$$P(R|A) = 0.99$$

$$P(A|R) = \frac{P(A) \cdot P(R|A)}{P(R)}$$

Moreover, using the Rule of Total Probability,
$$P(R) = P(R|A) \cdot P(A) + P(R|not A) \cdot P(not A).$$

$$= 0.99 \cdot 0.05 + 0.1 \cdot 0.95$$

$$9.000 \times 0.99$$

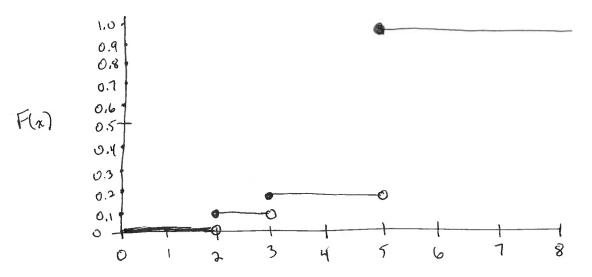
$$0.99 \times 0.05 + 0.1 \times 0.95$$

(This expression is enough, but the number turns out to be
$$P(A|R) \cong 0.343$$
)

2 X has PMF
$$f(x) =$$

$$\begin{cases}
1/10 & \text{if } x = 2 \\
1/10 & \text{if } x = 3 \\
8/10 & \text{if } x = 5
\end{cases}$$

The CDF looks like the following picture



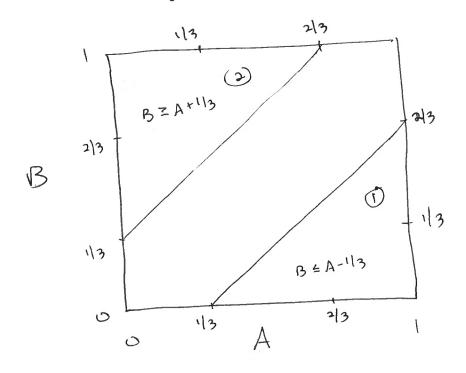
$$P(24 \times 44.5) = P(\{x: x \in (2,4.5]\})$$

$$= P(X=3), \text{ Since } x=3 \text{ is the only possible value of } x \text{ that fully in } (2,4.5].$$

$$= 1/10$$

$$P(2 \le X \le 4.5) = P(X = 2) + P(X = 3)$$

= $\frac{1}{10} + \frac{1}{10} = \frac{2}{10}$



Alice and Bob will miss each other if $|A-B| \ge 1/3$, since each will wait for a maximum of 1/3 of an Lour. And:

$$P(|A-B| \ge |I_3|) = P(A-B \ge |I_3|) + P(A-B \le -|I_3|)$$

$$= P(B \le A - |I_3|) + P(B \ge A + |I_3|)$$

$$= Area of triangle | + Area of triangle | 2$$

$$= \frac{2}{3} \cdot \frac{2}{3} \cdot \frac{1}{2} + \frac{2}{3} \cdot \frac{2}{3} \cdot \frac{1}{2}$$

$$= \frac{4}{3}$$

So p(meet) = 1 - 4/9 = 5/9

(4) Markov's argument is wrong; we can't calculate
$$E(T) = E(\frac{2}{7}) = \frac{2}{E(V)}$$

In general, E(f(x)) + f(E(x1)

Instead, to calculate E(T), note that there are two possibilities:

-If he walks, $T = \frac{2 \text{ miles}}{5 \text{ miles/hour}} = \frac{2}{5} \text{ hour}$

-If he rides, $T = \frac{2 \text{ miles}}{10 \text{ miles hour}} = \frac{2}{10} \text{ hour}$

Therefore, E(T) = 0.4 × = + 0.6 × = 10

This expression is enough, but the final value turns out to be $\frac{4}{10}$, $\frac{4}{10}$ + $\frac{6}{10}$ x $\frac{2}{10}$ = $\frac{16}{100}$ + $\frac{12}{100}$

= 28 hours

= 16.8 minutes

(no+ 15)

5) Part B
$$Y_{n} = \max \{X_{1}, ..., X_{N}\}$$
To find the PDF fly), first find the CDF.
$$F(y) = P(Y_{n} \leq y) = P(\max \{X_{1}, ..., X_{N}\} \leq y)$$

But
$$\max\{X_1,...,X_N\} \leq y \iff X_i \leq y$$
 for all $i=1,...,N$ (hint)

50
$$P(Y_n = y) = P(X_1 \leq y, X_2 \leq y, ..., X_n \leq y)$$

$$= \frac{N}{\prod} P(X_1 \leq y) \quad \text{By independence.}$$

$$= \frac{N}{[1 - e^{-\lambda y}]} \quad \text{By the given integral.}$$

$$= \frac{N}{[1 - e^{-\lambda y}]} \quad \text{By the given integral.}$$

Therefore
$$f(y) = F'(y) = N[1-e^{-\lambda y}]^{N-1} \lambda e^{-\lambda y}$$

This is the important thing to recognize

It didn't metter whether you remembered how to take this derivative by hard.