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## Part A: Hash Table Definitions (Conceptual Understanding)

Q1. Define "collision" in the context of hash tables.

A1: ~~如果 key 指向同一個 index 會發生碰撞~~

Q2. What is a "bucket" in a hash table?

A2: ~~儲存資料的地方~~Q3. Define "load factor ( $\alpha$ )" and explain why it affects performance.A3:  ~~$n/m$ ,  $n$ 是有幾個key被儲存  $m$ 是index有幾個  
人突m越接近越容易碰撞~~

Q4. What is "primary clustering," and which probing method suffers from it?

A4: ~~會聚集, linear probing  $(h(k) + i) \bmod 10$~~ 

Q5. What is "secondary clustering," and how is it different from primary clustering?

A5: ~~會因為 key 指向同一個 index, 間隔越跳越遠  
主要發生在  $(h(k) + ci + ci^2) \bmod 10$~~ 

Q6. Briefly explain the difference between:

- Open addressing
- Separate chaining

A6: ~~open addressing: array, 儲存資料只有固定空間~~~~separate chaining: linked list, 可以一直链接~~

## Part B: Hash Function Calculation (Collision & Pattern Observation)

Show your steps clearly.

Hash Function 1 — Division Method

$$h_1(k) = k \bmod 10$$

Hash Function 2 — Folding Method

Split key into two-digit chunks and sum the chunks.

$$h_2(k) = (\text{sum of 2-digit groups}) \bmod 11$$

Example:

Key = 8429  $\rightarrow$  groups: 84 + 29  $\rightarrow$  113  $\rightarrow$  113 mod 11 = 3

Q7. (Compute using Hash Function 1)

Given keys: 27, 37, 47, 57, 67

Compute their hash values using:

A7:  $27 \Rightarrow 27 \% 10 \Rightarrow 7$   
 $37 \Rightarrow 37 \% 10 \Rightarrow 7$   
 $47 \Rightarrow 47 \% 10 \Rightarrow 7$

$$h_1(k) = k \bmod 10$$

$$57 \Rightarrow 57 \% 10 \Rightarrow 7$$
  
 $67 \Rightarrow 67 \% 10 \Rightarrow 7$

Q8. (Identify collision pattern)

From your results in Q7:

- What pattern do you observe?
- Explain why these keys collide.

A8: 全部 index 都是 7 因為個尾數是 7 且是除以 10 的餘數

Q9. (Compute using Hash Function 2)

Compute  $h_2(k)$  for: 1234, 9217, 4519, 9902

A9:  $1234 \Rightarrow 12 + 34 \Rightarrow 46 \% 11 \Rightarrow 2$   
 $9217 \Rightarrow 92 + 17 \Rightarrow 109 \% 11 \Rightarrow 10$   
 $4519 \Rightarrow 45 + 19 \Rightarrow 64 \% 11 \Rightarrow 9$   
 $9902 \Rightarrow 99 + 2 \Rightarrow 101 \% 11 \Rightarrow 2$

Q10. (Compare distribution)

- Which hash function ( $h_1$  or  $h_2$ ) produced more collisions for the input set?
- Which seems to spread keys more evenly?
- Provide 1-2 sentences of explanation.

A10:  $h_1$  碰撞較多,  $h_2$  把 key 分比較開較隨機

因為  $h_1$  mod 的數是 10, 所以碰到個位數相同時, 會發生碰撞,  $h_2$  mod 的數是 11 是質數而且有先對 key 做處理