CONTENTS

Abstract—**This manual is an introduction to control systems based on GATE problems.Links to sample Python codes are available in the text.**

Download python codes using

1 STABILITY

1.1 Second order System

2 ROUTH HURWITZ CRITERION

3 COMPENSATORS

4 NYQUIST PLOT

4.1. Question-The open loop transfer function of a unity feedback system is given by

$$G(s) = \frac{\pi e^{-0.25s}}{s}$$

4.2. Find Re $\{G(j\omega)\}$ and Im $\{G(j\omega)\}$
Solution: substitute

$$S = j\omega \tag{4.2.1}$$

we get

$$G(j\omega) = -\frac{\pi}{\omega}(\sin 0.25\omega + j\cos 0.25\omega) \tag{4.2.2}$$

$$\text{Re}\{G(j\omega)\} = -\frac{\pi}{\omega}(\sin 0.25\omega) \tag{4.2.3}$$

$$\text{Im}\{G(j\omega)\} = -\frac{\pi}{\omega}(j\cos 0.25\omega) \tag{4.2.4}$$

4.3. Sketch the Nyquist plot.
Solution: The Nyquist plot is a graph of Re $\{G(j\omega)\}$ vs Im $\{G(j\omega)\}$. The following python code generates the Nyquist plot in Fig. 4.3
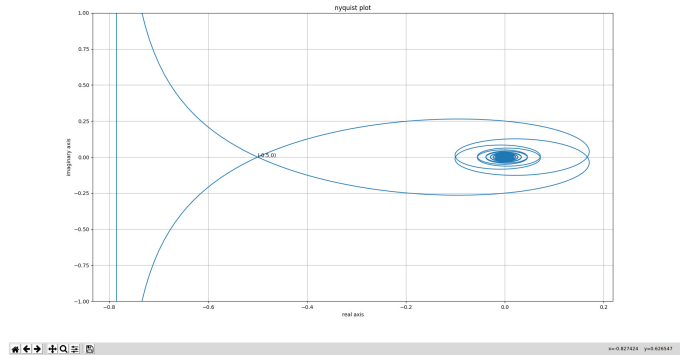
codes/ee18btech11007/nyquist.py

Fig. 4.3

4.4. Find the point at which the Nyquist plot of G(s) passes through negative real axis
Solution:

$$G(s) = \frac{\pi e^{-0.25s}}{s} \tag{4.4.1}$$

Nyquist plot cuts the negative real Axis at $\omega =$ phase cross over frequency,at phase cross over frequency the phase of nyquist plot becomes $-\pi$ radians.
substitute

$$s = j\omega. \tag{4.4.2}$$

$$G(j\omega) = -\frac{\pi}{\omega}(\sin 0.25\omega + j\cos 0.25\omega) \tag{4.4.3}$$

$$\angle G(j\omega) = -\pi/2 - 0.25\omega. \tag{4.4.4}$$

$$\angle G(j\omega)|_{\omega=\omega_{pc}} = -\pi \tag{4.4.5}$$

by solving for ω we get $\omega_{pc} = 2\pi$.
magnitude at any point is

$$X = |G(j\omega)| = \frac{\pi}{\omega}. \tag{4.4.6}$$

substituting $\omega = 2\pi$ in magnitude equation we get X=0.5.

so it intersects at (-0.5,0j)

we can verify with the following plot that it intersects at (-0.5,0j)

4.5. Use Nyquist stability criterion to determine if the system is stable?
Solution: Nyquist Stability Criterion - for the stability of a closed loop transfer function

G(s)/(1+G(s)*H(s)) ,the number of poles of G(s)*H(s) on right half of s-plane must equal the number of encirclement of nyquist contour of G(s)*H(s) about the critical point -1+0j

we must find

$$Z = P + N \qquad (4.5.1)$$

Variable	Description
Z	no of poles of G(s)/(1+G(s)*H(s)) in the right half of s-plane
P	no of poles of G(s)*H(s) in right half of s-plane
N	no of encirclement of G(s)*H(s) about -1+j0 in clockwise direction

NOTE-

- If a clockwise contour does not encircle zeros nor poles, then the plot will not encircle the origin.
- If a clockwise contour encircles a zero, then the plot will encircle the origin clockwise once.
- If a clockwise contour encircles a pole, then the plot will encircle the origin counterclockwise once.

from plot we get N=0 because there are no encirclements about -1+0j,and we already know P=0 since our G(s) doesnt have any poles on right half of s-plane

$$Z = 0 + 0 = 0 \qquad (4.5.2)$$

$\therefore$ the system is stable.