

CS 541 Artificial Intelligence: Homework 4

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Due: 12/06/2020, 8:00 pm EST

This assignment is dedicated to helping you understand GD and recommender systems. You need to download the **ml-latest-small.zip** at <https://grouplens.org/datasets/movielens/>

1 Data Set

Note that the zip file contains side information (e.g. tag applications) that will not be used in the project: we consider **only the ratings from the users**. Therefore, the first step is to pre-process the data, and organize all the users' ratings as a matrix. Suppose there are n users and p movies. Then the size of the rating matrix M is $n \times p$. Let us denote the index set of observed entries by Ω .

The second step is to divide Ω into two sets Ω_1 and Ω_2 : Ω_1 for training and Ω_2 for testing. To this end, we randomly choose 90 percent of entries in Ω to form Ω_1 , and Ω_2 consists of the remaining.

2 Learning

Then you will have to solve the following non-convex program to learn the prediction matrix:

$$\min_{U,V} F(U,V) := \frac{1}{2} \sum_{(i,j) \in \Omega_1} (M_{ij} - \mathbf{u}_i \mathbf{v}_j^\top)^2 + \frac{\lambda}{2} (\|U\|_F^2 + \|V\|_F^2) \quad (1)$$

where M_{ij} is the (i,j) th entry of M , \mathbf{u}_i and \mathbf{v}_j are the i th and j th row of U and V respectively.

1. Derive the gradient $\frac{\partial F(U,V)}{\partial U}$ and $\frac{\partial F(U,V)}{\partial V}$.
2. Suppose $\lambda = 1$. Describe the update rule of GD and implement it with Python. You can randomly initialize all \mathbf{u}_i and \mathbf{v}_j . Note that you need to carefully choose the learning rate.
3. Plot the objective value against the number of iterations, and summarize your findings.

3 Evaluation

After we terminate GD, we will obtain the solution U, V . Our prediction matrix X is then given by $X = UV^\top$. We evaluate the performance of our prediction matrix X by root-mean-square error (RMSE):

$$\text{RMSE} := \sqrt{\frac{1}{|\Omega_2|} \sum_{(i,j) \in \Omega_2} (M_{ij} - X_{ij})^2}.$$

1. Record the RMSE for the choice $\lambda = 1$.
2. Now pick λ from $\{10^{-6}, 10^{-3}, 0.1, 0.5, 2, 5, 10, 20, 50, 100, 500, 1000\}$. For each value, learn and evaluate your model. Plot RMSE against λ and summarize your findings.