
FACE RECOGNITION

Min Fang



CONTENT

01

Introduction

02

Objective

03

Method Selection

04

Experiment

05

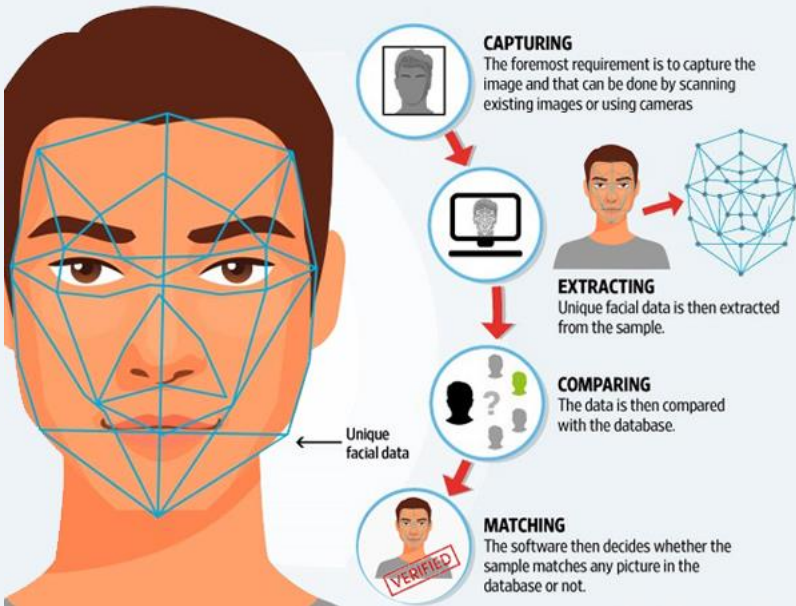
Conclusion

06

Reference

Face Recognition

significant attention because of its numerous applications



Access control

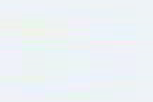
Surveillance

Security

Law enforcement

Internet communication

Computer entertainment

Illumination

Challenge

Variation

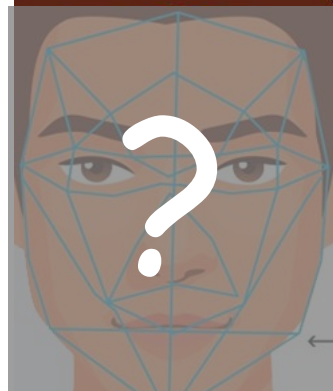
Occlusion

Pose

Expression

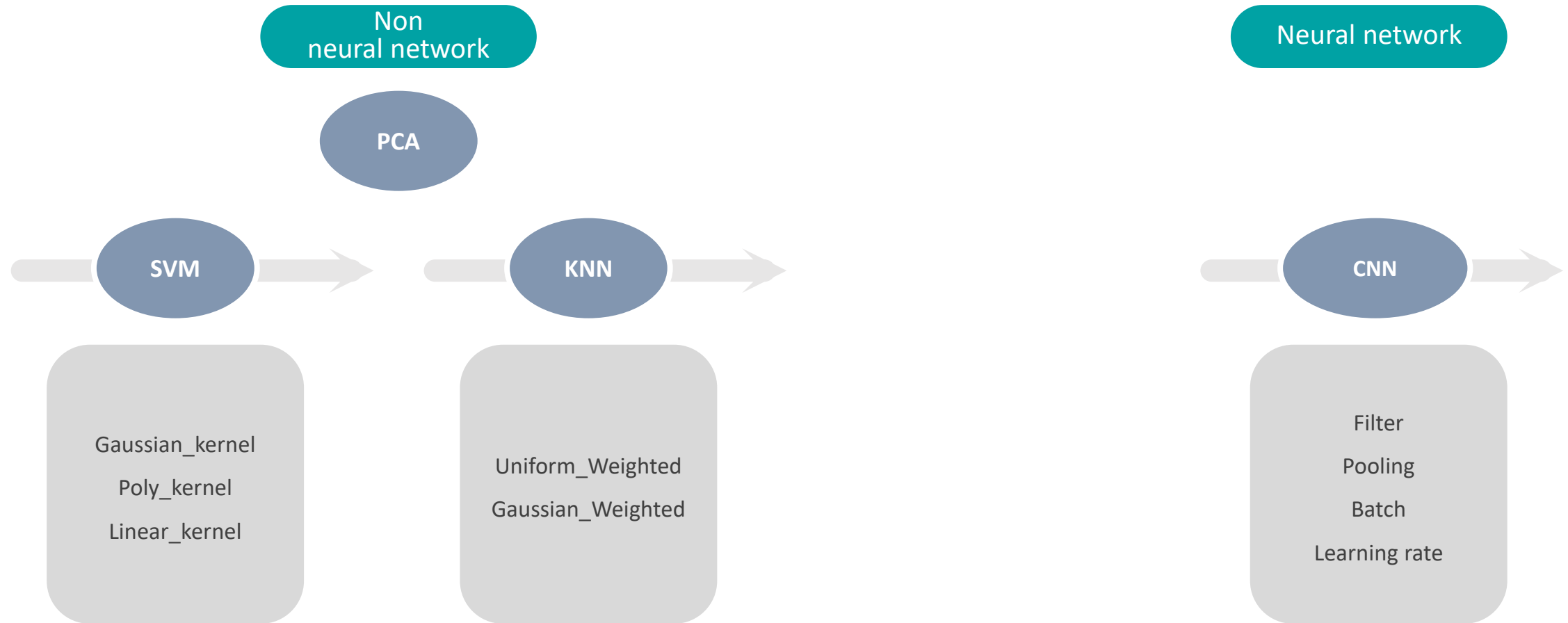
How precisely classify face under Illumination variation?

Illumination



Pose

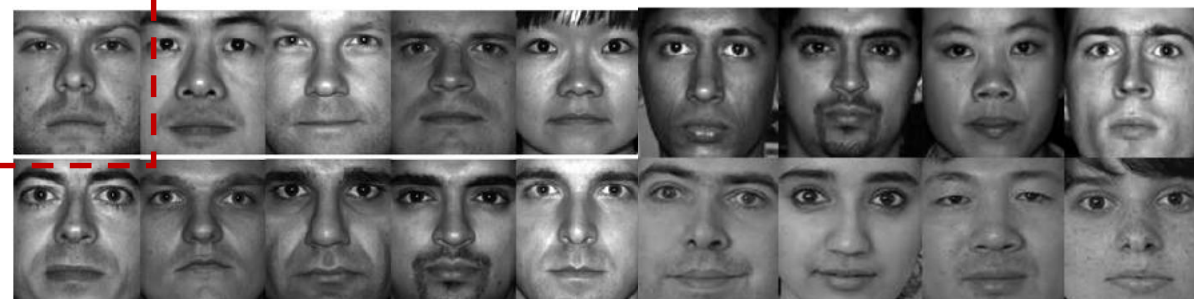
How precisely classify face under Pose variation?





192 × 168 pixels

contains 2414 images
38 different people
under
1 pose
64 illuminations



Cropped version of the Yale Face Database B

UCSD. Vision

<http://vision.ucsd.edu/~leekc/ExtYaleDatabase/ExtYaleB.html>

After deleting unrelated images

Load image data from each subject folder

totally 2410 * 32256 matrix (as Row Matrix)

Split train and test data by ratio: 9 vs 1

Train: 2169

Test: 241

| label | train_size | | | label | test_size | | |
|-------|------------|----|----|-------|-----------|----|----|
| 01 | 57 | 21 | 61 | 01 | 7 | 21 | 3 |
| 02 | 59 | 22 | 57 | 02 | 4 | 22 | 7 |
| 03 | 58 | 23 | 57 | 03 | 5 | 23 | 7 |
| 04 | 59 | 24 | 59 | 04 | 5 | 24 | 5 |
| 05 | 51 | 25 | 57 | 05 | 12 | 25 | 7 |
| 06 | 58 | 26 | 58 | 06 | 6 | 26 | 6 |
| 07 | 51 | 27 | 57 | 07 | 13 | 27 | 6 |
| 08 | 54 | 28 | 57 | 08 | 10 | 28 | 7 |
| 09 | 58 | 29 | 58 | 09 | 6 | 29 | 6 |
| 10 | 58 | 30 | 55 | 10 | 6 | 30 | 9 |
| 11 | 54 | 31 | 56 | 11 | 6 | 31 | 8 |
| 12 | 53 | 32 | 53 | 12 | 6 | 32 | 11 |
| 13 | 54 | 33 | 61 | 13 | 6 | 33 | 3 |
| 15 | 56 | 34 | 60 | 15 | 7 | 34 | 4 |
| 16 | 53 | 35 | 57 | 16 | 9 | 35 | 7 |
| 17 | 60 | 36 | 55 | 17 | 3 | 36 | 9 |
| 18 | 63 | 37 | 59 | 18 | 3 | 37 | 5 |
| 19 | 57 | 38 | 60 | 19 | 7 | 38 | 4 |
| 20 | 59 | 39 | 60 | 20 | 5 | 39 | 4 |

? Number of components

140 is enough to classify for **human** eye

But

More difficult to classify for **computer**



Grid Search
(optimal PCA)

Eigenvectors #20



Eigenvectors #100



Eigenvectors #180



Eigenvectors #260



Eigenvectors #40



Eigenvectors #120



Eigenvectors #200



Eigenvectors #280



Eigenvectors #60



Eigenvectors #140



Eigenvectors #220



Eigenvectors #300



Eigenvectors #80



Eigenvectors #160



Eigenvectors #240



Eigenvectors #320



Subject 19_Eigenface

Number of components = 200



X_{train} : 2169 * 200

X_{test} : 241 * 200



Grid Search_SVM(gaussian)

$N_FEATURES_OPTIONS = \text{range}(150, 250, 50)$

$C_OPTIONS = [1e3, 5e3, 1e4, 5e4, 1e5]$

$GAMMA_OPTIONS = [0.0001, 0.0005, 0.001, 0.005, 0.01, 0.1]$

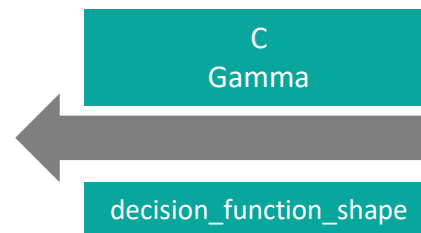


$N_FEATURES_OPTIONS = 200$

Predicting people's names on the test set
done in 0.228s

| | precision | recall | f1-score | support |
|-------------|-----------|--------|----------|---------|
| 01 | 1.00 | 1.00 | 1.00 | 7 |
| 02 | 1.00 | 1.00 | 1.00 | 4 |
| 03 | 1.00 | 1.00 | 1.00 | 5 |
| 04 | 1.00 | 1.00 | 1.00 | 5 |
| 05 | 1.00 | 1.00 | 1.00 | 12 |
| 06 | 1.00 | 1.00 | 1.00 | 6 |
| 07 | 0.93 | 1.00 | 0.96 | 13 |
| 08 | 1.00 | 1.00 | 1.00 | 10 |
| 09 | 1.00 | 1.00 | 1.00 | 6 |
| 10 | 1.00 | 1.00 | 1.00 | 6 |
| 11 | 0.86 | 1.00 | 0.92 | 6 |
| 12 | 1.00 | 1.00 | 1.00 | 6 |
| 13 | 1.00 | 1.00 | 1.00 | 6 |
| 15 | 1.00 | 1.00 | 1.00 | 7 |
| 16 | 0.89 | 0.89 | 0.89 | 9 |
| 17 | 1.00 | 1.00 | 1.00 | 3 |
| 18 | 0.00 | 0.00 | 0.00 | 0 |
| 19 | 1.00 | 1.00 | 1.00 | 7 |
| 20 | 0.83 | 1.00 | 0.91 | 5 |
| 21 | 1.00 | 1.00 | 1.00 | 3 |
| 22 | 1.00 | 1.00 | 1.00 | 7 |
| 23 | 1.00 | 0.86 | 0.92 | 7 |
| 24 | 1.00 | 1.00 | 1.00 | 5 |
| 25 | 1.00 | 0.86 | 0.92 | 7 |
| 26 | 1.00 | 1.00 | 1.00 | 6 |
| 27 | 1.00 | 1.00 | 1.00 | 6 |
| 28 | 1.00 | 1.00 | 1.00 | 7 |
| 29 | 1.00 | 0.83 | 0.91 | 6 |
| 30 | 1.00 | 1.00 | 1.00 | 9 |
| 31 | 1.00 | 1.00 | 1.00 | 8 |
| 32 | 1.00 | 0.82 | 0.90 | 11 |
| 33 | 1.00 | 1.00 | 1.00 | 3 |
| 34 | 1.00 | 1.00 | 1.00 | 4 |
| 35 | 0.88 | 1.00 | 0.93 | 7 |
| 36 | 0.90 | 1.00 | 0.95 | 9 |
| 37 | 1.00 | 1.00 | 1.00 | 5 |
| 38 | 1.00 | 0.75 | 0.86 | 4 |
| 39 | 1.00 | 1.00 | 1.00 | 4 |
| avg / total | 0.98 | 0.97 | 0.97 | 241 |
| 39 | 1.00 | 1.00 | 1.00 | 4 |
| avg / total | 0.98 | 0.97 | 0.97 | 241 |

Time: 0.228s
Accuracy: 0.98



Optimal_sigma

$$\sigma = \frac{1}{n} \sum_{i=1}^n \|\mathbf{x}_i - k\text{NN}(\mathbf{x}_i)\|_2$$

- Sampling 800 points by **label proportion** with **K=7**
- compute the **optimal** $\sigma = 113.0556$, $\gamma = 3.9119\text{e-}05$

+ Grid Search

C = 1e5

Gamma = 3.9119e-05

Decision_function_shape = "OVR"

Predicting people's names on the test set
done in 0.392s

| | precision | recall | f1-score | support |
|-------------|-----------|--------|----------|---------|
| 01 | 1.00 | 1.00 | 1.00 | 7 |
| 02 | 1.00 | 1.00 | 1.00 | 4 |
| 03 | 1.00 | 1.00 | 1.00 | 5 |
| 04 | 1.00 | 1.00 | 1.00 | 5 |
| 05 | 1.00 | 1.00 | 1.00 | 12 |
| 06 | 1.00 | 1.00 | 1.00 | 6 |
| 07 | 1.00 | 0.92 | 0.96 | 13 |
| 08 | 1.00 | 1.00 | 1.00 | 10 |
| 09 | 0.86 | 1.00 | 0.92 | 6 |
| 10 | 0.86 | 1.00 | 0.92 | 6 |
| 11 | 1.00 | 1.00 | 1.00 | 6 |
| 12 | 1.00 | 1.00 | 1.00 | 6 |
| 13 | 1.00 | 1.00 | 1.00 | 6 |
| 15 | 1.00 | 1.00 | 1.00 | 7 |
| 16 | 0.90 | 1.00 | 0.95 | 9 |
| 17 | 1.00 | 1.00 | 1.00 | 3 |
| 19 | 1.00 | 1.00 | 1.00 | 7 |
| 20 | 1.00 | 1.00 | 1.00 | 5 |
| 21 | 1.00 | 1.00 | 1.00 | 3 |
| 22 | 1.00 | 0.86 | 0.92 | 7 |
| 23 | 0.88 | 1.00 | 0.93 | 7 |
| 24 | 1.00 | 1.00 | 1.00 | 5 |
| 25 | 1.00 | 1.00 | 1.00 | 7 |
| 26 | 1.00 | 1.00 | 1.00 | 6 |
| 27 | 1.00 | 1.00 | 1.00 | 6 |
| 28 | 0.88 | 1.00 | 0.93 | 7 |
| 29 | 1.00 | 0.83 | 0.91 | 6 |
| 30 | 1.00 | 0.89 | 0.94 | 9 |
| 31 | 1.00 | 1.00 | 1.00 | 8 |
| 32 | 1.00 | 0.82 | 0.90 | 11 |
| 33 | 1.00 | 1.00 | 1.00 | 3 |
| 34 | 1.00 | 1.00 | 1.00 | 4 |
| 35 | 0.88 | 1.00 | 0.93 | 7 |
| 36 | 1.00 | 1.00 | 1.00 | 9 |
| 37 | 1.00 | 1.00 | 1.00 | 5 |
| 38 | 1.00 | 1.00 | 1.00 | 4 |
| 39 | 1.00 | 1.00 | 1.00 | 4 |
| avg / total | 0.98 | 0.98 | 0.97 | 241 |

Time: 0.392s
Accuracy: 0.98

C
Degree

decision_function_shape

Grid Search

DEGREE_OPTIONS = [2,3]

C_OPTIONS = [1e3, 5e3, 1e4, 5e4, 1e5]



C = 1e4

Degree = 2

Decision_function_shape = "OVR"

Predicting people's names on the test set
done in 0.108s

| | precision | recall | f1-score | support |
|-------------|-----------|--------|----------|---------|
| 01 | 1.00 | 1.00 | 1.00 | 7 |
| 02 | 1.00 | 1.00 | 1.00 | 4 |
| 03 | 1.00 | 1.00 | 1.00 | 5 |
| 04 | 1.00 | 1.00 | 1.00 | 5 |
| 05 | 1.00 | 1.00 | 1.00 | 12 |
| 06 | 1.00 | 1.00 | 1.00 | 6 |
| 07 | 1.00 | 1.00 | 1.00 | 13 |
| 08 | 1.00 | 1.00 | 1.00 | 10 |
| 09 | 1.00 | 1.00 | 1.00 | 6 |
| 10 | 1.00 | 1.00 | 1.00 | 6 |
| 11 | 1.00 | 1.00 | 1.00 | 6 |
| 12 | 1.00 | 1.00 | 1.00 | 6 |
| 13 | 1.00 | 1.00 | 1.00 | 6 |
| 15 | 1.00 | 1.00 | 1.00 | 7 |
| 16 | 0.90 | 1.00 | 0.95 | 9 |
| 17 | 0.75 | 1.00 | 0.86 | 3 |
| 19 | 1.00 | 1.00 | 1.00 | 7 |
| 20 | 1.00 | 1.00 | 1.00 | 5 |
| 21 | 1.00 | 1.00 | 1.00 | 3 |
| 22 | 1.00 | 1.00 | 1.00 | 7 |
| 23 | 1.00 | 1.00 | 1.00 | 7 |
| 24 | 1.00 | 1.00 | 1.00 | 5 |
| 25 | 1.00 | 1.00 | 1.00 | 7 |
| 26 | 1.00 | 1.00 | 1.00 | 6 |
| 27 | 1.00 | 1.00 | 1.00 | 6 |
| 28 | 1.00 | 1.00 | 1.00 | 7 |
| 29 | 1.00 | 0.83 | 0.91 | 6 |
| 30 | 1.00 | 0.89 | 0.94 | 9 |
| 31 | 1.00 | 1.00 | 1.00 | 8 |
| 32 | 1.00 | 0.91 | 0.95 | 11 |
| 33 | 1.00 | 1.00 | 1.00 | 3 |
| 34 | 1.00 | 1.00 | 1.00 | 4 |
| 35 | 0.88 | 1.00 | 0.93 | 7 |
| 36 | 1.00 | 1.00 | 1.00 | 9 |
| 37 | 1.00 | 1.00 | 1.00 | 5 |
| 38 | 1.00 | 1.00 | 1.00 | 4 |
| 39 | 1.00 | 1.00 | 1.00 | 4 |
| avg / total | 0.99 | 0.99 | 0.99 | 241 |

Time: 0.1s
Accuracy: 0.99

C

decision_function_shape

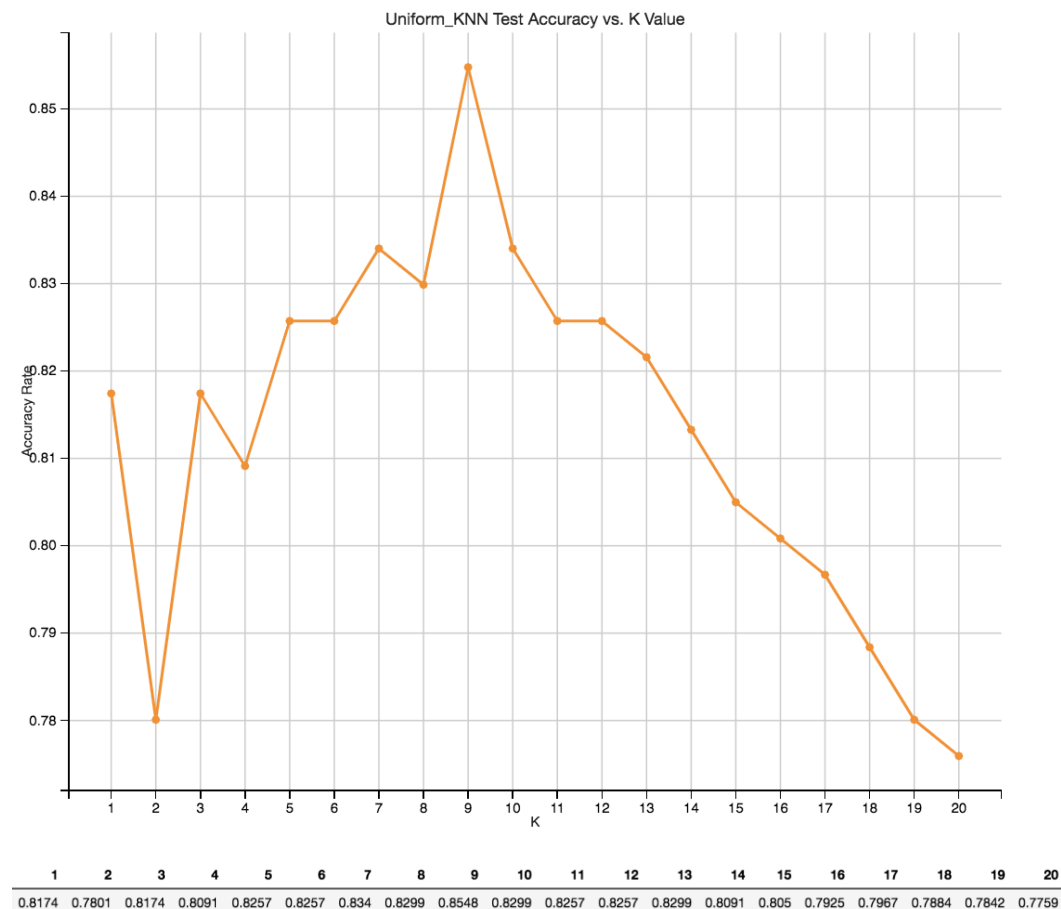
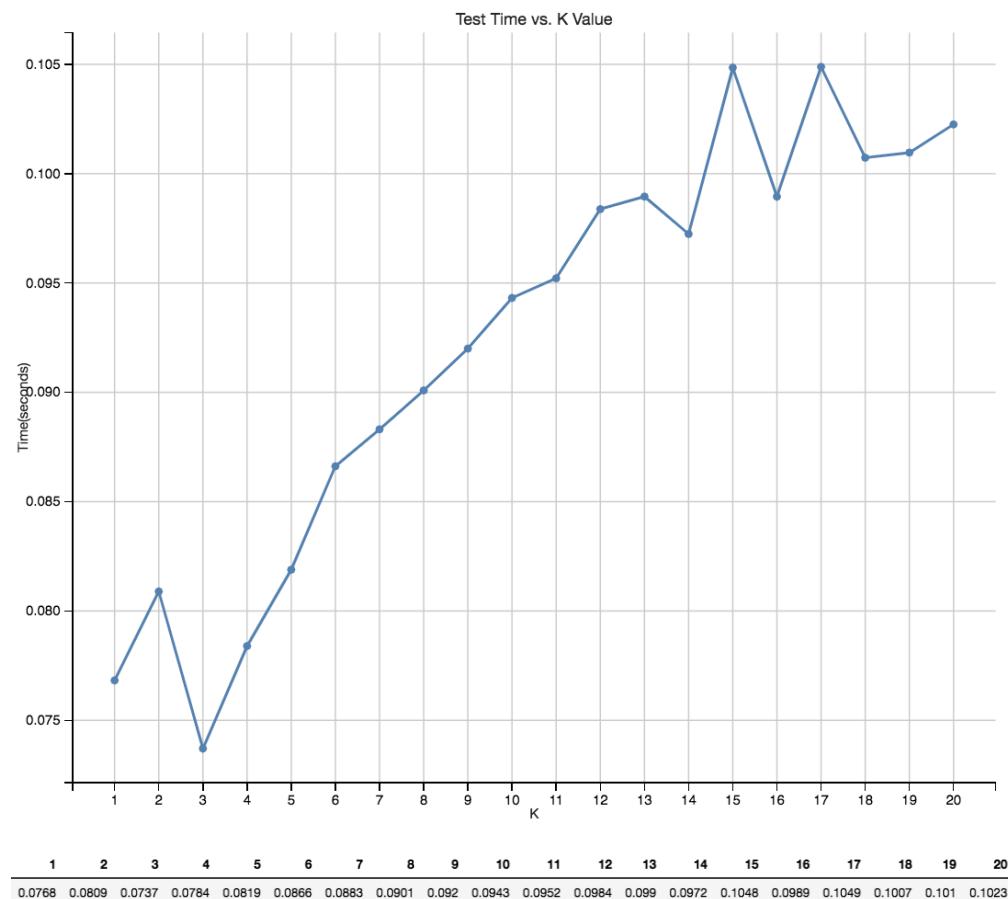
Grid Search

C_OPTIONS = [1e3, 5e3, 1e4, 5e4, 1e5]

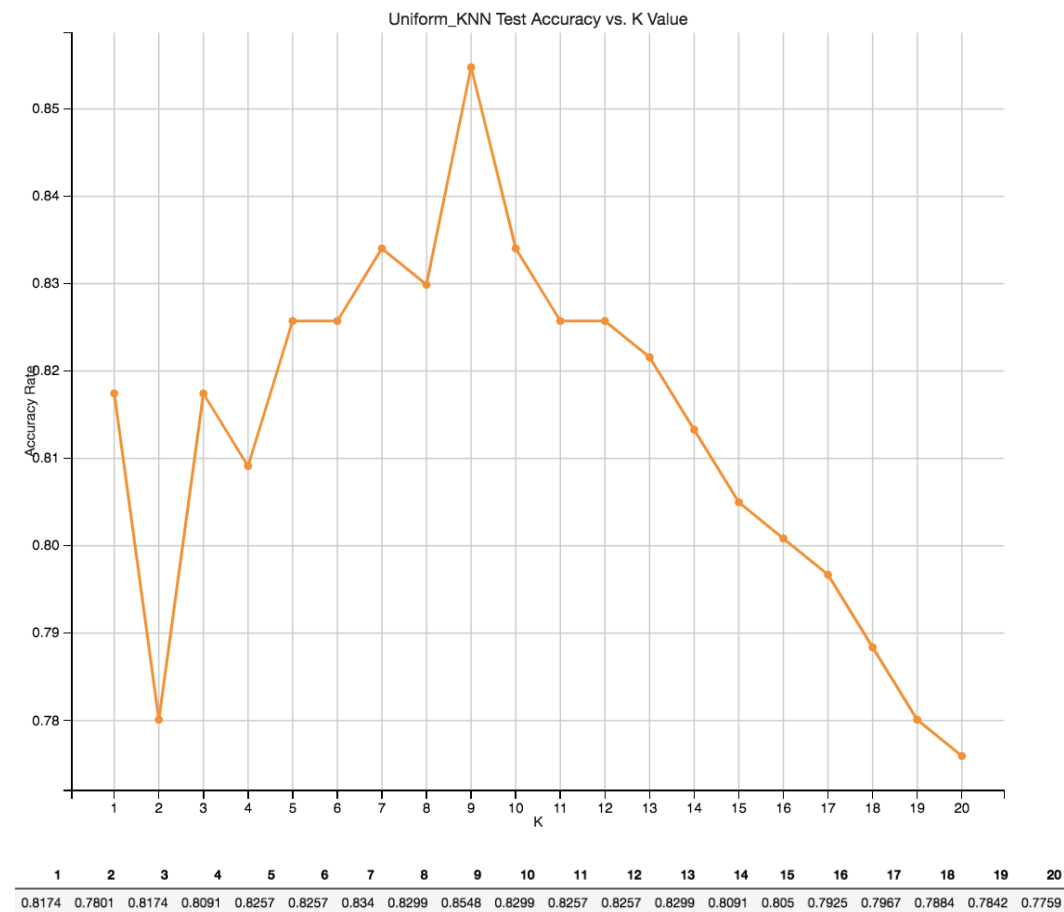
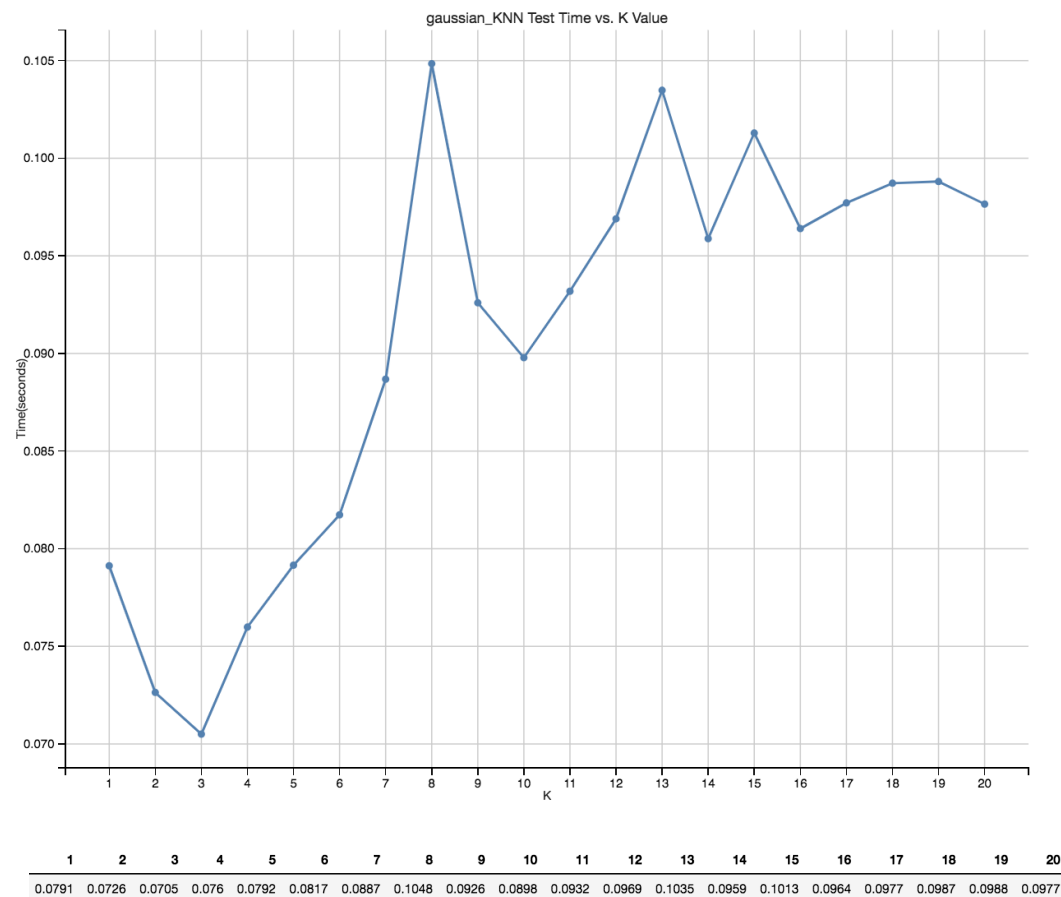


C = 1e3

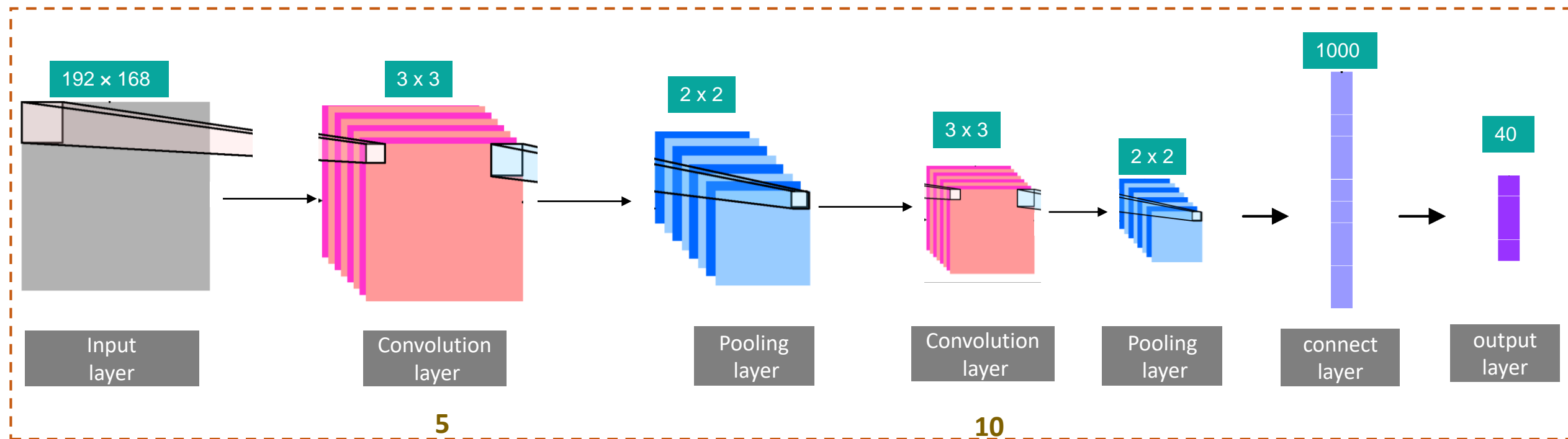
Decision_function_shape = "OVR"



Optimal K = 9
Optimal accuracy = 0.85



Optimal K = 9
Optimal accuracy = 0.85

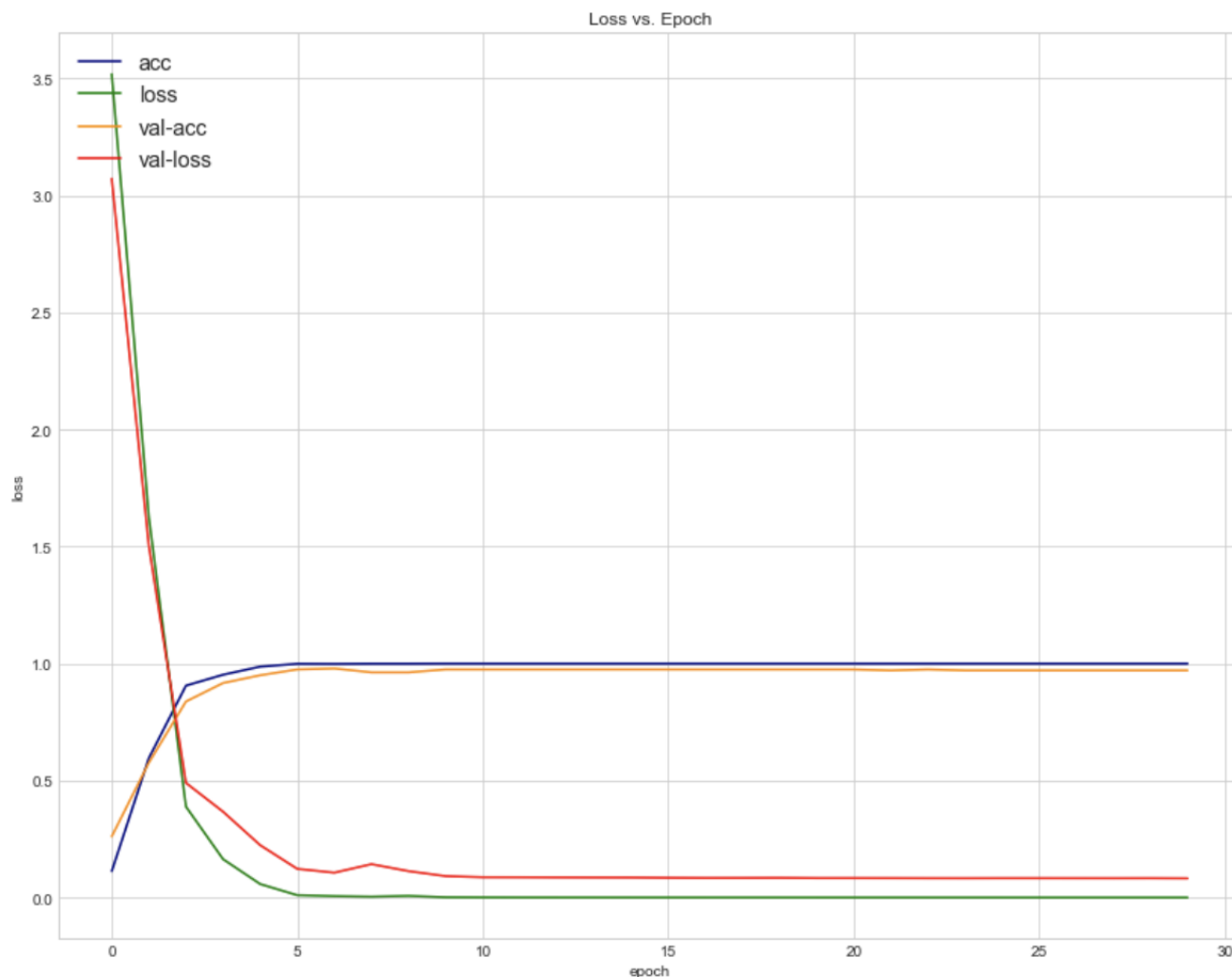


epoch = ?
batch size = 40
learning rate = ?
decay = 1e-6
Momentum = 0.9

Train on 2169 samples, validate on 241 samples

```
Epoch 1/20
- 28s - loss: 2.8309 - acc: 0.2955 - val_loss: 2.3157 - val_acc: 0.3983
Epoch 2/20
- 25s - loss: 0.8050 - acc: 0.7847 - val_loss: 1.0823 - val_acc: 0.6805
Epoch 3/20
- 26s - loss: 0.2591 - acc: 0.9331 - val_loss: 0.3446 - val_acc: 0.8963
Epoch 4/20
- 25s - loss: 0.1123 - acc: 0.9756 - val_loss: 0.9439 - val_acc: 0.7759
Epoch 5/20
- 29s - loss: 0.1222 - acc: 0.9742 - val_loss: 0.2534 - val_acc: 0.9212
Epoch 6/20
- 26s - loss: 0.0139 - acc: 0.9986 - val_loss: 0.1411 - val_acc: 0.9627
Epoch 7/20
- 26s - loss: 0.0022 - acc: 1.0000 - val_loss: 0.1206 - val_acc: 0.9710
Epoch 8/20
- 24s - loss: 0.0012 - acc: 1.0000 - val_loss: 0.1187 - val_acc: 0.9668
Epoch 9/20
- 24s - loss: 9.5081e-04 - acc: 1.0000 - val_loss: 0.1201 - val_acc: 0.9668
Epoch 10/20
- 24s - loss: 8.0084e-04 - acc: 1.0000 - val_loss: 0.1198 - val_acc: 0.9668
Epoch 11/20
- 23s - loss: 6.9909e-04 - acc: 1.0000 - val_loss: 0.1196 - val_acc: 0.9668
Epoch 12/20
- 23s - loss: 6.1535e-04 - acc: 1.0000 - val_loss: 0.1199 - val_acc: 0.9668
Epoch 13/20
- 23s - loss: 5.5325e-04 - acc: 1.0000 - val_loss: 0.1186 - val_acc: 0.9710
Epoch 14/20
- 23s - loss: 5.0282e-04 - acc: 1.0000 - val_loss: 0.1191 - val_acc: 0.9710
Epoch 15/20
- 24s - loss: 4.6045e-04 - acc: 1.0000 - val_loss: 0.1196 - val_acc: 0.9710
Epoch 16/20
- 23s - loss: 4.2575e-04 - acc: 1.0000 - val_loss: 0.1203 - val_acc: 0.9710
Epoch 17/20
- 23s - loss: 3.9592e-04 - acc: 1.0000 - val_loss: 0.1199 - val_acc: 0.9710
Epoch 18/20
- 23s - loss: 3.6939e-04 - acc: 1.0000 - val_loss: 0.1198 - val_acc: 0.9710
Epoch 19/20
- 23s - loss: 3.4539e-04 - acc: 1.0000 - val_loss: 0.1200 - val_acc: 0.9710
Epoch 20/20
- 23s - loss: 3.2489e-04 - acc: 1.0000 - val_loss: 0.1200 - val_acc: 0.9710
```

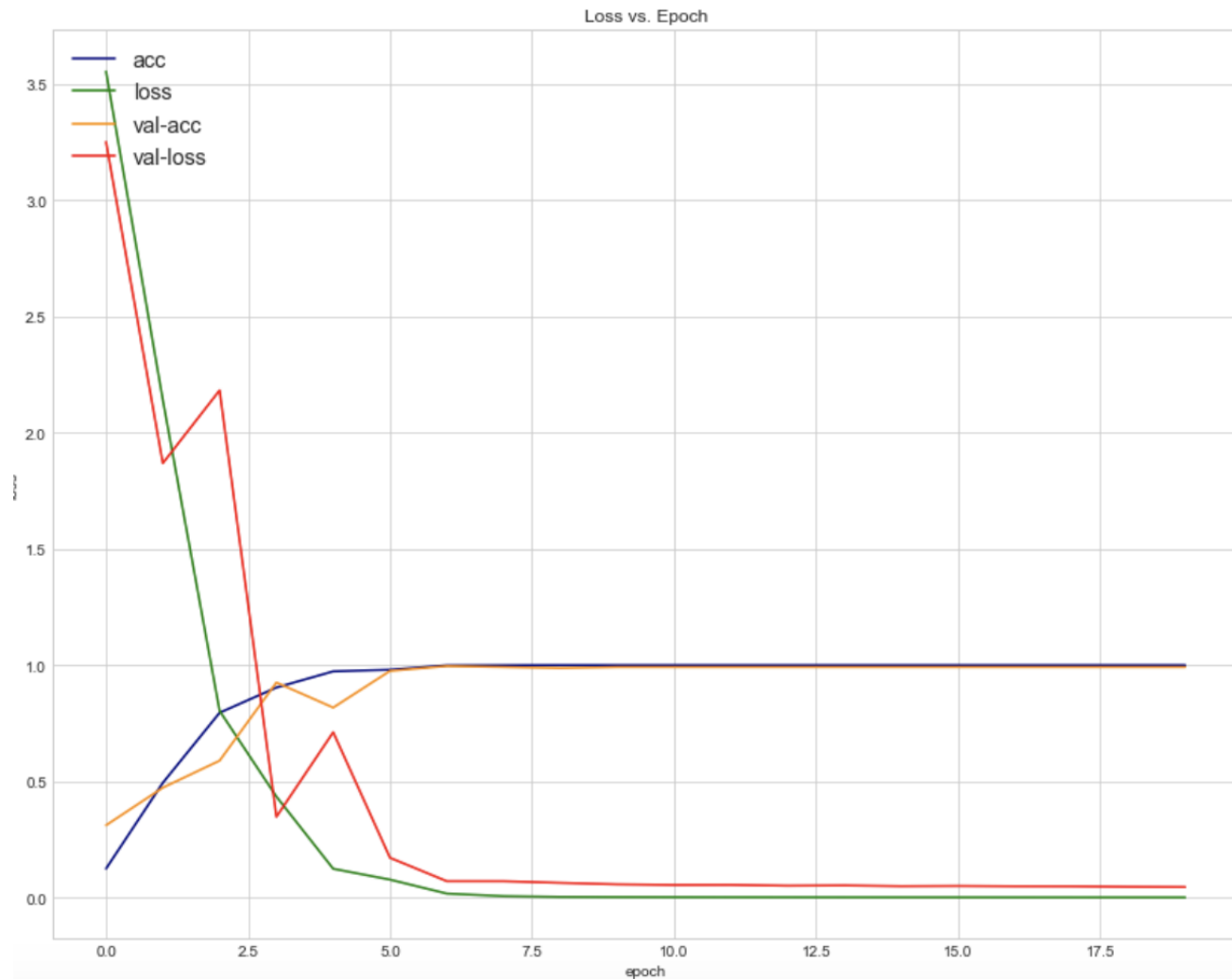
learning rate = 0.002



Train on 2169 samples, validate on 241 samples

```
Epoch 1/20
- 25s - loss: 3.5532 - acc: 0.1245 - val_loss: 3.2501 - val_acc: 0.3112
Epoch 2/20
- 24s - loss: 2.1410 - acc: 0.4938 - val_loss: 1.8681 - val_acc: 0.4730
Epoch 3/20
- 23s - loss: 0.8033 - acc: 0.7953 - val_loss: 2.1818 - val_acc: 0.5892
Epoch 4/20
- 24s - loss: 0.4346 - acc: 0.9036 - val_loss: 0.3477 - val_acc: 0.9253
Epoch 5/20
- 26s - loss: 0.1243 - acc: 0.9733 - val_loss: 0.7114 - val_acc: 0.8174
Epoch 6/20
- 27s - loss: 0.0776 - acc: 0.9802 - val_loss: 0.1716 - val_acc: 0.9751
Epoch 7/20
- 25s - loss: 0.0176 - acc: 0.9991 - val_loss: 0.0709 - val_acc: 0.9959
Epoch 8/20
- 25s - loss: 0.0065 - acc: 0.9995 - val_loss: 0.0707 - val_acc: 0.9917
Epoch 9/20
- 28s - loss: 0.0033 - acc: 1.0000 - val_loss: 0.0637 - val_acc: 0.9876
Epoch 10/20
- 25s - loss: 0.0025 - acc: 1.0000 - val_loss: 0.0574 - val_acc: 0.9917
Epoch 11/20
- 26s - loss: 0.0022 - acc: 1.0000 - val_loss: 0.0547 - val_acc: 0.9917
Epoch 12/20
- 25s - loss: 0.0019 - acc: 1.0000 - val_loss: 0.0550 - val_acc: 0.9917
Epoch 13/20
- 26s - loss: 0.0017 - acc: 1.0000 - val_loss: 0.0515 - val_acc: 0.9917
Epoch 14/20
- 25s - loss: 0.0015 - acc: 1.0000 - val_loss: 0.0527 - val_acc: 0.9917
Epoch 15/20
- 26s - loss: 0.0014 - acc: 1.0000 - val_loss: 0.0495 - val_acc: 0.9917
Epoch 16/20
- 26s - loss: 0.0013 - acc: 1.0000 - val_loss: 0.0505 - val_acc: 0.9917
Epoch 17/20
- 26s - loss: 0.0012 - acc: 1.0000 - val_loss: 0.0491 - val_acc: 0.9917
Epoch 18/20
- 25s - loss: 0.0011 - acc: 1.0000 - val_loss: 0.0488 - val_acc: 0.9917
Epoch 19/20
- 26s - loss: 0.0010 - acc: 1.0000 - val_loss: 0.0470 - val_acc: 0.9917
Epoch 20/20
- 25s - loss: 9.7845e-04 - acc: 1.0000 - val_loss: 0.0459 - val_acc: 0.9917
506.5965440273285 s
```

learning rate = 0.001



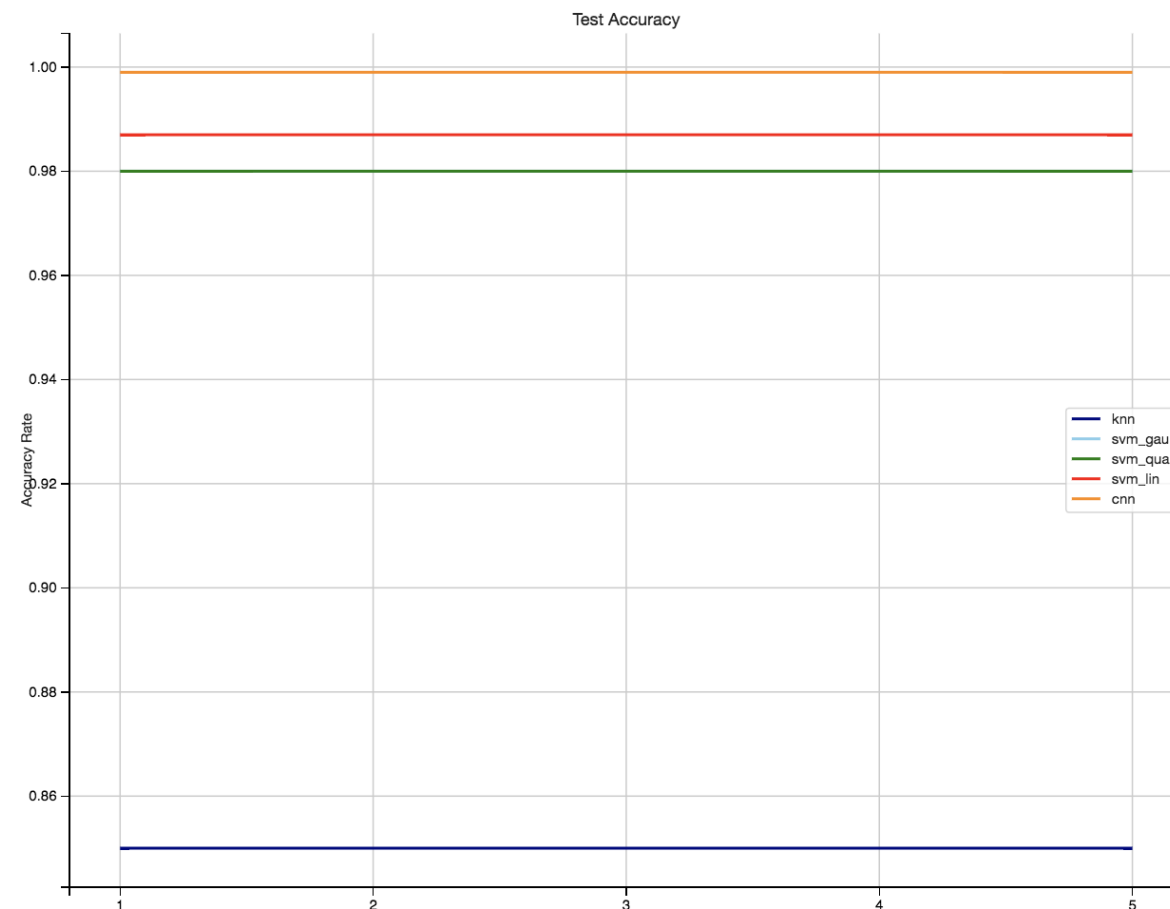
| Method | Time (s) | Accuracy |
|----------------|----------|----------|
| KNN(K=9) | 0.09 | 0.85 |
| SVM (Gaussian) | 0.23 | 0.98 |
| SVM (poly=2) | 0.39 | 0.98 |
| SVM (linear) | 0.10 | 0.987 |
| CNN (lr=0.001) | 502 | 0.999 |

Same pose under Illumination variation

Convolution Neural Network performs **best** with the highest test accuracy **0.999**

KNN performs **worst** with the lowest test accuracy **0.85**

There's **no significant difference** among the choices of kernel function choices for **SVM**



**How about
Pose & Illumination Variation
?**

;

POSE & ILLUMINATION VARIATION



Extended Yale Face Database B

UCSD. Vision

<http://vision.ucsd.edu/~leekc/ExtYaleDatabase/ExtYaleB.html>

contains 16128 images of 28 human subjects
under 9 poses and 64 illumination conditions

640 × 480 pixels

Based on these experiments and data:

Cropped data VS Extended data

- more pictures as training >>> easier to classify a subject, even adding pose variation

7 subject VS 12 subjects (extended data)

- less subjects >>> easier to classify

7 subjects :

11/12/13/15/16/17/18

| Method | Time | Accuracy |
|----------------|-------|----------|
| KNN(K=2) | 0.09 | 1 |
| SVM (Gaussian) | 0.19 | 1 |
| SVM (poly=2) | 0.754 | 1 |
| SVM (linear) | 0.94 | 1 |
| CNN | 821 | 1 |

12 subjects :

11/12/13/15/16/17/18/19/23/25/29/36

| Method | Time | Accuracy |
|----------------|------|----------|
| KNN(K=1) | 0.17 | 0.93 |
| SVM (Gaussian) | 0.19 | 0.98 |
| SVM (poly=3) | 4.77 | 0.99 |
| SVM (linear) | 0.75 | 0.98 |
| CNN | | 0.99 |

Georghiades, A.S., Belhumeur, P.N., Kriegman, D.J., *“From Few to Many: Illumination Cone Models for Face Recognition under Variable Lighting and Pose,”* IEEE Trans. Pattern Anal. Mach. Intelligence, 2001, Vol.23, pp.643-660

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V. Tata, *“Simple Image Classification using Convolutional Neural Network,”* <https://becominghuman.ai/building-an-image-classifier-using-deep-learning-in-python-totally-from-a-beginners-perspective-be8dbaf22dd8>

THANKS