CSE 240A Branch Predictor Project:
G-Share, Tournament, and a Custom TAGE Implementation

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Abstract

Branch prediction is a critical optimization in modern CPU microarchitecture, allowing processors to reduce pipeline stalls and improve instruction throughput. This project implements three branch predictors—G-Share, Tournament, and a custom TAGE-based predictor—within a common simulator framework. We present the overall design, implementation, experimental observations, and final results on six benchmark trace files. The TAGE predictor achieves the best accuracy, significantly outperforming simpler G-Share and Tournament schemes. Memory usage for each predictor is analyzed to ensure compliance with the 64K+256-bit constraint.

1 Introduction

In modern high-performance processors, *branch prediction* is used to anticipate the direction of branch instructions before they are resolved, thus reducing stall cycles caused by control hazards. Various prediction schemes exist, trading off complexity and accuracy.

In this project, we:

- Implement a **G-Share** predictor using global history registers.

- Implement a **Tournament** predictor combining local and global schemes via a meta-predictor.

- Propose a **Custom** TAGE-based predictor that uses multiple tagged prediction tables of differing history lengths.

Our experimentation involves six traces representing a broad range of workloads: integer, floating-point, and memory-intensive. We measure misprediction rates, memory usage, and highlight each predictor's advantages and disadvantages.

2 Implementation

This section details the workings of each predictor, their configurations, and the pros and cons of each.

2.1 G-Share Predictor

High-Level Concept   G-Share uses a Global History Register (GHR) of length N bits. To predict an upcoming branch, it XORs these N bits of the GHR with the lower N bits of the Program Counter (PC) to index into a table of 2-bit saturating counters. A typical 2-bit saturating counter has states $\{$`SN`, `WN`, `WT`, `ST`$\}$, with transitions based on whether the branch was taken or not.

Advantages

- Simple to implement and relatively compact.

- Captures some global correlation via the XOR of history and PC bits.

Disadvantages

- Can suffer from *aliasing* if many different branches map to the same table entries.

- Does not directly capture strong local correlations.

Historical Evolution   G-Share was introduced as an improvement over basic bimodal predictors, mitigating some aliasing by mixing PC bits with a global history pattern [1].

2.2 Tournament Predictor

High-Level Concept   Tournament prediction [2] blends:

1. A *Global* predictor indexed by a global history register.

2. A *Local* predictor keyed by PC-based local histories.

3. A *Meta-* or *Choice* predictor that decides on a per-branch basis whether to trust local or global prediction.

Advantages

- Adapts to both local and global correlation patterns within the same workload.

- Often achieves better accuracy than a purely global or purely local approach.

Disadvantages

- More storage overhead (multiple tables) compared to G-Share alone.

- Must keep track of and update three separate structures: global, local, and choice.

Historical Evolution   First proposed by McFarling [2], the basic tournament approach is still used in contemporary commercial designs (with additional enhancements and refinements).

2.3 Custom TAGE Predictor

High-Level Concept The TAGE (**TA**gged **GE**ometric) family [3, 4, 5] extends the idea of combining multiple predictor components with *tagged* tables, each using differently *geometrically increasing* history lengths. TAGE tracks short- and long-range history segments in parallel. When a misprediction occurs, it dynamically decides if and how to allocate new entries in one of these tagged tables.

Advantages

- State-of-the-art accuracy on many benchmark suites.

- Adapts well to varying branch behaviors and path-based correlation.

Disadvantages

- Complex design and more sophisticated update policies.

- Requires careful parameter tuning to remain within hardware budgets (e.g., 64K bits).

Historical Evolution TAGE and its variants have repeatedly topped academic branch predictor competitions. Seznec [4] demonstrated that properly tuned TAGE-style predictors approach very low misprediction rates while respecting hardware constraints.

3 Observation and Experimental Results

We ran the predictor simulator on six distributed traces:

- `int_1`, `int_2` (Integer workloads)

- `fp_1`, `fp_2` (Floating-point workloads)

- `mm_1`, `mm_2` (Memory-intensive workloads)

Each run reports:

- Number of branch instructions processed

- Mispredictions encountered

- Misprediction rate (%)

- Approximate memory usage (bits)

3.1 Final Results (from `runall.sh`)

Table 1 summarizes the final misprediction rates observed for:

- `Static` predictor (always predict Taken),

- `G-Share` with 13 bits of global history,

- `Tournament` with `ghistoryBits = 9`, `lhistoryBits = 10`, and `pcIndexBits = 10`,

- `Custom TAGE` using our default multi-bank configuration.

Trace	Static (%)	G-Share:13 (%)	Tourn:9:10:10 (%)	TAGE (%)
int_1	44.136	13.839	12.622	6.592
int_2	5.508	0.420	0.426	0.254
fp_1	12.128	0.825	0.991	0.767
fp_2	42.350	1.678	3.246	0.236
mm_1	50.353	6.696	2.581	0.343
mm_2	37.045	10.138	8.483	5.292

Table 1: Final Misprediction Rates (%) for the 6 Traces (from `runall.sh`)

Analysis.

1. **Static** performs poorly on most traces, confirming the necessity of dynamic branch prediction.

2. **G-Share** yields substantial accuracy gains over Static but is outperformed by Tournament on several workloads.

3. **Tournament** typically does better than G-Share, reflecting the benefit of combining local and global components.

4. **TAGE** significantly reduces mispredictions across the board, highlighting the power of multi-length history tracking.

3.2 Memory Usage

Our code prints approximate bit usage for each predictor:

- *G-Share (13 bits)*: $2^{13} \times 2 = 16384$ bits

- *Tournament (9:10:10)*: $\underbrace{(2^9 \times 2) + (2^9 \times 2)}_{\text{Global + Choice}} + \underbrace{(2^{10} \times 2^{10} \times \dots)}_{\text{Local}} \approx 14\text{kb total}$

- *TAGE (Custom)*: The multi-bank structure sums to about 63.25kb (63,250 bits), which satisfies the $64\text{K} + 256$ bit limit.

4 Extensions: Additional Experiments

Beyond the final settings, we performed extended sweeps of G-Share and Tournament parameters across various `ghistoryBits`, `lhistoryBits`, and `pcIndexBits`. Figures 1 and 2 present two of these visualizations:

- **G-Share Sweep (Figure 1)**: We vary `ghistoryBits` from 8 to 16, plotting misprediction rate for each of the six traces and an overall average line. As the history length grows, accuracy generally improves, though memory usage also increases.

- **Tournament Heatmap (Figure 2)**: For each of four `pcIndexBits` values (9 to 12), we map `ghistoryBits` (horizontal) vs. `lhistoryBits` (vertical) and color the cell by the *average* misprediction rate across all six traces. Darker (blue) regions indicate lower misprediction rates, while lighter (yellow) regions indicate higher misprediction rates.
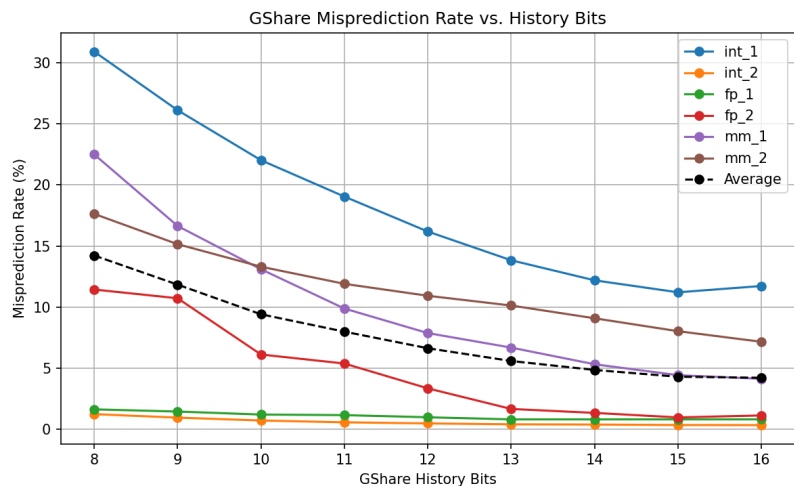
Figure 1: G-Share Misprediction Rate vs. History Bits (8–16) for the Six Traces + Average
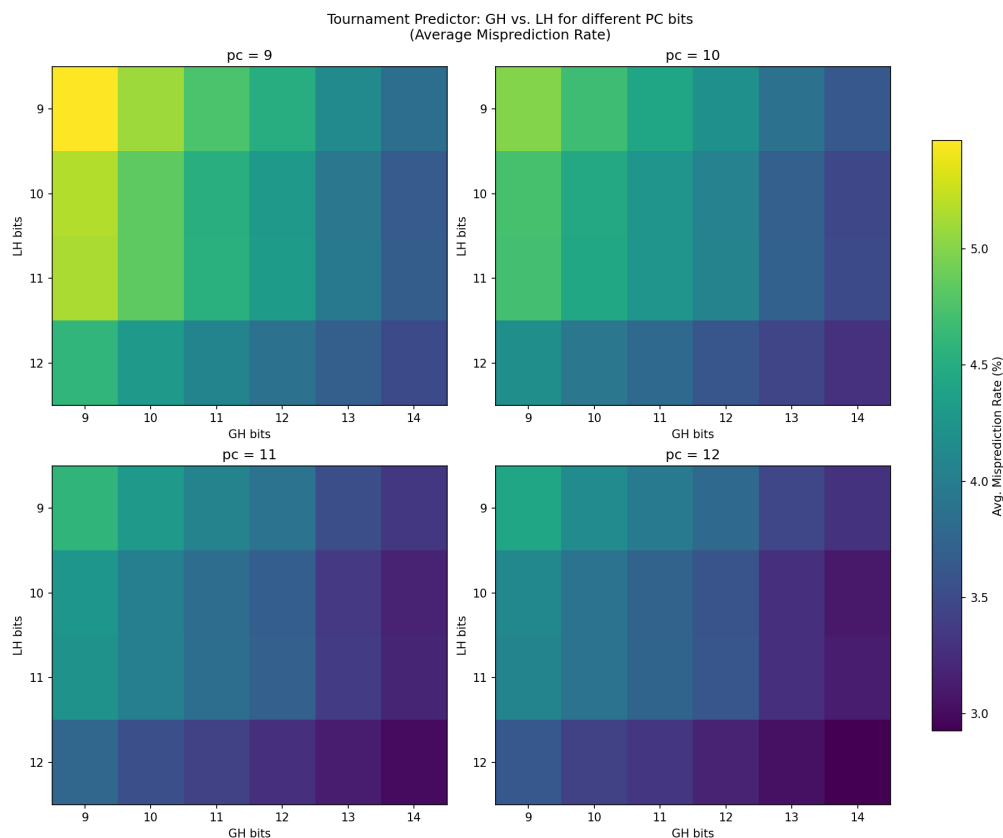

Figure 2: Tournament Predictor: GH vs. LH for Different PC Bits (Average Misprediction Rate)

Overall, these sweeps reveal how increasing history length generally improves accuracy but also increases storage cost. In the tournament predictor heatmaps, `pcIndexBits` around 10–12 combined with moderate `ghistoryBits` and `lhistoryBits` can yield strong performance. The sweet spot in each subfigure often balances the trade-off between local and global correlation capture.

5 Results and Conclusion

Summary of Findings.

- TAGE outperforms simpler schemes in every tested scenario, though it uses more complex data structures.

- Tournament is a balanced design, typically besting G-Share, especially on memory-heavy traces.

- G-Share is a well-known baseline, relatively simple and fairly robust, but not as adaptive as Tournament or TAGE.

- Static is uniformly poor across the traces, highlighting the importance of dynamic branch prediction.

Future Work.

- **Perceptron or ML-based Branch Prediction:** Investigate neural methods.

- **Further TAGE Tuning:** Adjusting bank sizes, tags, or path history lengths for optimal coverage.

- **Hybrid Schemes:** Combine TAGE with other advanced predictors (e.g., loop predictors) to handle highly repetitive branches.

References

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[2] S. McFarling, "Combining Branch Predictors," *WRL Technical Note TN-36*, Digital Equipment Corporation, 1993. `https://www.ece.ucdavis.edu/~akella/270W05/mcfarling93combining.pdf`

[3] A. Seznec and P. Michaud, "A Case for (Partially) TAgged GEometric History Length Branch Prediction," *Journal of Instruction-Level Parallelism*, 2006. `https://www.irisa.fr/caps/people/seznec/JILP-COTTAGE.pdf`

[4] A. Seznec, "A 256Kbits L-TAGE Branch Predictor," *Journal of Instruction-Level Parallelism*, 2007. `https://www.irisa.fr/caps/people/seznec/L-TAGE.pdf`

[5] A. Seznec, "TAGE-SC-L Branch Predictors Again," *Journal of Instruction-Level Parallelism*, 2011. `https://www.cs.cmu.edu/~18742/papers/Seznec2011.pdf`

A Appendix: AI Tool Usage and Chat Logs

A.1 Overview

In compliance with the project requirement to cite AI assistance and include prompts + outcomes, this appendix contains the key conversations with OpenAI's ChatGPT (model gpt-4o). Below are excerpts showcasing how the tool was used to help debug code, generate example snippets, and provide explanatory text. All of these AI-generated outputs were manually reviewed and substantially adapted.

A.2 Conversation 1: TAGE predictor counter debug

Me: I have a partially implemented TAGE predictor in C code, but I'm running into a

GPT-4o: Absolutely, I'd be glad to help you debug your TAGE predictor implementatio

To dig into it properly, could you share:

1. The relevant code snippet for your **TAGE table entry structure**, especially th
2. The part of the code where you **update** the saturating counters.
3. The defined **limits** for your saturating counters (e.g., are they 2-bit? 3-bit

With that info, I can pinpoint exactly where the issue is. In the meantime, here ar

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Quick Checks for Debugging

1. **Counter Saturation Boundaries**:
   Make sure you're checking boundaries before updating:
   ```c
   if (entry.counter < MAX_COUNTER) {
       entry.counter++;
   }
   ```
   and
   ```c
   if (entry.counter > MIN_COUNTER) {
       entry.counter--;
   }
   ```

2. **Bit-width Constants**:
   If your counters are, say, 3-bit (i.e., range -4 to 3 for signed, or 0 to 7 for
   – You're using the correct type (signed vs. unsigned).
   – Your increments/decrements respect the upper/lower limits.

3. **Initialization**:
   Counters should be initialized to a neutral state, typically 0 or mid-range.

4. **Sign Confusion**:
   Are you using a signed saturating counter and treating it like an unsigned one

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If you're not sure where the issue is, paste the key sections of your code here, an

Me: Yeah here's the code:

```
static inline void tage_train(uint32_t pc, uint8_t outcome) {
    int needAllocate = 0;
    if (primaryBank < NUM_BANKS) {
        int8_t pCtr = tageBank[primaryBank].entry[ bankGlobalIndex[primaryBank] ].s
        // If mispredicted and the sign of pCtr is opposite the actual outcome => n
        if ((lastPrediction != outcome) && ((pCtr >= 0) != outcome)) {
            needAllocate = 1;
        }
    } else {
        needAllocate = (lastPrediction != outcome);
    }

    if (needAllocate) {
        int8_t minUse = 127;
        for (int i = 0; i < primaryBank; i++) {
            int8_t u = tageBank[i].entry[ bankGlobalIndex[i] ].usefulness;
            if (u < minUse) {
                minUse = u;
            }
        }
        if (minUse > 0) {
            for (int i = primaryBank - 1; i >= 0; i--) {
                // This might decrement usefulness too aggressively without bound c
                tageBank[i].entry[ bankGlobalIndex[i] ].usefulness--;
            }
        } else {
            int Y = rand() & ((1 << (primaryBank - 1)) - 1);
            int X = primaryBank - 1;
            while ((Y & 1) != 0) {
                X--;
                Y >>= 1;
                if (X < 0) break;
            }
            for (int i = X; i >= 0; i--) {
                if (tageBank[i].entry[ bankGlobalIndex[i] ].usefulness == minUse) {
                    // Re-init but never resets saturateCounter properly
                    tageBank[i].entry[ bankGlobalIndex[i] ].tag = generateGlobalEnt
                    tageBank[i].entry[ bankGlobalIndex[i] ].saturateCounter =
                        (outcome == TAKEN) ? 2 : -2; // Wrong initial range
                    tageBank[i].entry[ bankGlobalIndex[i] ].usefulness = 0;
                    break;
                }
            }
        }
    }
```

```
    // Directly increment/decrement saturateCounter with no range checks
    if (primaryBank < NUM_BANKS) {
        if (outcome == TAKEN) {
            tageBank[primaryBank].entry[ bankGlobalIndex[primaryBank] ].saturateCou
        } else {
            tageBank[primaryBank].entry[ bankGlobalIndex[primaryBank] ].saturateCou
        }
    } else {
        // update Bimodal (incorrectly { no bounding)
        int idx = pc % BIMODAL_SIZE;
        if (outcome == TAKEN) {
            t_bimodalPredictor[idx]++;
        } else {
            t_bimodalPredictor[idx]--;
        }
    }

    // If primary != alternate, we update the primary's usefulness if we used it
    // (again without bounding, which can go out of range)
    if (lastPrediction != alternatePrediction) {
        if (primaryBank < NUM_BANKS) {
            if (lastPrediction == outcome) {
                tageBank[primaryBank].entry[ bankGlobalIndex[primaryBank] ].usefuln
            } else {
                tageBank[primaryBank].entry[ bankGlobalIndex[primaryBank] ].usefuln
            }
        }
    }

    // Shift in new outcome
    for (int i = MAX_HISTORY_LEN - 1; i > 0; i--) {
        t_globalHistory[i] = t_globalHistory[i - 1];
    }
    t_globalHistory[0] = outcome ? TAKEN : NOTTAKEN;

    // Update path history
    t_pathHistory <<= 1;
    t_pathHistory += (pc & 1);
    t_pathHistory &= ((1 << 16) - 1);

    // Update compressed histories (but missing some checks or re-initializations)
    for (int i = 0; i < NUM_BANKS; i++) {
        t_updateCompressed(&tageBank[i].indexCompressed, t_globalHistory);
        t_updateCompressed(&tageBank[i].tagCompressed[0], t_globalHistory);
        t_updateCompressed(&tageBank[i].tagCompressed[1], t_globalHistory);
    }
}
```

GPT-4o: Below is a rundown of what's causing your **saturating counters** to go out

1. **No Bound Checks** when incrementing or decrementing the saturating counters.
2. **Re-initialization Values** (`+2` or `-2`) that may be inconsistent with the de
3. **Usefulness Counters** also updated without bounding, which can similarly wrap

Let's walk through the details.

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1. Missing Bound Checks in Saturating Counter Updates

Right now, you do:
```c
if (outcome == TAKEN) {
    tageBank[primaryBank].entry[ bankGlobalIndex[primaryBank] ].saturateCounter++;
} else {
    tageBank[primaryBank].entry[ bankGlobalIndex[primaryBank] ].saturateCounter--;
}
```
with no checks. If you keep incrementing, you eventually push `saturateCounter` abc

How to Fix

1. **Decide the width** of your counters. Commonly in TAGE, each tagged entry uses
   - Negative values (4 to 1) => \predict not taken"
   - Zero or positive (0 to +3) => \predict taken"
   - And you saturate at **4** (min) or **+3** (max).

2. **Clamp** on increment/decrement. For example, if using a 3-bit range of `-4..+3
   ```c
   #define MAX_CNT  3   // +3 is the maximum
   #define MIN_CNT -4   // -4 is the minimum

   int8_t *ctr = &tageBank[primaryBank].entry[ bankGlobalIndex[primaryBank] ].satur
   if (outcome == TAKEN) {
       if (*ctr < MAX_CNT) {
           (*ctr)++;
       }
   } else {
       if (*ctr > MIN_CNT) {
           (*ctr)--;
       }
   }
   ```

That way, the counter does not exceed +3 or drop below 4, ensuring proper saturatin

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2. Re-Initializing the Counter to +2 or 2

Inside your \allocate" path, you do:
```c
tageBank[i].entry[ bankGlobalIndex[i] ].saturateCounter =
    (outcome == TAKEN) ? 2 : -2;  // Wrong initial range if 2-bit or mismatch
```
This can be **fine** if your saturating counter range is at least ±2. (In a 3-bit s

How to Fix

- Confirm your desired saturating counter width and sign convention.
- If it's 3 bits (4..+3), re-initializing to ±2 is perfectly valid. Just make sure
- If it's 2 bits (2..+1), then you must clamp '+2' or '-2' to that narrower range.

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3. No Bound Checks for Usefulness Counters

You also have a \usefulness" field:
```c
// This might decrement usefulness too aggressively without bound checks
tageBank[i].entry[ bankGlobalIndex[i] ].usefulness--;
```
and later:
```c
if (lastPrediction == outcome) {
    tageBank[primaryBank].entry[ bankGlobalIndex[primaryBank] ].usefulness++;
} else {
    tageBank[primaryBank].entry[ bankGlobalIndex[primaryBank] ].usefulness--;
}
```
If 'usefulness' is supposed to be a small saturating counter (e.g., 2 bits or 3 bit

How to Fix

- Decide the max/min for 'usefulness' (e.g., 0..3).
- Clamp it in exactly the same way:
  ```c
  #define U_MAX 3
  #define U_MIN 0

  if (tageBank[i].entry[ bankGlobalIndex[i] ].usefulness > U_MIN) {
      tageBank[i].entry[ bankGlobalIndex[i] ].usefulness--;
  }
```

```
  // Similarly for increment.
  ```
```

---

## 4. Bimodal Updates

In your bimodal branch:
```c
if (outcome == TAKEN) {
    t_bimodalPredictor[idx]++;
} else {
    t_bimodalPredictor[idx]--;
}
```
If `t_bimodalPredictor[idx]` is also a saturating counter (commonly 2 bits or 3 bit
```c
if (outcome == TAKEN) {
    if (t_bimodalPredictor[idx] < MAX_BIMODAL) {
        t_bimodalPredictor[idx]++;
    }
} else {
    if (t_bimodalPredictor[idx] > MIN_BIMODAL) {
        t_bimodalPredictor[idx]--;
    }
}
```

Putting It All Together

Key actions to fix the out-of-range saturating counter bug:

1. **Define constants** for the saturating counter bounds.
2. **Clamp** each increment/decrement to those bounds.
3. Ensure your **initial values** (like +2 or 2) fall within the same bounds.
4. Do the same for the **usefulness** counters and bimodal counters (if they're als

Once you add those fixes, you shouldn't see the counters blowing past the valid ran

A.3   Conversation 2: TAGE Predictor Overview

Me: Please provide a high-level explanation of how a TAGE predictor works, focusing

GPT-4o: Sure! Here's a high-level explanation of how a **TAGE (TAgged GEometric his

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Overview of TAGE

TAGE is a **state-of-the-art branch predictor** used in modern CPUs to guess the di

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Multi-bank Structure

- TAGE uses **multiple predictor components**, often called **banks or tables**.
- Each table (except for the base one) is associated with a **different history len
- The predictor uses **one base predictor** (often a simple bimodal predictor) and
- Each tagged table is indexed using a **compressed version** of the global branch

Key idea: If a long history length yields a confident prediction, use it. Other

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Geometric History Lengths

- Each tagged table uses a **different history length**, forming a **geometric prog
  ```
  L(i) = floor(ˆi), for i = 0 to N-1
  ```
  where:
  - `L(i)` is the history length for table `i`
  - `` is a geometric growth factor (e.g., 1.5 to 2)
  - `N` is the number of tagged tables
- This setup allows TAGE to cover a wide range of history lengths with **fewer tabl

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Partial Tag Generation

- Each entry in a tagged table stores a **partial tag** to match against the branch
- A **partial tag** is generated by:
  - **Hashing or folding** the program counter (PC) and the global history into a s
  - This allows a small tag to identify whether a prediction entry corresponds to t
- Partial tags help **differentiate between branches** that may map to the same tab

---

Prediction Process

1. For a given branch:
   - The PC and global history are used to index all tables.
   - The predictor searches for the **longest history match** among the tables.

2. If a match is found (tag matches), the prediction from that table is used.
3. If no match, the base predictor is used.
4. If two or more matches exist, the **longest matching history** wins.

Summary

- **Multi-bank structure**: Multiple tables store predictions with varying history
- **Geometric history lengths**: History lengths grow exponentially to capture both
- **Partial tags**: Small hash-like signatures identify valid entries for a given F

Let me know if you want a diagram or a more detailed example to go with this!

A.4   Conversation 3: TAGE predictor bit calculation

Me: I'm trying to keep my TAGE predictor under 64K + 256 bits. How do I calculate t

GPT-4o: Great question! Let's break this down and calculate the storage used per en

---

Per-Entry Bit Usage (per bank)

For **each TAGE predictor bank entry**, you typically store:

1. **Tag** = 10 bits
2. **Saturating Counter** = 3 bits
3. **Usefulness Counter** = 2 or 3 bits (depends on your design)

So per entry:
- If 2-bit usefulness: `10 + 3 + 2 = 15 bits`
- If 3-bit usefulness: `10 + 3 + 3 = 16 bits`

Compressed Histories

Compressed histories are used to save storage on the history-based indexing and

- You typically store a **compressed history** for each bank, used in indexing and
  - The global history length used
  - Number of banks
  - The folding strategy

In many designs, each compressed history is ˜10{16 bits per component (depending on
- One for index generation (per bank)
- One for tag generation (per bank)

So rough estimate:
`~2 compressed histories × N banks × ~16 bits = small amount`
Say for 8 banks: `2 × 8 × 16 = 256 bits` | which actually matches the **+256** in y

 Conclusion: You're allowed to spend **64K bits (65,024 bits)** on your *tables

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Storage Budget Summary

You have:
- **64K bits = 65,024 bits for TAGE entries**
- **+256 bits for compressed histories**

Let's calculate how many entries you can have per bank.

Example: How Many Entries per Bank?

Let's say:
- 4 banks
- Usefulness counter = 2 bits
- So each entry = 15 bits

Assuming equal size per bank:
```
Total bits per bank = 65,024 / 4 = 16,256 bits
Entries per bank = 16,256 / 15  1,083 entries
```

If usefulness = 3 bits (16 bits per entry):
```
Entries per bank = 16,256 / 16 = 1,016 entries
```

You can also vary the number of entries per bank (fewer entries for longer-history

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Other Considerations:

- **Base Predictor**: Don't forget that TAGE usually includes a base predictor (lik
- **Banked vs Fully Associative**: If you implement associativity or partial associ
- **Replacement Information**: If you store any replacement priority bits, you'll r

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```
### TL;DR:

- **Per-entry size = tag (10) + ctr (3) + useful (2{3) = 15{16 bits**
- **Compressed histories  256 bits total | fits within the \+256 bits" budget**
- Use your total bit budget (65,024) to divide across banks and determine entry cou
```

Let me know how many banks you're using or if you want help optimizing your layout!

A.5   Conversation 4: TAGE Training Function Annotation

Me:

Could you annotate the tage_train() function?

```c
static inline void tage_train(uint32_t pc, uint8_t outcome) {
    int needAllocate = 0;
    if (primaryBank < NUM_BANKS) {
        int8_t pCtr = tageBank[primaryBank].entry[ bankGlobalIndex[primaryBank] ].s
        // If mispredicted and the sign of pCtr is opposite the actual outcome => n
        if ((lastPrediction != outcome) && ((pCtr >= 0) != outcome)) {
            needAllocate = 1;
        }
    } else {
        needAllocate = (lastPrediction != outcome);
    }

    if (needAllocate) {
        int8_t minUse = 127;
        for (int i = 0; i < primaryBank; i++) {
            int8_t u = tageBank[i].entry[ bankGlobalIndex[i] ].usefulness;
            if (u < minUse) {
                minUse = u;
            }
        }
        if (minUse > 0) {
            for (int i = primaryBank - 1; i >= 0; i--) {
                tageBank[i].entry[ bankGlobalIndex[i] ].usefulness--;
            }
        } else {
            int Y = rand() & ((1 << (primaryBank - 1)) - 1);
            int X = primaryBank - 1;
            while ((Y & 1) != 0) {
                X--;
                Y >>= 1;
                if (X < 0) break;
            }
            for (int i = X; i >= 0; i--) {
```

```
            if (tageBank[i].entry[ bankGlobalIndex[i] ].usefulness == minUse) {
                // Re-init
                tageBank[i].entry[ bankGlobalIndex[i] ].tag = generateGlobalEnt
                tageBank[i].entry[ bankGlobalIndex[i] ].saturateCounter =
                    (outcome == TAKEN) ? 0 : -1;
                tageBank[i].entry[ bankGlobalIndex[i] ].usefulness = 0;
                break;
            }
        }
    }
}

// Update the saturating counter
if (primaryBank < NUM_BANKS) {
    updateSaturate(
        &tageBank[primaryBank].entry[ bankGlobalIndex[primaryBank] ].saturateCo
        outcome,
        LEN_COUNTS
    );
} else {
    // update Bimodal
    int idx = pc % BIMODAL_SIZE;
    updateSaturateMinMax(&t_bimodalPredictor[idx], outcome, 0, (1 << LEN_BIMODA
}

// If primary != alternate, we update the primary's usefulness if we used it
if (lastPrediction != alternatePrediction) {
    if (primaryBank < NUM_BANKS) {
        updateSaturateMinMax(
            &tageBank[primaryBank].entry[ bankGlobalIndex[primaryBank] ].useful
            (lastPrediction == outcome),
            0, 3
        );
    }
}

// Shift in new outcome
for (int i = MAX_HISTORY_LEN - 1; i > 0; i--) {
    t_globalHistory[i] = t_globalHistory[i - 1];
}
t_globalHistory[0] = outcome ? TAKEN : NOTTAKEN;

// Update path history
t_pathHistory <<= 1;
t_pathHistory += (pc & 1);
t_pathHistory &= ((1 << 16) - 1);

// Update compressed histories
```

```cpp
    for (int i = 0; i < NUM_BANKS; i++) {
        t_updateCompressed(&tageBank[i].indexCompressed, t_globalHistory);
        t_updateCompressed(&tageBank[i].tagCompressed[0], t_globalHistory);
        t_updateCompressed(&tageBank[i].tagCompressed[1], t_globalHistory);
    }
}
```

GPT-4o: Below is an annotated version of the `tage_train()` function. The annotatio

---

```cpp
static inline void tage_train(uint32_t pc, uint8_t outcome) {
    // 1. Determine whether we need to allocate a new entry in the TAGE tables (i.e.
    //     the prediction was mispredicted and we have reason to believe a new entry
    //     improve future prediction accuracy).

    int needAllocate = 0;

    // primaryBank is the TAGE bank (or set of banks) that provided the final predi
    // If primaryBank is valid (less than NUM_BANKS), we have a prediction from TAG
    // Otherwise, the prediction came from the bimodal predictor.
    if (primaryBank < NUM_BANKS) {
        // pCtr is the saturating counter from the TAGE table entry in the primary
        int8_t pCtr = tageBank[primaryBank].entry[ bankGlobalIndex[primaryBank] ].s

        // If the final prediction was wrong AND the sign of pCtr is opposite from
        // we may want to allocate a new entry from the other TAGE banks (which did
        // This is a typical "allocate on misprediction" strategy for TAGE.
        if ((lastPrediction != outcome) && ((pCtr >= 0) != outcome)) {
            needAllocate = 1;
        }
    } else {
        // If the prediction was from the bimodal predictor, we consider allocating
        // if the prediction was simply incorrect.
        needAllocate = (lastPrediction != outcome);
    }

    // 2. If we need to allocate, determine whether it is possible or desirable to
    //     TAGE banks use a "usefulness" counter to decide if an entry is worth repl

    if (needAllocate) {
        int8_t minUse = 127;

        // Search for the minimum "usefulness" across all banks that are more selec
        // The lower this value, the more likely it is that an entry can be replace
        for (int i = 0; i < primaryBank; i++) {
            int8_t u = tageBank[i].entry[ bankGlobalIndex[i] ].usefulness;
```

```
        if (u < minUse) {
            minUse = u;
        }
    }

    // If all banks have high usefulness, we decrement the usefulness counters
    // for entries to become less useful and thus replaceable in the future).
    if (minUse > 0) {
        for (int i = primaryBank - 1; i >= 0; i--) {
            tageBank[i].entry[ bankGlobalIndex[i] ].usefulness--;
        }
    } else {
        // Otherwise, at least one bank has minimal usefulness, and we can repl
        // those banks with a new tag/saturating counter.

        // Y is used here to randomly select which bank (among the possible one
        // The expression "(1 << (primaryBank - 1)) - 1" essentially creates a
        // For example, if primaryBank = 3, we get (1 << 2) - 1 = 3 (binary 11)
        int Y = rand() & ((1 << (primaryBank - 1)) - 1);
        int X = primaryBank - 1;

        // This loop steps backward through the banks (less selective to more s
        // finds one that is randomly selected to allocate.
        while ((Y & 1) != 0) {
            X--;
            Y >>= 1;
            if (X < 0) break;
        }

        // Once we choose bank X, look for an entry in that bank with usefulnes
        // We then re-initialize it with the new tag, a saturating counter bias
        // and reset usefulness.
        for (int i = X; i >= 0; i--) {
            if (tageBank[i].entry[ bankGlobalIndex[i] ].usefulness == minUse) {
                // Re-initialize the entry with the new tag and starting counte
                tageBank[i].entry[ bankGlobalIndex[i] ].tag = generateGlobalEnt
                tageBank[i].entry[ bankGlobalIndex[i] ].saturateCounter =
                    (outcome == TAKEN) ? 0 : -1;
                tageBank[i].entry[ bankGlobalIndex[i] ].usefulness = 0;
                break;
            }
        }
    }
}

// 3. Update the saturating counter in the primary bank (if used), or the bimod
//    Saturating counters move up/down based on whether the outcome was TAKEN o
if (primaryBank < NUM_BANKS) {
```

```
        updateSaturate(
            &tageBank[primaryBank].entry[ bankGlobalIndex[primaryBank] ].saturateCo
            outcome,
            LEN_COUNTS
        );
    } else {
        // If the prediction came from the bimodal predictor, update it instead.
        int idx = pc % BIMODAL_SIZE;
        updateSaturateMinMax(&t_bimodalPredictor[idx], outcome, 0, (1 << LEN_BIMODA
    }

    // 4. If the primary prediction was different from the alternate prediction,
    //    update the usefulness counter for the primary table's entry. We reward or
    //    the primary TAGE entry if it got the actual outcome right or wrong, respe
    if (lastPrediction != alternatePrediction) {
        if (primaryBank < NUM_BANKS) {
            updateSaturateMinMax(
                &tageBank[primaryBank].entry[ bankGlobalIndex[primaryBank] ].useful
                (lastPrediction == outcome),
                0, 3
            );
        }
    }

    // 5. Update the global history with the new outcome. This shifts the array t_g
    //    and inserts the latest taken/not-taken result at the front (index 0).
    for (int i = MAX_HISTORY_LEN - 1; i > 0; i--) {
        t_globalHistory[i] = t_globalHistory[i - 1];
    }
    t_globalHistory[0] = outcome ? TAKEN : NOTTAKEN;

    // Update the path history (which often tracks the program-counter's least sign
    t_pathHistory <<= 1;
    t_pathHistory += (pc & 1);
    t_pathHistory &= ((1 << 16) - 1); // keep only the lower 16 bits

    // 6. Update the compressed histories for each TAGE bank. Compressed history is
    //    and tag TAGE tables with partial, hashed versions of the global history.
    for (int i = 0; i < NUM_BANKS; i++) {
        t_updateCompressed(&tageBank[i].indexCompressed, t_globalHistory);
        t_updateCompressed(&tageBank[i].tagCompressed[0], t_globalHistory);
        t_updateCompressed(&tageBank[i].tagCompressed[1], t_globalHistory);
    }
}
```

Summary of Key Points

1. **`needAllocate`:** Determines if the predictor will attempt to allocate a new e

2. **Usefulness Counters:** TAGE uses \usefulness" to determine if an entry is like

3. **Random Replacement Among Candidates:** If multiple entries are at minimum usef

4. **Updating Saturating Counters:** After each prediction, the saturating counter

5. **Usefulness Update:** If the primary TAGE bank disagreed with the alternate but

6. **Updating History:** Global history (`t_globalHistory`), path history (`t_pathH

A.6 Conversation 5: Docker setup for predictor

Me: Show me how to set up a Docker container to compile and run `predictor.c` with

GPT-4o: Sure! Let's walk through setting up a Docker container that compiles and ru

---

Step 1: Project Layout (Assumed)

Suppose your project folder looks like this on your **Windows host**:

```
C:\Users\YourName\branch_predictor\

 predictor.c
 Makefile
 sim
 trace\
    trace1.bz2
    trace2.bz2
```

We'll mount this directory into Docker.

Step 2: Create a Dockerfile (optional)

If you want a custom environment, create a `Dockerfile` like this:

```Dockerfile
FROM ubuntu:22.04

# Install build tools and bunzip2
RUN apt update && apt install -y build-essential bzip2
```

```
WORKDIR /app
```

Build it with:

```bash
docker build -t predictor-env .
```

Alternatively, you can skip this and use a base image like `gcc` with bzip2.

Step 3: Run Docker with Proper Mounts

On **Windows**, your path `/mnt/c/Users/YourName/branch_predictor` corresponds to

Here's the Docker run command:

```bash
docker run --rm -it -v /mnt/c/Users/YourName/branch_predictor:/app -w /app predicto
```

Or, if you didn't build a custom image:

```bash
docker run --rm -it -v /mnt/c/Users/YourName/branch_predictor:/app -w /app ubuntu:2
```

Then install the tools inside the container:

```bash
apt update
apt install -y build-essential bzip2
```

Step 4: Compile with Make

Inside the container (you're now at `/app`, which is your Windows project dir):

```bash
make
```

This should compile `predictor.c` into the binary `sim`.

Step 5: Run Sim with `.bz2` Trace Files

Assuming `sim` takes a trace file as argument like this:

```bash
./sim -t trace/trace1.bz2
```

You can run any of the traces like:

```bash
./sim -t trace/trace1.bz2
./sim -t trace/trace2.bz2
```

If you want to loop over them:

```bash
for f in trace/*.bz2; do
  ./sim -t "$f"
done
```

Full Session Recap (All Together)

```bash
docker run --rm -it -v /mnt/c/Users/YourName/branch_predictor:/app -w /app ubuntu:2

# In Docker:
apt update
apt install -y build-essential bzip2
make
./sim -t trace/trace1.bz2
```

Would you like help writing a `Makefile`, if you don't already have one? Or a scrip

A.7 Conversation 2: Gshare Misprediction Rate Difference

Me: Can you explain why the runall.sh script outputs "Misprediction Rate: 0.826" fo

GPT-4o: The slight difference in **Misprediction Rate** between `gshare:14` (0.826)

Let me break it down for you:

What is gshare?

gshare is a dynamic branch predictor that uses:

- **Global History Register (GHR)**: tracks outcomes of recent branches.
- **Program Counter (PC)**: identifies the current branch.
- These two are XOR'ed together to generate an **index** into a **prediction table**

What does `gshare:14` or `gshare:15` mean?

These likely refer to the number of **index bits** used to access the prediction ta
- `gshare:14` → 14 bits are used to index the table.
- `gshare:15` → 15 bits are used.

This affects:
- **Table size** (2^1 vs. 2^1 entries).
- **Indexing behavior**, because more bits from the PC and GHR are used in the XOR.

Why the slight difference?

1. **Structural behavior:**
   - A larger table (`gshare:15`) generally helps | more entries, less aliasing.
   - But it can also cause **different aliasing patterns**: more bits from the GHR
   - This can cause **some branches to benefit** and others to suffer, especially o

2. **Trace sensitivity:**
   - The `fp_1` trace might have branch patterns that align better with 14 bits tha

3. **Rounding error?**
   - If the misprediction rate is output as a **rounded float**, e.g. 0.826 vs. 0.8
     - `0.8264` (rounded to 0.826)
     - `0.8265` (rounded to 0.827)

Is randomness involved?

Unlikely unless:

- The simulator is non-deterministic (e.g., uses random initial table values or thr
- You're using randomized inputs or seeds (e.g., in a neural predictor or ML-based

If you're using a standard gshare implementation and always run the same trace (`fp

---

Summary:

The difference in misprediction rate between `gshare:14` and `gshare:15` is due to

If you want, I can show you how to visualize the indexing to see exactly which bits