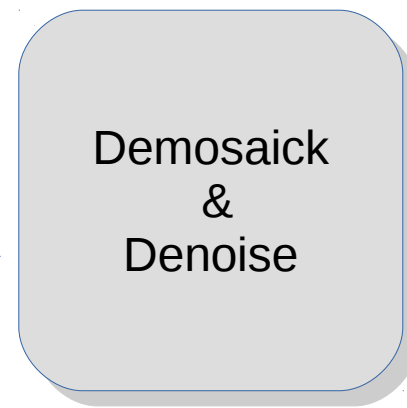
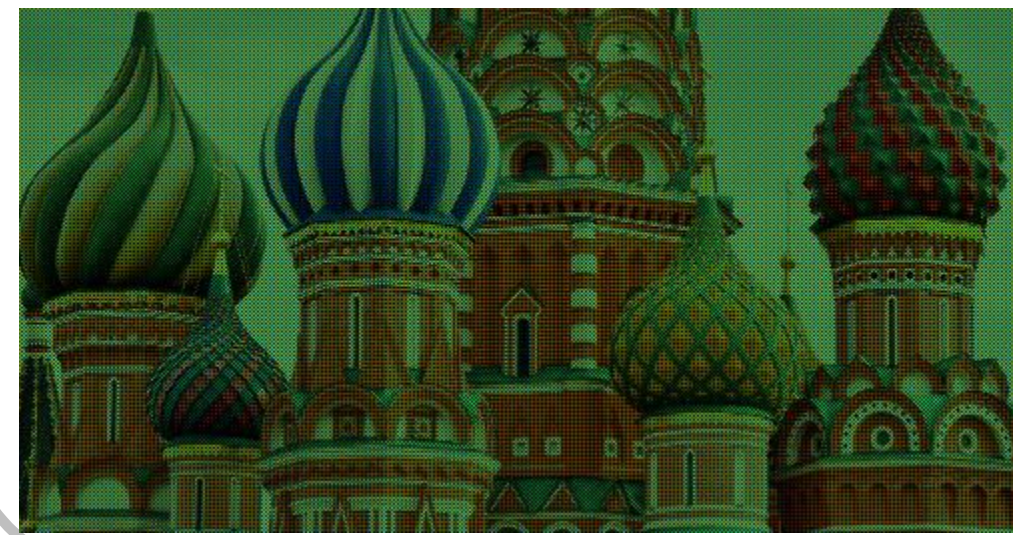




### 1. Motivation - Contributions

- Demosaicking and denoising are among the most crucial steps of modern digital camera pipelines and their joint treatment is a highly ill-posed inverse problem where at-least two-thirds of the information are missing and the rest are corrupted by noise.
  - Reconstruction errors in the early stages produce unsatisfying end results.
- We designed a **novel deep network** that
  - is inspired by classical image regularization approaches and optimization strategy.
  - tackles the demosaicking and denoising problem **jointly**.
  - performs very well even when trained on small datasets and using a small number of parameters.
  - works with any Color Filter Array (CFA).

Noisy Light Intensity Measurements



End Result



### 2. Problem Formulation

- Demosaicking : estimate  $\mathbf{x} \in \mathbb{R}^N$  according to the model :  $\mathbf{y} = \mathbf{M}\mathbf{x} + \mathbf{n}$ 
  - $\mathbf{M} \in \mathbb{R}^{N \times N}$  is a diagonal binary and singular matrix that models the CFA pattern
- Variational problem formulation (P1):

$$Q(\mathbf{x}) = \arg \min_{\mathbf{x}} \frac{1}{2\sigma^2} \|\mathbf{y} - \mathbf{M}\mathbf{x}\|_2^2 + \phi(\mathbf{x})$$

- Two challenges arise, how to:
  - Efficiently minimize  $Q(\mathbf{x})$  function
  - Properly define  $\phi(\mathbf{x})$  to constrain the set of solutions
- We opt to design a network that successfully overcomes both challenges

### 3. Majorization Minimization (MM) Framework

- Minimize (P1) via successive minimization of a surrogate/majorizer function  $\tilde{Q}(\mathbf{x}, \mathbf{x}^{(t)})$  that upper-bounds (P1)
- Iteratively solve  $\mathbf{x}^* = \arg \min_{\mathbf{x}} Q(\mathbf{x})$  via  $\mathbf{x}^{(t+1)} = \arg \min_{\mathbf{x}} \tilde{Q}(\mathbf{x}; \mathbf{x}^{(t)})$
- Where  $\tilde{Q}(\mathbf{x}; \mathbf{x}^{(t)}) > Q(\mathbf{x}), \forall \mathbf{x} \neq \mathbf{x}^{(t)}$  and  $\tilde{Q}(\mathbf{x}^{(t)}; \mathbf{x}^{(t)}) = Q(\mathbf{x}^{(t)})$
- Deriving a **majorizer of the data-fidelity term**:
 
$$\tilde{d}(\mathbf{x}, \mathbf{x}_0) = \frac{1}{2\sigma^2} \|\mathbf{y} - \mathbf{M}\mathbf{x}\|_2^2 + d(\mathbf{x}, \mathbf{x}_0)$$
  - Where  $d(\mathbf{x}, \mathbf{x}_0) = \frac{1}{2\sigma^2} (\mathbf{x} - \mathbf{x}_0)^T [\alpha \mathbf{I} - \mathbf{M}] (\mathbf{x} - \mathbf{x}_0)$  is a distance function between  $\mathbf{x}$  and  $\mathbf{x}_0$
  - For requirements to hold,  $d(\mathbf{x}, \mathbf{x}_0)$  needs to be PSD matrix therefore  $\alpha > \|\mathbf{M}\|_2 \geq 1$
- The majorizer take the following form that **resembles a denoising problem (P2)**:

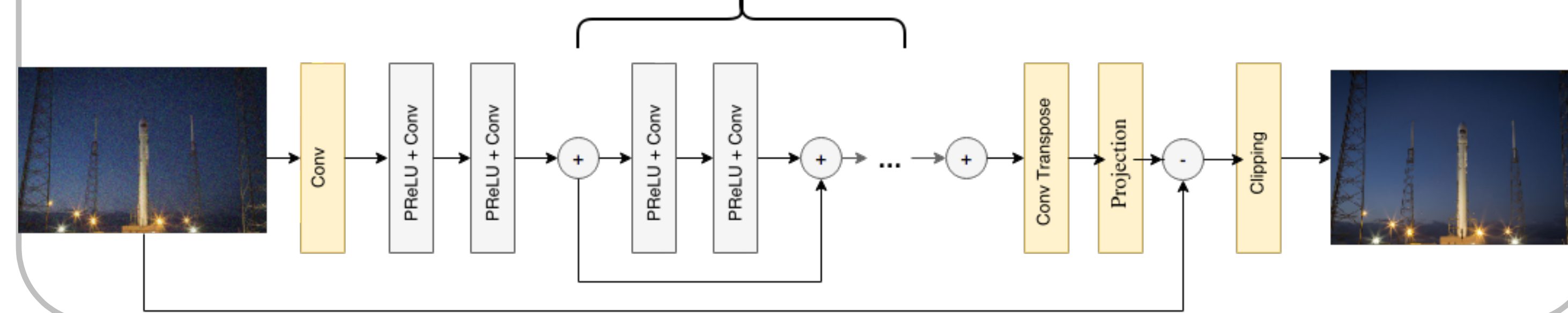
$$\tilde{Q}(\mathbf{x}, \mathbf{x}_0) = \frac{1}{2(\sigma/\sqrt{a})^2} \|\mathbf{x} - \mathbf{z}\|_2^2 + \phi(\mathbf{x}) + c, \text{ where } \mathbf{z} = \mathbf{y} + (\mathbf{I} - \mathbf{M})\mathbf{x}_0$$

### 4. Residual Denoising Network (ResDNet)

- We need to derive a network that works for a **wide range of noise levels** to solve (P2)
  - Make use of  $D$  CNNs layers with weight normalization and PReLU activation function
  - Implement a residual approach to subtract the noise realization
- Projection Layer normalizes the noise realization estimate to have the desired variance  $\sigma$ .

$$\mathcal{P}_c(\mathbf{y}) = \varepsilon \frac{\mathbf{y}}{\max(\|\mathbf{y}\|_2, \varepsilon)}, \varepsilon = e^{\gamma\theta}, \theta = \sigma\sqrt{N-1}$$

Number of pixels



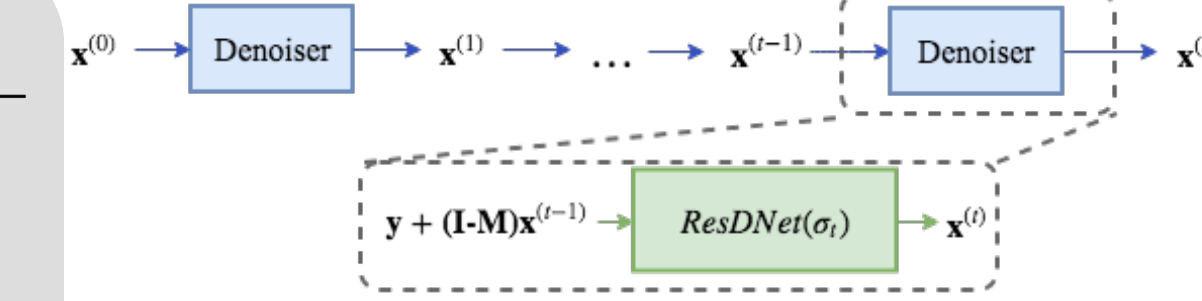
### 5. Demosaicking Network Architecture

- Unroll  $K$  **Majorization Minimization iterations** as a network and use *ResDNet* for each denoising step
  - Promote parameter sharing in each step to keep a low number of parameters (~380.000)
  - Extrapolate results of each iteration to accelerate MM Framework

**Algorithm 1:** The proposed demosaicking network described as an iterative process. The ResDnet parameters remain the same in every iteration.

**Input:**  $\mathbf{M}$  : CFA,  $\mathbf{y}$  : input,  $K$  : iterations,  $\mathbf{w} \in \mathbb{R}^K$  : extrapolation weights,  $\sigma \in \mathbb{R}^K$  : noise vector

$\mathbf{x}^0 = 0, \mathbf{x}^1 = \mathbf{y};$   
**for**  $i \leftarrow 1$  **to**  $K$  **do**  
      $\mathbf{u} = \mathbf{x}^{(i)} + \mathbf{w}_i(\mathbf{x}^{(i)} - \mathbf{x}^{(i-1)});$   
      $\mathbf{x}^{(i+1)} = \text{ResDNet}((\mathbf{I} - \mathbf{M})\mathbf{u} + \mathbf{y}, \sigma_i);$   
**end**



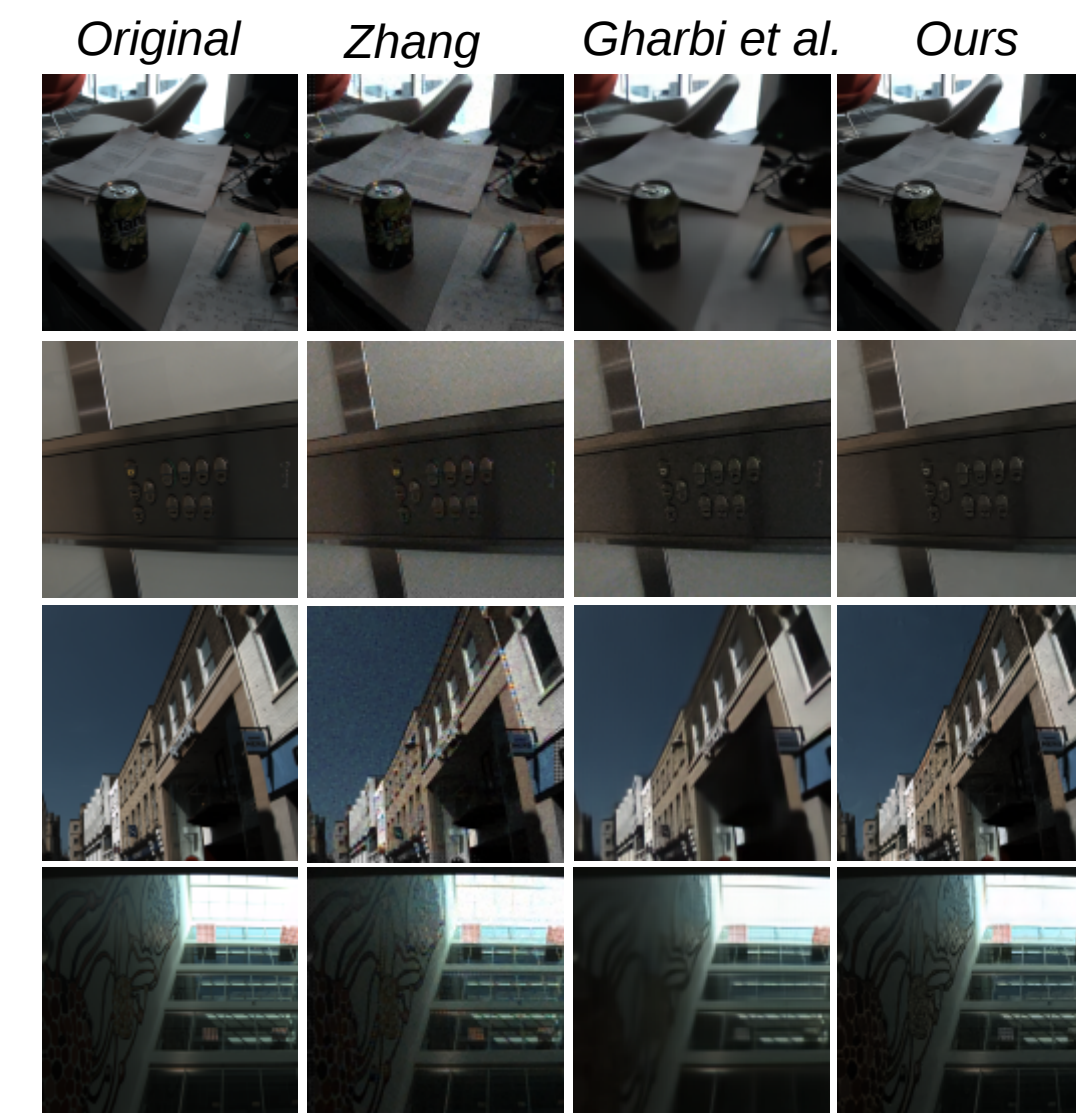
### 6. Comparisons & Results

- Bayer Demosaicking PSNR performance evaluation:

	noise-free		noisy	
	linRGB	sRGB	linRGB	sRGB
<b>Non-ML Methods:</b>				
bilinear	30.9	24.9	-	-
Zhang(NLM) [2]	38.4	32.1	-	-
Getreuer [41]	39.4	32.9	-	-
Heide [5]	40.0	33.8	-	-
<b>Trained on MSR Dataset:</b>				
Khasabi [14]	39.4	32.6	37.8	31.5
Klatzer [19]	40.9	34.6	38.8	32.6
Bigdeli [42]	-	-	38.7	-
ours	<b>41.0</b>	<b>34.6</b>	<b>39.2</b>	<b>33.3</b>
<b>Trained on MIT Dataset:</b>				
Gharbi (sRGB)[20]	41.6	35.3	38.4	32.5
Gharbi (linRGB)	<b>42.7</b>	<b>35.9</b>	38.6	32.6
ours* (linRGB)	42.6	<b>35.9</b>	N/A	N/A

- Evaluation an simulated data:

	Kodak McM Vdp Moire			
<b>Non-ML Methods:</b>				
bilinear	32.9	32.5	25.2	27.6
Adobe Camera Raw 9	33.9	32.2	27.8	29.8
Buades [4]	37.3	35.5	29.7	31.7
Zhang (NLM) [2]	37.9	36.3	30.1	31.9
Getreuer [41]	38.1	36.1	30.8	32.5
Heide [5]	40.0	38.6	27.1	34.9
<b>Trained on MSR Dataset:</b>				
Klatzer [19]	35.3	30.8	28.0	30.3
ours	39.2	34.1	29.2	29.7
<b>Trained on MIT Dataset:</b>				
Gharbi [20]	41.2	39.5	34.3	<b>37.0</b>
ours*	<b>41.5</b>	<b>39.7</b>	<b>34.5</b>	<b>37.0</b>



- Fuji XTRANS Demosaicking evaluation:

	noise-free	
	linear	sRGB
<b>Trained on MSR Dataset:</b>		
Khashabi [14]	36.9	30.6
Klatzer [19]	39.6	33.1
ours	<b>39.9</b>	<b>33.7</b>
<b>Trained on MIT Dataset:</b>		
Gharbi [20]	39.7	33.2