

# Algorithm Practice Exam (Paper-and-Pencil Mode)

## 1. Sentiment Analysis (Graded)

English	Chinese (中文)
<p>Problem:</p> <p>Calculate the sentiment score of the tweet: 'The service was not very good.'</p> <p>Given Lexicon:</p> <ul style="list-style-type: none"><li>- good: +2</li><li>- service: 0 (neutral)</li></ul> <p>Rules:</p> <ol style="list-style-type: none"><li>'very' (intensifier): increases the score of the next word by 50%.</li><li>'not' (negator): multiplies the score of the following phrase by -0.8.</li></ol>	<p>题目:</p> <p>计算推文 Sentiment 分数: 'The service was not very good.'</p> <p>给定词典:</p> <ul style="list-style-type: none"><li>- good: +2</li><li>- service: 0 (中性)</li></ul> <p>规则:</p> <ol style="list-style-type: none"><li>'very' (加强词): 将下一个词的分数增加 50%。</li><li>'not' (否定词): 将后续短语的分数乘以 -0.8。</li></ol>
<p>Solution:</p> <ol style="list-style-type: none"><li><b>Identify Sentiment Words</b>: 'good' (+2).</li><li><b>Apply Intensifier</b>: 'very' modifies 'good'. <math>\text{Score('very good')} = \text{Score('good')} * 1.5 = 2 * 1.5 = 3.</math></li><li><b>Apply Negation</b>: 'not' modifies 'very good'. <math>\text{Score('not very good')} = \text{Score('very good')} * -0.8 = 3 * -0.8 = -2.4.</math></li></ol> <p><b>Final Score</b>: -2.4.</p>	<p>解析:</p> <ol style="list-style-type: none"><li><b>识别情感词</b>: 'good' (+2)。</li><li><b>应用加强词</b>: 'very' 修饰 'good'。 <math>\text{分数('very good')} = \text{分数('good')} * 1.5 = 2 * 1.5 = 3.</math></li><li><b>应用否定词</b>: 'not' 修饰 'very good'。 <math>\text{分数('not very good')} = \text{分数('very good')} * -0.8 = 3 * -0.8 = -2.4.</math></li></ol> <p><b>最终分数</b>: -2.4。</p>

## 2. Pointwise Mutual Information (PMI)

English	Chinese (中文)
<b>Problem:</b> Calculate PMI(coffee, cup).  <b>Corpus Statistics:</b> - Total word pairs (\$N\$): 10,000 - Count('coffee') (\$c_x\$): 100 - Count('cup') (\$c_y\$): 200 - Count('coffee', 'cup') co-occurrence (\$c_{xy}\$): 20	<b>题目:</b> 计算 PMI(coffee, cup)。  <b>语料库统计:</b> - 总词对数 (\$N\$): 10,000 - Count('coffee') (\$c_x\$): 100 - Count('cup') (\$c_y\$): 200 - Count('coffee', 'cup') 共现 (\$c_{xy}\$): 20
<b>Solution:</b> Formula: $PMI(x, y) = \log_2 \frac{P(x,y)}{P(x)P(y)}$  1. <b>Calculate Probabilities:</b> $P(x) = 100 / 10000 = 0.01$ $P(y) = 200 / 10000 = 0.02$ $P(x,y) = 20 / 10000 = 0.002$  2. <b>Compute Ratio:</b> $\frac{0.002}{0.01 \times 0.02} = \frac{0.002}{0.0002} = 10$  3. <b>Logarithm:</b> $PMI = \log_2(10) \approx 3.32$	<b>解析:</b> 公式: $PMI(x, y) = \log_2 \frac{P(x,y)}{P(x)P(y)}$  1. <b>计算概率:</b> $P(x) = 100 / 10000 = 0.01$ $P(y) = 200 / 10000 = 0.02$ $P(x,y) = 20 / 10000 = 0.002$  2. <b>计算比率:</b> $\frac{0.002}{0.01 \times 0.02} = \frac{0.002}{0.0002} = 10$  3. <b>取对数:</b> $PMI = \log_2(10) \approx 3.32$

### 3. Naive POS Tagging

English	Chinese (中文)
<b>Problem:</b> Tag the word 'tweeted' in the sentence 'He tweeted.'  <b>Training Data:</b> - 'tweet': {Verb: 10, Noun: 2} - 'tweeted': Not in training data (Unknown)  <b>Rules for Unknown Words:</b> 1. If capitalized -> NNP (Proper Noun) 2. If ends with 'ed' -> VBD (Past Tense Verb) 3. Default -> NN (Noun)	<b>题目:</b> 为句子 'He tweeted' 中的 'tweeted' 标注词性。  <b>训练数据:</b> - 'tweet': {Verb: 10, Noun: 2} - 'tweeted': 不在训练数据中 (未知词)  <b>未知词规则:</b> 1. 如果首字母大写 -> NNP (专有名词) 2. 如果以 'ed' 结尾 -> VBD (过去式动词) 3. 默认 -> NN (名词)
<b>Solution:</b> 1. <b>Lookup:</b> Check 'tweeted' in the training dictionary. <b>Result:</b> Not found (Unknown).  2. <b>Apply Unknown Word Rules</b> (in order): - Is it capitalized? No ('t' is lowercase). - Does it end with 'ed'? <b>Yes</b> .  3. <b>Conclusion:</b> Assign tag <b>VBD</b> based on the suffix rule.	<b>解析:</b> 1. <b>查找:</b> 在训练字典中查找 'tweeted'。 <b>结果:</b> 未找到 (未知词)。  2. <b>应用未知词规则</b> (按顺序): - 首字母大写吗? 否 ('t' 小写)。 - 以 'ed' 结尾吗? <b>是</b> 。  3. <b>结论:</b> 根据后缀规则标记为 <b>VBD</b> 。

### 4. Jaccard Similarity

English	Chinese (中文)
<p>Problem:</p> <p>Calculate the Jaccard Similarity between Doc A and Doc B.</p> <p>- Doc A: 'apple banana apple' - Doc B: 'apple orange banana'</p>	<p>题目:</p> <p>计算文档 A 和文档 B 的 Jaccard 相似度。</p> <p>- Doc A: 'apple banana apple' - Doc B: 'apple orange banana'</p>
<p>Solution:</p> <p>1. <b>Create Sets</b> (Unique words): <math>\text{Set}(A) = \{\text{'apple'}, \text{'banana'}\}</math> <math>\text{Set}(B) = \{\text{'apple'}, \text{'orange'}, \text{'banana'}\}</math></p> <p>2. <b>Intersection</b> (<math>A \cap B</math>): Words in both: 'apple', 'banana'. Count = 2.</p> <p>3. <b>Union</b> (<math>A \cup B</math>): All unique words: 'apple', 'banana', 'orange'. Count = 3.</p> <p>4. <b>Calculate Jaccard</b>: <math>J(A,B) = \frac{ A \cap B }{ A \cup B } = \frac{2}{3} \approx 0.67</math></p>	<p>解析:</p> <p>1. <b>创建集合</b> (唯一词): <math>\text{Set}(A) = \{\text{'apple'}, \text{'banana'}\}</math> <math>\text{Set}(B) = \{\text{'apple'}, \text{'orange'}, \text{'banana'}\}</math></p> <p>2. <b>交集</b> (<math>A \cap B</math>): 两者都有的词: 'apple', 'banana'。数量 = 2。</p> <p>3. <b>并集</b> (<math>A \cup B</math>): 所有唯一词: 'apple', 'banana', 'orange'。数量 = 3。</p> <p>4. <b>计算 Jaccard</b>: <math>J(A,B) = \frac{ A \cap B }{ A \cup B } = \frac{2}{3} \approx 0.67</math></p>