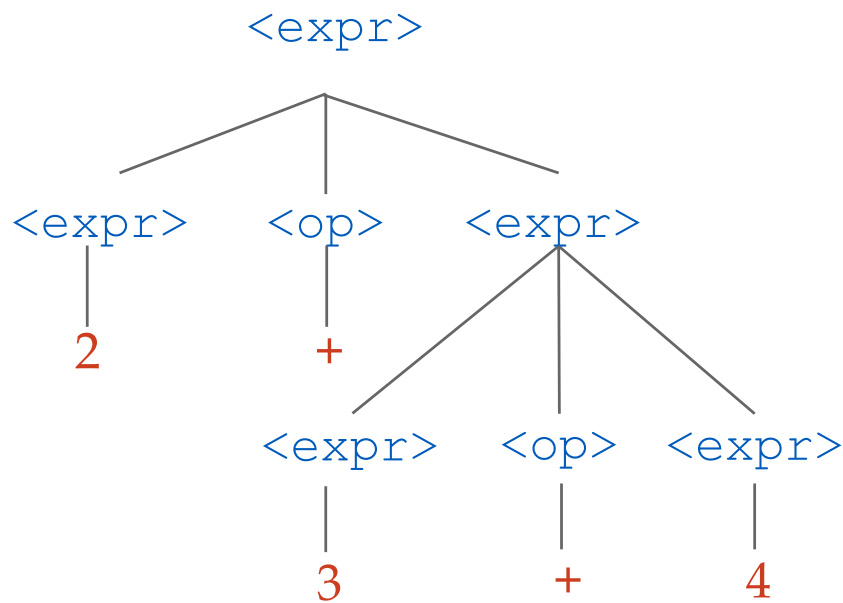
<expr> ::= 1|2|3|4|5|6|7|8|9|0

Is this grammar ambiguous? Show why?

How can we avoid ambiguity?

How can we **disambiguate** between the two parse trees for the following expression?

2+3+4



How can we avoid ambiguity?

How can we **disambiguate** between the two parse trees for the following expression?

$2+3+4$

First idea: make the **parentheses** part of the language

$((2+3)+4)$

$(2+(3+4))$

We need to
add them
everywhere!

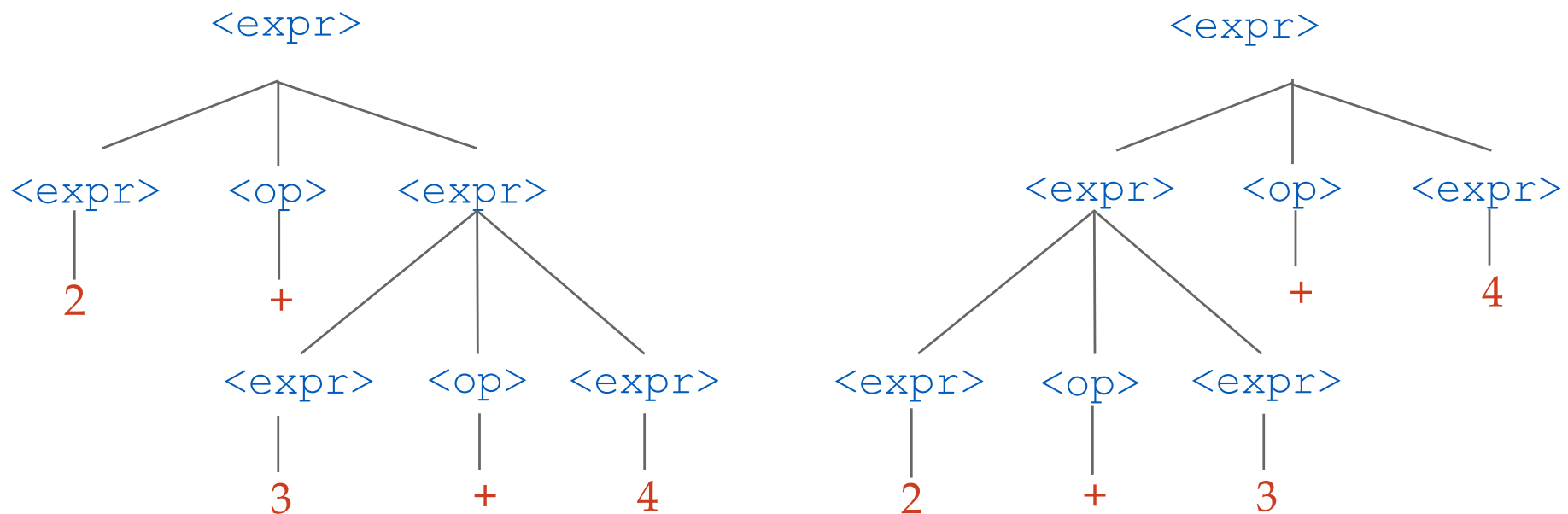
One way to do this is to change the grammar:

```
<expr> ::= ( <expr> <op> <expr> )  
<expr> ::= 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0  
<op>    ::= + | - | * | /
```

We add
parentheses
around every
expression

How can we avoid ambiguity and preserve the structure of the grammar?

Second idea: If we use the **parse tree** to indicate **precedence levels** of the operators, **we cannot have ambiguity**.



Problem: it requires to work directly with parse trees.

How can we avoid ambiguity and preserve the structure of the grammar?

Why is the previous grammar ambiguous?

$$2+3*4$$

Two “classes” of operations that have different precedence and the grammar does not distinguish them.

$$2+3+4$$

Two “occurrences” of the same operations have the same precedence and the grammar does not distinguish them.

Dealing with associativity?

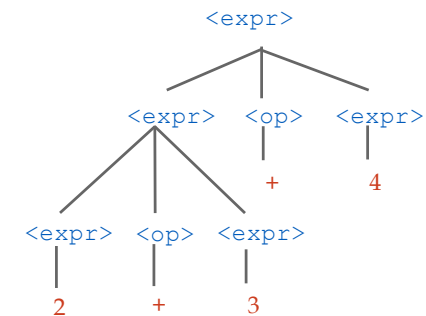
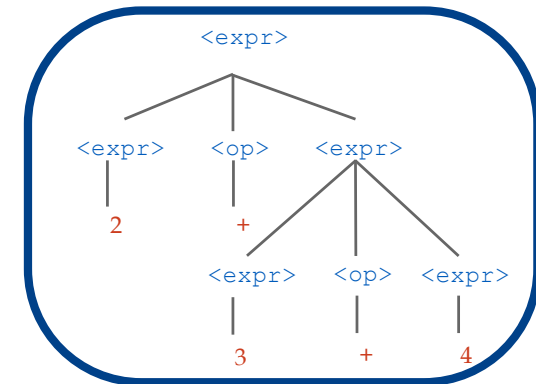
2+3+4

Two “occurrences” of the same operations have the same precedence and the grammar does not distinguish them.

```
<expr> ::= <expr> <op> <expr>
<expr> ::= 1|2|3|4|5|6|7|8|9|0
<op>    ::= +|-|*|/
```

We need to break the symmetry and commit to one choice.

```
<expr> ::= <const> | <const> <op> <expr>
<const> ::= 1|2|3|4|5|6|7|8|9|0
<op>    ::= +|-|*|/
```



Dealing with associativity?

```
<expr> ::= <const> | <const><op><expr>  
<const> ::= 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0  
<op>     ::= + | - | * | /
```

We use two
nonterminal
to break the
symmetry

How can we derive the following expression?

2+3+4+5

```
<expr> => <const> <op> <expr>  
      => 2 <op> <expr>  
      => 2 + <expr>  
      => 2 + <const> <op> <expr>  
      => 2 + 3 <op> <expr>  
      => 2 + 3 + <expr>  
      => 2 + 3 + <const> <op> <expr>  
      => 2 + 3 + 4 <op> <expr>  
      => 2 + 3 + 4 + <expr>  
      => 2 + 3 + 4 + <const>  
      => 2 + 3 + 4 + 5
```


Dealing with associativity?

```
<expr> ::= <const> | <const><op><expr>  
<const> ::= 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0  
<op>      ::= + | - | * | /
```

We use two
nonterminal
to break the
symmetry

How can we recognize the following expression?

2+3+4+5

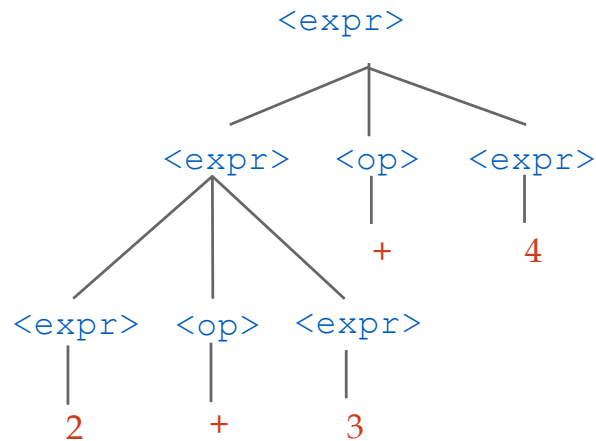
Dealing with associativity?

```
<expr> ::= <const> | <const><op><expr>  
<const> ::= 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0  
<op>    ::= + | - | * | /
```

We use two
nonterminal
to break the
symmetry

How can we implement it?

Associativity by Grammar Design



Left-associative

<expr>	::=	<const> <expr><op><const>
<const>	::=	1 2 3 4 5 6 7 8 9 0
<op>	::=	+

Left-recursive

Right-associative

<expr>	::=	<const> <const><op><expr>
<const>	::=	1 2 3 4 5 6 7 8 9 0
<op>	::=	+

Right-recursive

