# Erasmus Mundus WAVES GEOMAR, DeepSeaMonitoring

## Report

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#### 1 Introduction

The goal of this report is an overview of the literature covered in the scope of the research on the acoustic response of the bubble along with the results of different implementations.

This report is structured with a theoretical part and practical sections. Theoretical includes the following subsections:

- sound propagation basic concepts
- general SONAR principles and systems. The basics of acoustic wave propagation are explained and techniques utilized in SONAR systems

- beamforming and matched filtering
- cross-section scattering, backscattering, single and multiple scattering,
- natural frequency provided by bubble,
- single bubble model present in the literature (Thuraisigham and others).
- Minaert frequency, Rayleigh-Plesset equation of air bubble.

The practical part includes the following subsections:

- Calculation: After that the results of the implementation of a single bubble model are shown.
- Results and the interpretation of them and further developments are described as well

In the end, the conclusion provides a summary of the whole report.

### 2 Theoretical part

#### 2.1 Sound propagation

The wave's acoustic energy is assumed to be uniformly distributed over the area  $4\pi r^2$  of a sphere with the radius r. Therefore, the **acoustic intensity** at the distance r from the source is given by Equation 1:

$$I(r) = \frac{P}{4\pi r^2} \tag{1}$$

with the radiated power P of the source, measured in Watt.

As the acoustic wave propagates forward, mainly two types of propagation losses occur, with respect to the wave's intensity:

• the geometric spreading loss is related to the quadratic increase in the sphere's surface with the rise of the propagation distance.

The transmitted acoustic energy is conserved but distributed over an increased surface area. This results in a decrease in the acoustic intensity.

• the absorption loss is caused by the dissipation of acoustic energy. As seawater is a dissipative propagation medium lurton2002introduction, parts of the acoustic wave's energy are absorbed due to water viscosity (for sound frequencies of order 1MHz) and chemical relaxation effects (for frequencies up to 300kHz)

ainslie\_principles\_2010. This causes an exponential decrease in the acoustic pressure of the wave, proportional to the increasing propagation distance

The transmission loss (TL) is the loss in SNR due to the propagation losses. Assuming the simplification of non-absorbing water, the formula of the transmission loss for the modelling of the spherical spreading loss at the propagation distance r is given by:

$$TL_{spherical} = 20\log_{10}r\tag{2}$$

The cylindrical spreading loss takes into account that the propagating acoustic waves are bounded by two parallel planes, the bottom and surface of the sea:

$$TL_{cylindrical} = 10\log_{10}r\tag{3}$$

The target strength (TS) is a measure for the reflection strength of a target object. It is given by the ratio of the incident acoustic intensity  $I_i(r)$ , compared to the reflected acoustic intensity  $I_r(r)$ 

$$TS = 10\log_{10}\frac{I_r}{I_i} \tag{4}$$

#### 2.2 SONAR

SONAR is an echo-ranging device emitting and receiving sound wave signals to investigate the water surroundings. The acronym stands for sound navigation ranging. There are active and passive types of sonar, where only the first one can transmit the signal, while both can receive it.

The operation of an active SONAR is based on the use of transmitting projectors and receiving hydrophones. The projector converts a transmit signal to acoustic pressure waves, which emit from the projector's location and propagate through a physical medium like water, gas or solids hodges\_underwater\_2011. The transmission energy of the SONAR can be focused in a wanted direction by using beamforming. The transmitted waves get reflected by backscattering objects and are recorded by receiving hydrophones. To detect the transmitted signals in the received signals, the matched filter can be applied. Applying the principle of echolocation ainslie\_principles\_2010, the distance to and direction of backscattering objects can be determined by analyzing the time delay and phase relations between the transmitted and received signals.

The fields of usage: communication, detection or characterization of objects.

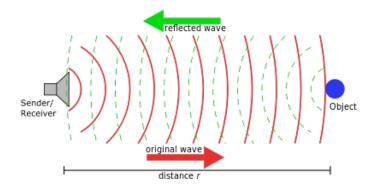


Figure 1: A scheme of the sonar principle of work

#### 2.3 Beamforming

The transmission energy of the SONAR can be focused in a wanted direction by using beamforming. The general idea of beamforming is to process receive and/or transmit signals, using an array with multiple receivers or transmitters, to achieve an SNR gain by constructive superposition. The processing depends on the geometric alignment of the array elements and the steering of the formed beam into the target direction. Signals coming from the wanted direction are added in phase, causing the amplification of the wanted signal components, while signals from unwanted directions are attenuated by destructive interference.

The spatial filter is called a beamformer as it allows to amplify selectively the arriving signal to each receiver from a narrow range of angles **hodges\_underwater\_2011**.

The delay-and-sum beamformer where each of the  $N_{R_x}$  output signal  $y_m(n)$  recorded by the m-th hydrophone is delayed by a number of samples, which can be calculated with the following formula:

$$\tau_m = \frac{d_m sin(\varphi_s)}{c} f_s \tag{5}$$

#### 2.4 Matched filtering

The matched filter is used for detecting the presence of the known transmit signal x(n) in a noisy receive signal y(n). It is optimal for detecting a waveform in the presence of white noise. For the signal x(n) of length  $n \in 0, ..., N_x-1$ , the impulse response of the matched filter

$$h(n) = x(N_x - 1 - n)$$

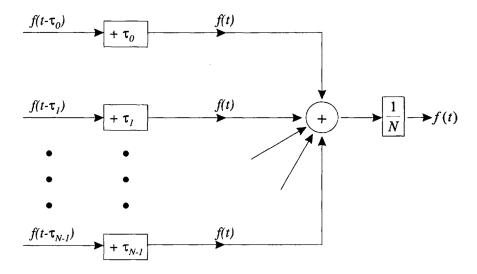


Figure 2: Delay-and-sum beamformer trees\_optimum\_2002

is given by the time-reversal of the signal x(n). The output of the matched filter is then given by the convolution sum:

$$y_{mf}(n) = y(n) * h(n) = \sum_{k=0}^{N_y - 1} y(k)h(n - k)$$
(6)

between the received signal y(n) of length  $n \in 0, ..., N_y-1$  and the impulse response of the matched filter. The output of the matched filter is a measure for the resemblance of the target signal x(n) in the received signal y(n) at time n, being maximal if both signals align.

This measure of similarity between two stationary random processes x(n) and y(n) at lag l is defined by the cross-correlation:

$$r_{xy}(l) = E\{x(n+l)y(n)\}$$

Two random process signals are orthogonal if their cross-correlation  $r_{xy}(l)$  is zero at all lags. As this expectation can be difficult to evaluate in practice, it can be estimated by the cross-correlation for deterministic signals.

#### 2.5 Scattering

Scattering from a small object:

Scattering cross-section - how much of the incoming wave gets scattered in the direction of the emitter, the ratio of the scattered power to the emitted intensity from a certain

grazing angle of an incident plane wave.

$$\sigma_{\theta_{in}} = \frac{W}{I(\theta_{in})}$$

where  $\sigma$  is the scattered power per unit incident intensity and has dimensions of area.

$$\sigma_{\Omega}(\theta_{in}; \theta_{out}, \phi) = \frac{W_{\Omega}(\theta_{out}, \phi)}{I(\theta_{in})}$$

where

backscattering: The backscattering cross-section is defined as the differential cross-section evaluated in the backscattering direction, multiplied by  $4\pi$ 

$$\sigma^{back}(\theta) = 4\pi\sigma_{\Omega}(\theta; \theta, \phi) \tag{7}$$

#### 2.6 Single bubble model

Bubbles produce an acoustic signal owing to compression of the gas in the bubble. The 'spring' of the compressible gas and the mass of liquid around the bubble create a natural oscillator, sending a pressure oscillation through the liquid and interacting with the neighbouring bubbles [Anisotropy in the sound field generated by a bubble chain, J. Sound Vib. 278 (2004) 807–823.] This is so called coupled-oscillator theory under the self-consistent approach by describing the collective scattering due to individual bubble interaction with the others

Consists of calculating the volume of the backscattering strength by the one of models present in the literature (Thuraisingham).

A formula of the backscattering cross-section of an individual bubble, which is valid for a wide range of ka. This formula is derived by correcting a final factor reported by Thuraisingham. ([Zhang et al., 2022, p. 2-3])

$$\sigma_{bs} = \frac{a^2}{(\omega_0^2/\omega^2 - 1 - 2ka\beta_0/\omega)^2 + (2\beta_0/\omega + ka\omega_0^2/\omega^2)^2} \frac{(\sin(ka)/ka)^2}{1 + (ka)^2}$$
(8)

This is adapted from Ainslie and Leighton (2009, 2011) to include the final factor, which was proposed by Thuraisingham (1997). This expression implicitly includes radiation damping, with the effect of the other two damping mechanisms (viscous and thermal damping) being combined into a single damping factor, 0. This formulation provides a consistent approach to incorporating radiation damping into the backscattering model, something which, as Ainslie and Leighton (2011) showed, cannot be achieved using di-

mensionless damping coefficient, which is the prevailing approach (Veloso et al., 2015). In Equation 7, the frequency  $\omega_0$  is defined through the solution of the equation:

$$\omega_0 = \sqrt{\mathcal{R}\{\Omega^2(r,\omega)\}}\tag{9}$$

where  $\mathcal{R}\{\,\cdot\,\}$  denotes the real part of a complex number;

when the process is adiabatic or isothermal  $\omega_0$  is the resonant Minnaert angular frequency (undamped natural frequency) of a bubble vibrating volumetrically with small amplitude oscillations;

The backscattering cross-section of a single bubble can be presented as the target strength:

$$TS = 10\log \sigma_{bs} \tag{10}$$

natural frequency provided by bubble,

Minaert frequency and, Rayleigh-Plesset equation of air bubble.

- 3 Calculation
- 4 Results
- 5 Interpretation
- 6 Conclusion