

a) Calculator Class:

Algorithm evalExp(expression)

Input a String mathematical expression

Output result of the expression

tokens \leftarrow expression.split(" ")

while (!valStk.isEmpty())

valStk.pop()

i \leftarrow 0

while (i < tokens.length)

z \leftarrow tokens[i]

if (isNumber(z)) **then**

valStk.push(Double.parseDouble(z))

else if (z.equals("(")) **then**

while (!opStk.top().equals("("))

doOp()

opStk.pop()

else

repeatOps(z)

opStk.push(z)

i++

repeatOps("\$")

return valStk.top()

Algorithm repeatOps(op)

Input a String operator op

while (valStk.size() > 1 && prec(op) >= prec(opStk.top()))

if (opStk.top().equals("(")) **then**

break

doOp()

Algorithm doOp()

op \leftarrow opStk.pop()

x \leftarrow (double) valStk.pop()

y \leftarrow (double) valStk.pop()

switch (op)

case "+":

valStk.push(y + x)

break

case "-":

```

        valStk.push(y - x)
        break
    case "*":
        valStk.push(y * x)
        break
    case "/":
        valStk.push(y / x)
        break
    case "^":
        valStk.push(Math.pow(y, x))
        break
    case ">":
        if (y > x) then
            valStk.push(1.0);
        else
            valStk.push(0.0);
        break
    case "<":
        if (y < x) then
            valStk.push(1.0);
        else
            valStk.push(0.0);
        break
    case ">=":
        if (y >= x) then
            valStk.push(1.0);
        else
            valStk.push(0.0);
        break
    case "<=":
        if (y <= x) then
            valStk.push(1.0);
        else
            valStk.push(0.0);
        break
    case "==":
        if (y == x) then
            valStk.push(1.0);
        else
            valStk.push(0.0);
        break
    case "!=":
        if (y != x) then
            valStk.push(1.0);

```

```
    else
        valStk.push(0.0);
    break
```

Algorithm prec(op)

Input a String operator op

Output precedence of the operator

switch (op)

```
    case "(":
    case ")":
        return 1
    case "^":
        return 2
    case "*":
    case "/":
        return 3
    case "+":
    case "-":
        return 4
    case ">":
    case "<":
    case ">=":
    case "<=":
        return 5
    case "==":
    case "!=":
        return 6
    case "$":
        return 7
```

return -1

Algorithm isNumber(z)

Input a String z

Output true if the string is a number, false otherwise

try

```
    Double.parseDouble(z)
```

```
    return true
```

catch (NumberFormatException e)

```
    return false
```

b) The time complexity of the algorithm is $O(n)$, where n is the number of tokens in the expression. Each token is processed once, and the operations on the stacks are constant time operations, $O(1)$. The stack's size doubles when needed, maintaining an amortized constant time for push operations. The space complexity is also $O(n)$ due to the use of two stacks (valStk and opStk) to hold all values and operators. The space required is proportional to the number of elements in the input expression.