Development 8 - Exercises Unit 4

Exercise 1:

Implement a function

```
let filter = <a>(predicate: (x: a) => boolean) => (1: List<a>): List<a>
```

that inserts in the output list only the elements for which predicate returns true

Exercise 2:

Implement a function

```
let map = \langle a, b \rangle (f: (x: a) \Rightarrow b) \Rightarrow (1: List \langle a \rangle): List \langle b \rangle
```

that applies the function f to all the elements of 1 and returns a list containing the results.

Exercise 3:

Implement a function

```
let fold = \langle s, a \rangle(f: (state: s) => (x: a) => s) => (init: s) => (l: List\langle a \rangle): s
```

that applies a function ${\tt f}$ to elements in the same position from 1, threading an accumulator argument of type ${\tt s}$ through the computation.

Exercise 4:

Implement a function

```
let apply = \langle a, b \rangle (f: (x: a) \Rightarrow b) \Rightarrow (x: a): b
```

that applies function 'f' to element 'x'.

Exercise 5:

Implement a function

```
let curry = \langle a, b, c \rangle (f: Tuple\langle a, b \rangle \Rightarrow c) \Rightarrow (x: a) \Rightarrow (y: b): c
```

that applies function 'f' using as input elements 'x' and 'y' stored as a tuple.

Exercise 6:

Implement a function

```
let mapFold = \langle a, b \rangle (f: (x: a) \Rightarrow b) \Rightarrow (1: List \langle a \rangle): List \langle b \rangle
```

that implements map only using fold

Exercise 7:

Implement a function

```
let filterFold = <a>(predicate: (x: a) => boolean) => (1: List<a>): List<a>
```

that implements filter only using fold

Exercise 8:

Implement a function

```
let flatten = <a>(1: List<List<a>>): List<a>
```

that takes a list of lists and places all their elements it into a single one. Use fold to implement this function.

Exercise 9:

Implement a function

```
let map2 = \langle a, b, c \rangle (f: (x: a) = \rangle (y: b) = \rangle c) = \rangle (11: List \langle a \rangle) = \rangle (12: List \langle b \rangle): List \langle c \rangle
```

that applies the function f to the elements in the same position of two lists of equal length 11 and 12.

Exercise 10:

Implement a function

```
let fold2 = \langle s, a, b \rangle(f: (state: s) => (x: a) => (y: b) => s) => (init: s) => (11: List\langle a \rangle) => (12: List\langle b \rangle): s
```

that applies a function f to elements in the same position from 11 and 12, threading an accumulator argument of type s through the computation.

Exercise 11:

Implement a function

```
let zip = <a, b>(11: List<a>) => (12: List<b>): List<Tuple<a, b>>
```

that take two lists with the same length and creates a list of pairs containing the elements that are in the same position from both lists. Implement this function by using normal recursion and then by using fold2

Exercise 12:

Implement a function

```
let map2Safe = <a, b, c>(f: (x: a) \Rightarrow (y: b) \Rightarrow c) \Rightarrow (11: List<a>) \Rightarrow (12: List<b>): List<0ption<c>>
```

that applies the function f to the elements in the same position of two lists11 and 12, possibly with different length. If an element of one list does not have a correspondent element in the second list, then the function returns None.

Example: Summing the elements of [1, 2, 3, 4] and [4, 5] with map2Safe returns [Some(5), Some(7), None, None]