### Predictive Models for Credit Card Default

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- Preliminary Data Analysis
  - Outlier Detection: Mahalanobis distance
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- Parametric Methods
  - Lasso, Ridge, Elastic, Logistic Regression, Naive Bayes, LDA
- Non parametric Methods
  - K-Nearest Neighbors, Random Forest
- 6 Conclusion



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# Background

It is a necessity for banks to construct models to decide whether a client would default his credit card payment.

- Credit risk is the traditional risk of banking industry and managing credit risk has been a key part of the banking business.
- To increase market share, the credit card issuers over-issued credit cards to many unqualified applicants.
- Card holders overused credit card regardless of their repayment ability.
- It would be too expensive have a close background check for each individual applicants



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### Data

### Payment data from a bank in Taiwan in October, 2005

Variable Name	Description	
Y	Default status	
$LIMIT_{BAL}$	Credit limit	
SEX	Gender	
EDUCATION	Education	
MARRIAGE	Marital status	
AGE	Age	
$PAY_0 - PAY_6$	Historical payment	
$BILL_{AMT1} - BILL_{AMT6}$	Bill statement amount	
$PAY_{AMT1} - PAY_{AMT6}$	Previous payment amount	

### Outlier Detection

- Use Mahalanobis distance to detect outliers
- 95% quantile from the chi-square distribution

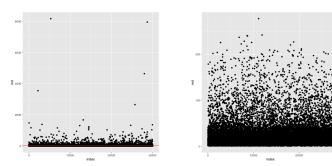


Figure: Mahalanobis Distance



### **Dimension Reduction**

- There is a strong linear relationship between some predictors
- Collinearity will cause problems for our later model fitting

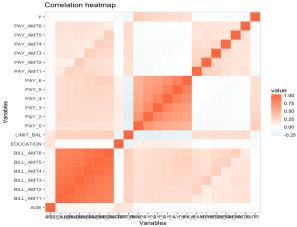
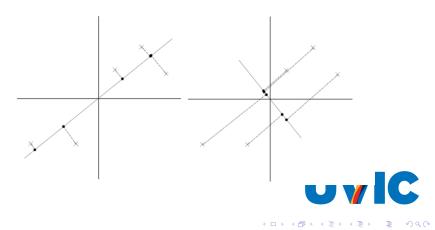




Figure: Correlation Heatmap for Predictors

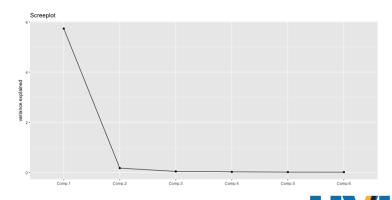
# Principal Component Analysis

- Principal component: Linear combination of inputs
- Aim: Capture as much of the variation as possible



# Principal Component Analysis

### Plot of variance (Scree plot) for each PC





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### **Evaluation Criteria**

We use the following criteria to compare our models.

- Accuracy
- ROC Curve
- Lift Chart



### Confusion Matrix

		Actual Class	
		Positive(1)	Negative (0)
Predicted Class	Positive(1)	TP	FP
	Negative(0)	FP	TN
		Sensitivity	1-Specificity
		$TPR = \frac{TP}{TP + FN}$	$FPR = \frac{FP}{FP+TN}$

Table: Table of Confusion

$$\begin{array}{l} {\sf Accuracy} = \frac{TP + TN}{P + N}, \\ {\sf where} \ P = TP + FN \ {\sf and} \ N = FP + TN \end{array}$$



# Brief Introduction to ROC

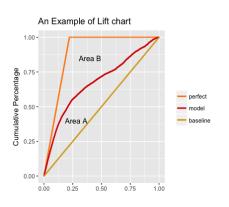
Given a set of prediction and a ranking classifier:

- Order the prediction by the probability from the highest to the lowest
- start from (1-FPR=0,TPR=0)
- for each prediction x in the sorted order if x is True Positive, move one step up if x is True Negative, move one step right
- evaluate AUC, where

$$AUC_{ROC} = \int_0^1 \frac{TP}{P} d\frac{FP}{N}$$



### Lift Chart



- A twist of ROC curve
- Depends on P:N ratio
- y-axis: TPR
- x-axis:  $\frac{TP+FP}{P+N}$

**GLM Final Project** 

- Baseline represents random predictions.
- Prefect line represents predictions without misclassification.
- Comparing criterion: Accuracy-ratio, where Accuracy-ratio= $\frac{Area_A}{Area_A+Area_B}$



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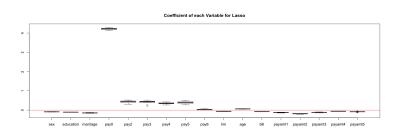


# Fit Lasso, Ridge and Elastic net model

- 10-fold Cross-Validation
- For Lasso, Ridge and Elastic net, fit each model with 1se and min lambda.
- When fitting elastic net, use second layer of CV to decide weight between L1 and L2 penalty.

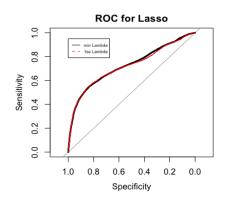


# Compare the Importance of each Variable by its Coefficient





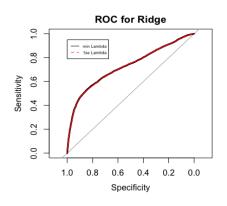
# ROC curve for Lasso and AUC



- Sensitivity = TPR
- Specificity = 1-FPR
- AUC (Lasso with min lambda)
   = 0.7252
- AUC (Lasso with 1se lambda) = 0.7217



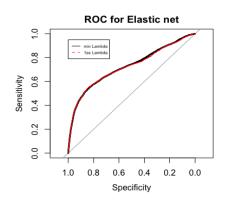
# ROC curve for Ridge and AUC



- Sensitivity = TPR
- Specificity = 1-FPR
- AUC (Ridge with min lambda)
   = 0.726
- AUC (Ridge with 1se lambda) = 0.7256



# ROC curve for ELastic net and AUC



- Sensitivity = TPR
- Specificity = 1-FPR
- AUC (Elastic net with min lambda)
   = 0.7254
- AUC (Elastic net with 1se lambda)= 0.723



# Compare Area Under Curve (AUC)

Table: AUC table

Model	AUC
Ridge with min Lambda	0.726
Ridge with 1se Lambda	0.7256
Lasso with min Lambda	0.7252
Lasso with 1se Lambda	0.7217
Elastic net with min Lambda	0.7254
ELastic net with 1se Lambda	0.723



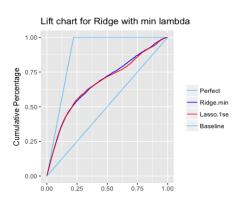
# Compare Accuracy Rate (With the best threshold)

Table: Accuracy Rate table

Model	Threshold	Accuracy
Ridge with min Lambda	0.4134485	0.8170759
Ridge with 1se Lambda	0.4101963	0.8160653
Lasso with min Lambda	0.4229622	0.8178245
Lasso with 1se Lambda	0.4069446	0.8192843
Elastic net with min Lambda	0.4257687	0.8180491
ELastic net with 1se Lambda	0.4063384	0.8173379



### Lift Chart



- Accuracy-ratio (Ridge with min lambda)
  - = 0.4519638
- Accuracy-ratio (Lasso with 1se lambda)
  - = 0.4434366



### Logistic Regression

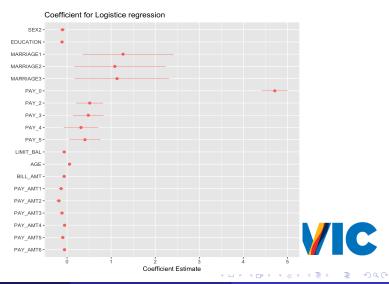
#### Basic Idea:

- Logistic regression is the type of regression we use for a response variable (Y) that follows a binomial distribution
- Model the log odds of the event (in our case, default) as a function of predictor variables

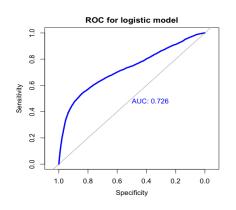


## Logistic Regression

Coefficient for the Logistic regression after variable selection (AIC)



# ROC Curve for Logistic Regression

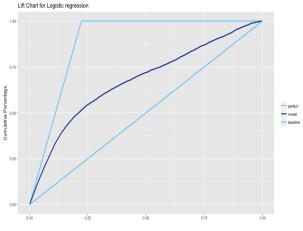


- Sensitivity = TPR
- Specificity = 1-FPR
- AUC = 0.726
- optimal cutoff = 0.4369
- accuracy rate = 0.817



# Logistic Regression

- Lift Chart for Logistic Regression
- Accuracy Ratio = 0.4521



# Machine Learning Models

### Non-parametric models:

- K-Nearest Neighbors
- Tree methods: Decision Tree and Random Forest

#### Parametric models:

- Linear Discriminant Analysis
- Naive Bayes



# Machine Learning Models

### Non-parametric models:

- K-Nearest Neighbors
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#### Parametric models:

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#### Criteria:

Area Under Curve (AUC) and Accuracy



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- Select a positive integer k
- Select closest k points near the new sample
- Find most common classification

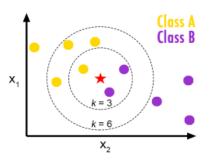


Figure: KNN Algorithm



- Select a positive integer k
- Select closest k points near the new sample
- Find most common classification

How do we select k?

- Try  $k = 1, 2, \dots, 100$
- 10-fold cross validation

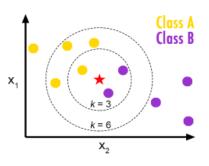


Figure: KNN Algorithm



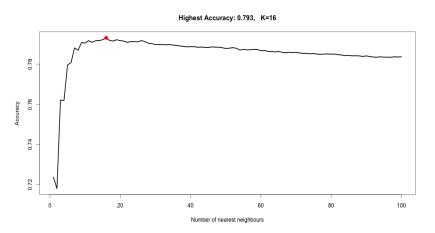


Figure: Tuning parameter: k



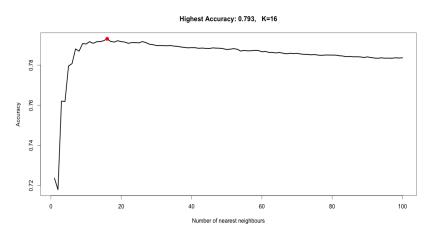


Figure: Tuning parameter: k



AUC: 0.547

### Tree Methods

#### Decision Tree:

- Visual representation
- Accommodate non-linear relations
- Easy to be interpreted!



## Decision Tree

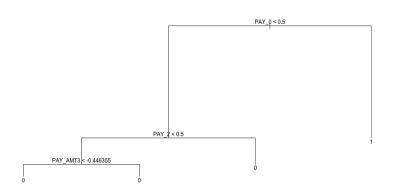


Figure: Decision Tree Before Pruning



#### Decision Tree

```
CP nsplit rel error xerror xstd
1 0.1853609 0 1.0000000 1.0000000 0.01148927
2 0.0100000 1 0.8146391 0.8146391 0.01063895

Variable importance
PAY_0 PAY_5 PAY_2 PAY_6 PAY_4 PAY_3
93 2 1 1 1 1
```

Figure: Complexity Parameter



#### **Decision Tree**

#### **Decision Tree After Pruning**

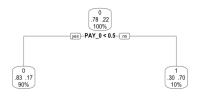


Figure: Decision Tree After Pruning



#### Tree Methods

#### Random Forest:

- More robust than decision tree using bootstrap
- Randomly select observations and predictors
- Majority rule



#### Random Forest

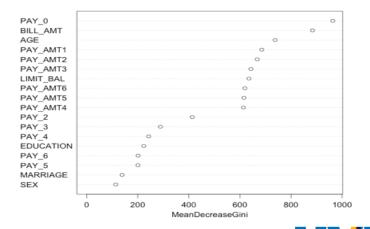


Figure: Importance of Variables



#### Random Forest

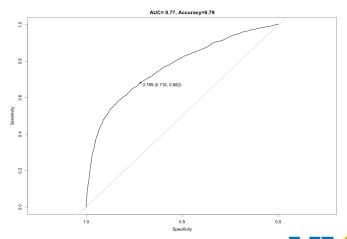


Figure: Random Forest: AUC



#### Random Forest

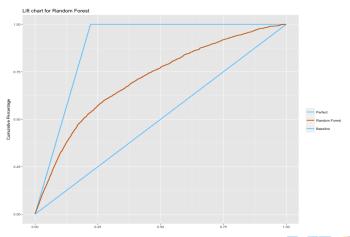


Figure: Accuracy ratio: 0.549



#### Parametric models

#### Linear Discriminant Analysis:

- Commonly used method to reduce high dimensions
- Find boundaries around clusters of classes

#### Naive Bayes:

Probabilistic classifiers based on applying Bayes' theorem



#### Parametric models

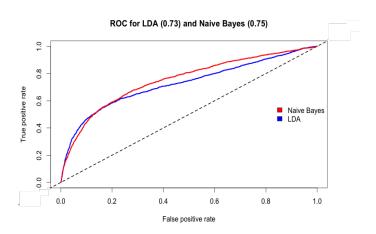


Figure: LDA v.s. Naive Bayes



# Model Comparison

Table: Best Model Comparison

Model	AUC	Accuracy
Random Forest	0.77	0.787
KNN	0.54	0.793
Logistic	0.73	0.816
Ridge (min)	0.73	0.817
Lasso (1se)	0.72	0.819
LDA	0.73	0.812
Naive Bayes	0.75	0.810



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# Conclusion

Table: Model Comparison

Model	Accuracy Ratio
Random Forest	0.539
Ridge (min)	0.452
Lasso (1se)	0.443
Logistic	0.452



#### Conclusion

Table: Model Comparison

Model	Accuracy Ratio
Random Forest	0.539
Ridge (min)	0.452
Lasso (1se)	0.443
Logistic	0.452

Random forest wins!



## Reference

- [1] Baesens B, Van Gestel T, Viaene S, Stepanova M, Suykens J, Vanthienen J. Benchmarking state-of-the-art classification algorithms for credit scoring. Journal of the operational research society. 2003 Jun 1:54(6):627-35.
- [2] Härdle W, Simar L. Applied multivariate statistical analysis. Berlin: Springer; 2007 Aug 9.
- [3] James G, Witten D, Hastie T, Tibshirani R. An introduction to statistical learning. New York: springer; 2013 Feb 11.
- [4] Yeh IC, Lien CH. The comparisons of data mining techniques for the predictive accuracy of probability of default of credit card clients. Expert Systems with Applications. 2009 Mar 1;36(2):2473-80.
- [5] Data source https://www.kaggle.com/uciml/default-of-credit-call

# Thank You

