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(%i1) /*on definit la matrice de Denavit Hartenberg*/

dhmatrix(a,alpha,r,theta) :=
matrix(
  [cos(theta)          , -sin(theta)          , 0          , a],
  [sin(theta)*cos(alpha), cos(theta)*cos(alpha), -sin(alpha), -r*sin(alpha)],
  [sin(theta)*sin(alpha), cos(theta)*sin(alpha), cos(alpha) , r*cos(alpha)],
  [0                    , 0                    , 0                    , 1]
) $

/*on definit toutes les matrices de changements*/

"T01";
T01:dhmatrix(0, 0      , 0 , q1);
"T12";
T12:dhmatrix(a1, 0 , 0 , q2);
"T23";
T23:dhmatrix(a2, 0 , q3, 0 );
"T34";
T34:dhmatrix(0, 0      , 0 , q4);

/*calcul de T04*/

T06: T01.T12.T23.T34;

/*on substitue par les valeurs q1,...,qn*/

"config 1";

T06_1:subst(0,q1,T06)$
T06_1:subst(0,q2,T06_1)$
T06_1:subst(0,q3,T06_1)$
T06_1:subst(0,q4,T06_1)$

T06_1;

"config 2";

T06_2:subst(%pi/2,q1,T06)$
T06_2:subst(0,q2,T06_2)$
T06_2:subst(0,q3,T06_2)$
T06_2:subst(0,q4,T06_2)$

T06_2;

"config 3";

T06_3:subst(0,q1,T06)$ 2
T06_3:subst(%pi/2,q2,T06_3)$
T06_3:subst(0,q3,T06_3)$
T06_3:subst(0,q4,T06_3)$

T06_3;

"config 4";

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(%o2) T_{01}

$$(\%o3) \begin{pmatrix} \cos(q1) & \sin(q1) & 0 & 0 \\ \sin(q1) & \cos(q1) & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

(%o4) T_{12}

$$(\%o5) \begin{pmatrix} \cos(q2) & \sin(q2) & 0 & a1 \\ \sin(q2) & \cos(q2) & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

(%o6) T_{23}

$$(\%o7) \begin{pmatrix} 1 & 0 & 0 & a2 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & q3 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

(%o8) T_{34}

$$(\%o9) \begin{pmatrix} \cos(q4) & \sin(q4) & 0 & 0 \\ \sin(q4) & \cos(q4) & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$(\%o10) \begin{pmatrix} \cos(q1) (\cos(q2) \cos(q4) \sin(q2) \sin(q4)) \sin(q1) (\cos(q2) \sin(q4) + \sin(q2) \cos(q4)) & \cos(q1) (\cos(q2) \cos(q4) \sin(q2) \sin(q4)) \sin(q1) (\cos(q2) \sin(q4) + \sin(q2) \cos(q4)) & \cos(q1) (\cos(q2) \cos(q4) \sin(q2) \sin(q4)) \sin(q1) (\cos(q2) \sin(q4) + \sin(q2) \cos(q4)) \\ \sin(q1) (\cos(q2) \cos(q4) \sin(q2) \sin(q4)) + \cos(q1) (\cos(q2) \sin(q4) + \sin(q2) \cos(q4)) & \cos(q1) (\cos(q2) \cos(q4) \sin(q2) \sin(q4)) + \cos(q1) (\cos(q2) \sin(q4) + \sin(q2) \cos(q4)) & \cos(q1) (\cos(q2) \cos(q4) \sin(q2) \sin(q4)) + \cos(q1) (\cos(q2) \sin(q4) + \sin(q2) \cos(q4)) \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

(%o11) $config1$

$$(\%o16) \begin{pmatrix} 1 & 0 & 0 & a2 + a1 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

(%o17) $config2$

$$(\%o22) \begin{pmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & a2 + a1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

(%o23) $config3$

$$(\%o28) \begin{pmatrix} 0 & 1 & 0 & a1 \\ 1 & 0 & 0 & a2 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

(%o29) *config4*

$$(\%o34) \begin{pmatrix} 0 & 1 & 0 & a2 + a1 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

(%o35) *config5*

$$(\%o40) \begin{pmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & a2a1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

(%o41) *config6*

$$(\%o46) \begin{pmatrix} 1 & 0 & 0 & a2 + a1 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0.5 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

(%o47) *config7*

$$(\%o52) \begin{pmatrix} 1 & 0 & 0 & a2 \\ 0 & 1 & 0 & a1 \\ 0 & 0 & 1 & 0.5 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

(%o53) *T04*

$$(\%o62) \begin{pmatrix} c1 (c2 c4 s2 s4) s1 (c2 s4 + c4 s2) & c1 (c2 s4 c4 s2) s1 (c2 c4 s2 s4) & 0 & c1 (a2 c2 + a1) a2 s1 s2 \\ s1 (c2 c4 s2 s4) + c1 (c2 s4 + c4 s2) & c1 (c2 c4 s2 s4) + s1 (c2 s4 c4 s2) & 0 & a2 c1 s2 + (a2 c2 + a1) s1 \\ 0 & 0 & 1 & q^3 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$