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Part A: Hash Table Definitions (Conceptual Understanding)

Q1. Define "collision" in the context of hash tables.

A1: 如果key指向同一個index會發生碰撞

Q2. What is a "bucket" in a hash table?

A2: 儲存資料的地方

Q3. Define "load factor (α)" and explain why it affects performance.

A3: n/m , n 是有幾個key被儲存 m 是index有幾個
 n 與 m 越接近越容易碰撞

Q4. What is "primary clustering," and which probing method suffers from it?

A4: 會聚集, linear probing $(h(k) + i) \bmod 10$

Q5. What is "secondary clustering," and how is it different from primary clustering?

A5: 會因為key指向同一個index, 間隔越跳越遠
主要發生在 $(h(k) + c_1i + c_2i^2) \bmod 10$

Q6. Briefly explain the difference between:

- Open addressing
- Separate chaining

A6: open addressing: array, 儲存資料只有固定空間

separate chaining: linked list, 可以一直銜接

Part B: Hash Function Calculation (Collision & Pattern Observation)

Show your steps clearly.

Hash Function 1 — Division Method

$$h_1(k) = k \bmod 10$$

Hash Function 2 — Folding Method

Split key into two-digit chunks and sum the chunks.

$$h_2(k) = (\text{sum of 2-digit groups}) \bmod 11$$

Example:

Key = 8429 \rightarrow groups: 84 + 29 \rightarrow 113 \rightarrow 113 mod 11 = 3

Q7. (Compute using Hash Function 1)

Given keys: 27, 37, 47, 57, 67

Compute their hash values using:

A7: $27 \Rightarrow 27 \bmod 10 \Rightarrow 7$
 $37 \Rightarrow 37 \bmod 10 \Rightarrow 7$
 $47 \Rightarrow 47 \bmod 10 \Rightarrow 7$
 $57 \Rightarrow 57 \bmod 10 \Rightarrow 7$
 $67 \Rightarrow 67 \bmod 10 \Rightarrow 7$

$h_1(k) = k \bmod 10$

Q8. (Identify collision pattern)

From your results in Q7:

- What pattern do you observe?
- Explain why these keys collide.

A8: 全部 index 都是 7 因為個尾數是 7 且是除以 10 的餘數

Q9. (Compute using Hash Function 2)

Compute $h_2(k)$ for: 1234, 9217, 4519, 9902

A9: $1234 \Rightarrow 12 + 34 \Rightarrow 46 \bmod 11 \Rightarrow 2$
 $9217 \Rightarrow 92 + 17 \Rightarrow 109 \bmod 11 \Rightarrow 10$
 $4519 \Rightarrow 45 + 19 \Rightarrow 64 \bmod 11 \Rightarrow 9$
 $9902 \Rightarrow 99 + 2 \Rightarrow 101 \bmod 11 \Rightarrow 2$

Q10. (Compare distribution)

- Which hash function (h_1 or h_2) produced more collisions for the input set?
- Which seems to spread keys more evenly?
- Provide 1–2 sentences of explanation.

A10: h_1 碰撞較多, h_2 把 key 分比較開較隨機

因為 $h_1 \bmod$ 的數是 10, 所以碰到個位數相同時, 會發生碰撞, $h_2 \bmod$ 的數是 11 是整數而且先對 key 做處理