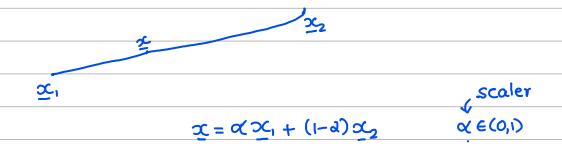


$$\underline{x} \in \mathbb{R}^n$$

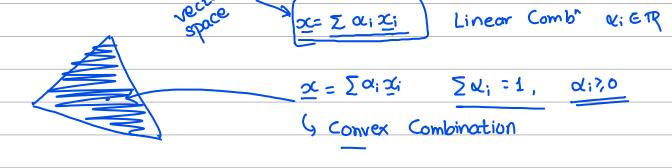


 $\dot{x}_{2}$ 

line segment 
$$\{x/x=\alpha x_1+(-\alpha)x_2, \alpha \in (0,1)\}$$
  
joining  $x_1,x_2 \in \mathbb{R}^{n}$ 

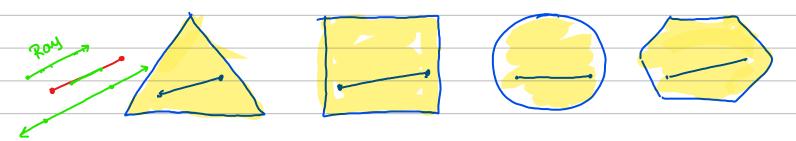
# Line passing 
$$\underline{x}, \underline{x}_2 \in \mathbb{R}^n$$
line segment  $\leftarrow convex comb$   $\underline{x} = \alpha \underline{x}_1 + (1-\alpha) \underline{x}_2 \quad \alpha \in (0,1)$ 

$$\underline{x} = \alpha \underline{x}_1 + (1-\alpha) \underline{x}_2 \quad \alpha \in (0,1)$$
line 1
linear comb

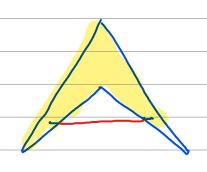


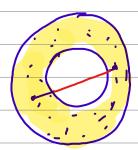
$$\left\{ \frac{\alpha}{\alpha} \middle| \frac{\alpha}{\alpha} = \sum_{i=1}^{n} \alpha_i \alpha_i, \alpha_{i,30}, \Sigma \alpha_{i-1} \right\}$$

Convex set if  $\chi x_1 \in A$ ,  $x = ux_1 + (1-u)x_2$   $y \propto e(0,1)$ then if  $x \in S$   $y \in A$  is convex set



Convex Sets





Non convex sets

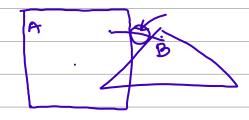
\* Ray is convex set  $\underline{x} = \underline{x}_0 + \underline{d} \cdot \underline{\alpha} \quad \alpha > 0$   $\underline{x}_1 \cdot \underline{\xi} \cdot \underline{x}_2 \in A$ 

$$\frac{\chi}{1-\lambda} = \frac{\chi_0 + d\alpha_1}{\chi_2 = \chi_0 + d\alpha_2}$$

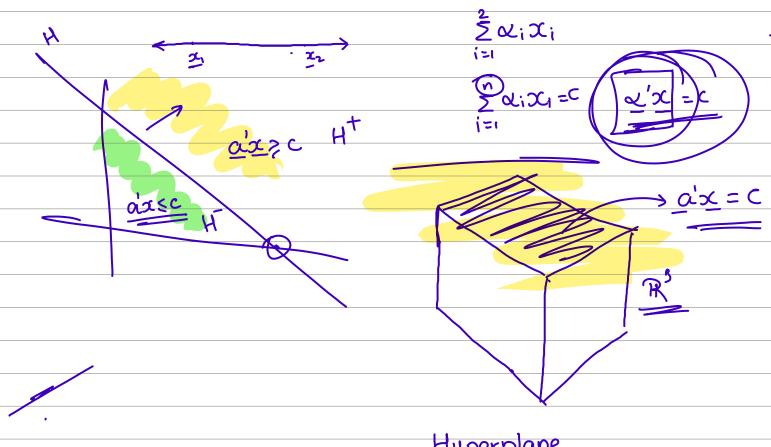
$$\frac{\lambda x_1 + (1-\lambda) x_2}{= x_0 + d( )} = x_0 + d( \lambda x_1 + (1-\lambda) x_2 )$$

$$= x_0 + d( ) \geq 0$$

$$\in A$$



- \* Union of convex sets may or may not be convex.
- \* Intersection of convex sets is also convex.



Hyperplane

H'=  $\{x \mid a'x > c\}$  half space

H= $\{x \mid a'x > c\}$  half space

H= $\{x \mid a'x = c\}$  Hyperplane

H= $\{x \mid a'x = c\}$  Hyperplane

H= $\{x \mid a'x = c\}$  Negative closed half space

 $H_0 = \left(\frac{\pi}{2} / a^{\frac{\pi}{2}} < c\right)$  -ve open half space

Hyperplane 
$$H = \{ \frac{x}{a} | \frac{a}{a} = c \}$$

$$\frac{\alpha x_1 + (1-\alpha)x_2}{\alpha'(\alpha x_1 + (1-\alpha)x_2)} = \alpha \alpha' x_1 + (1-\alpha)\alpha' x_2$$

$$= \alpha c + (1-\alpha)c$$

$$= c$$

 $\Rightarrow \alpha x + (r-d) x_2 \in H$ 

=) Hyperplane is convex set

Ht, HT, Ht, HT all are convex sets

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