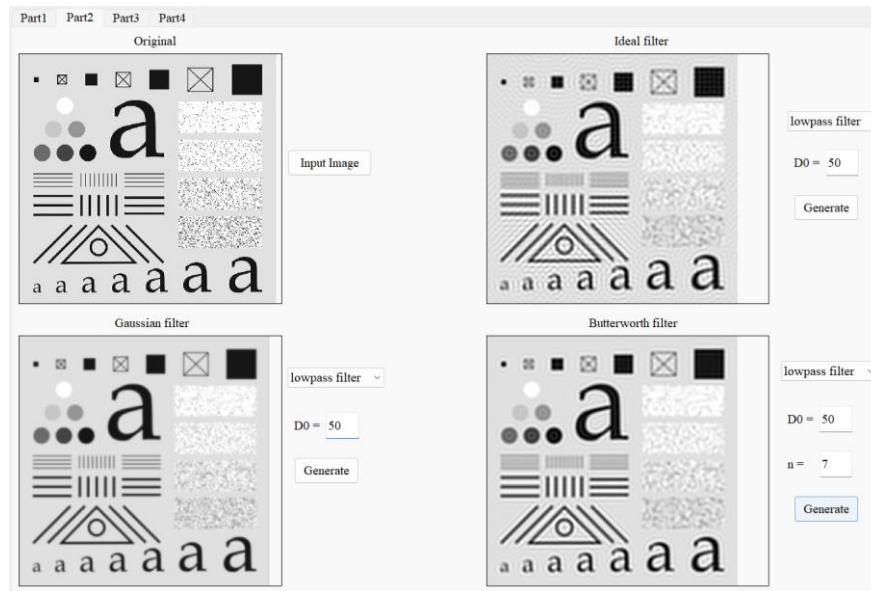
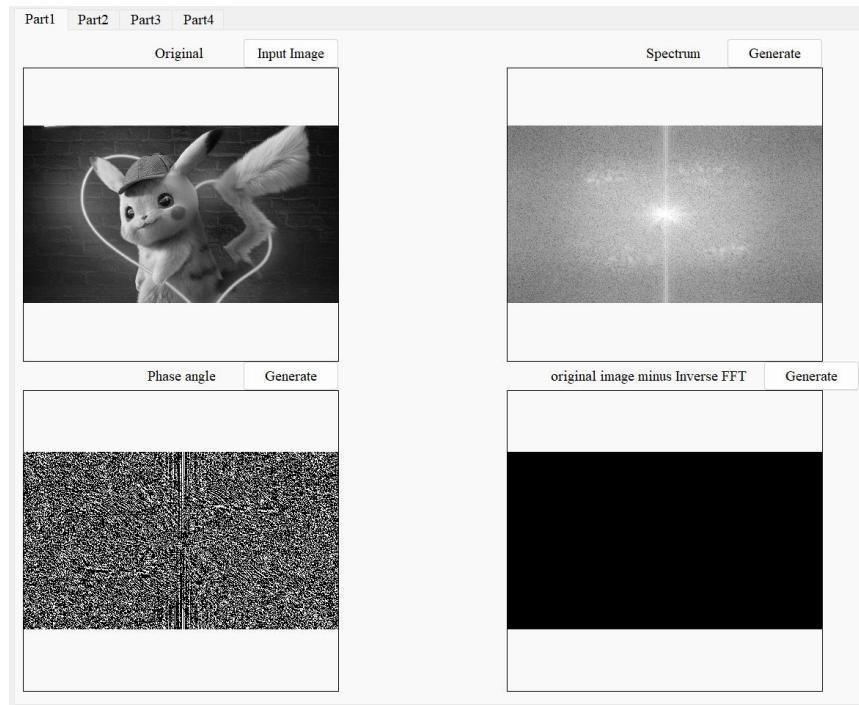
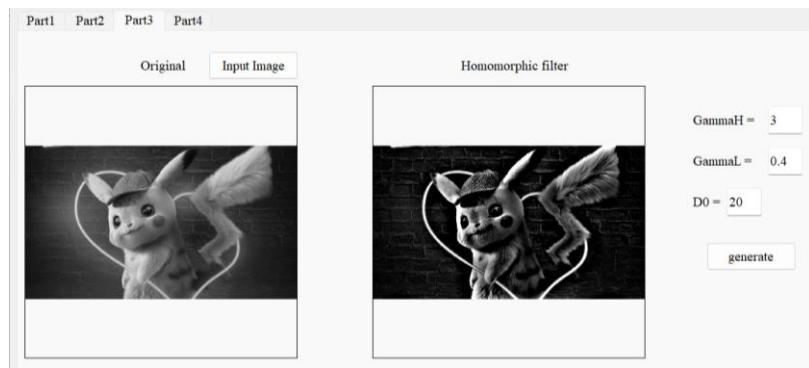


HW4 r12631001 許喬淇

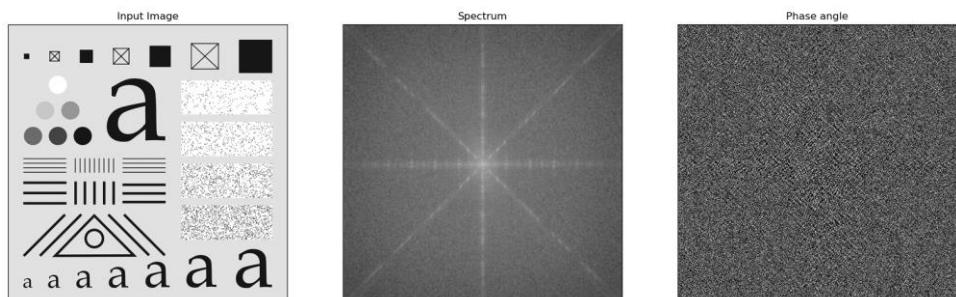
UI :





Part1 :

`button_clicked_input1()`取得影像路徑，`fft()`為快速傅立葉轉換，`ifft()`為反轉傅立葉轉換。下圖分別為原始影像、頻譜圖和向位角。



將原始影像減去 `ifft` 觀察差異，發現影像中有許多白點，因此傅立葉轉換前後的影像有差異。



對同一影像分別 `resize` 為(512, 512)、(1024, 1024)、(2048, 2048)，並計算 FFT 所需時間，發現隨著影像尺寸增加，運算時間也增加。

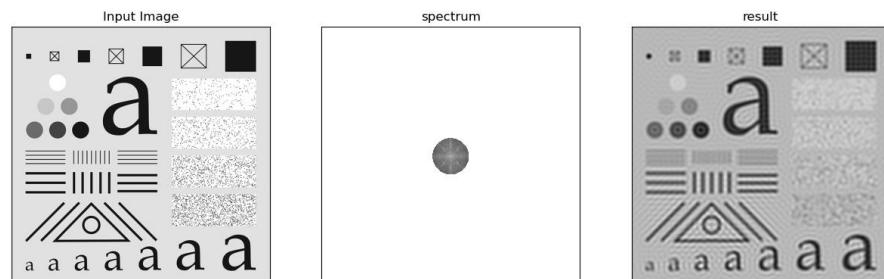
尺寸	(512, 512)	(1024, 1024)	(2048, 2048)
時間	0.0054s	0.0259s	0.1221s

Part2 :

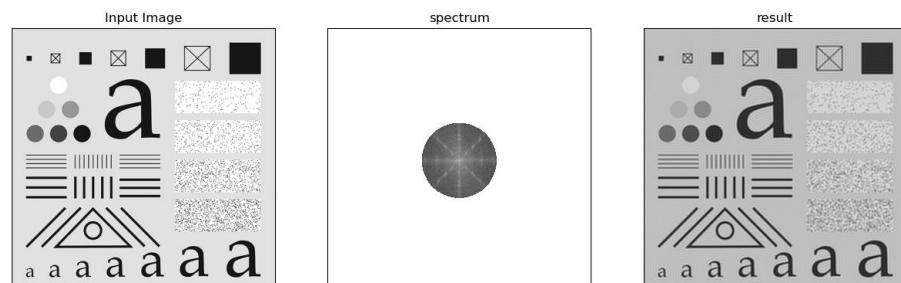
使用 `button_clicked_input2()` 取得影像路徑，影像經 `ideal_filter()`、
`gaussian_filter()`、`butterworth_filter()` 可得到各遮罩運算後的頻譜圖。

1. Ideal filter :

(a) Lowpass filter : D_0 越小則經遮罩運算之結果影像越模糊，反之越大則越清晰。

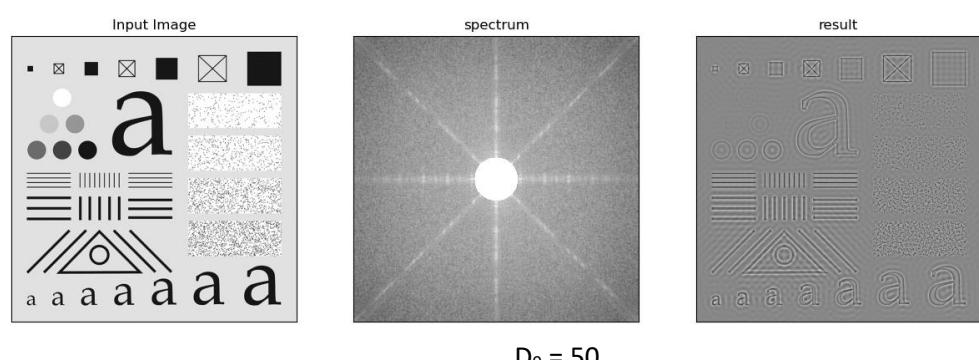


$$D_0 = 50$$

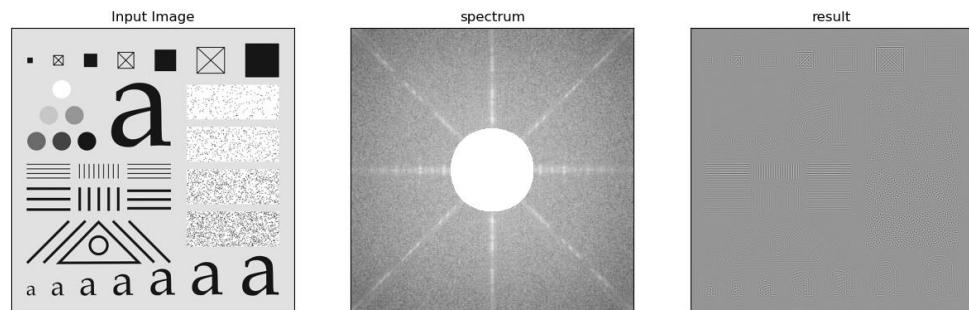


$$D_0 = 100$$

(b) Highpass filter : D_0 越小則經運算後結果之邊界較清晰，反之則越不清楚。



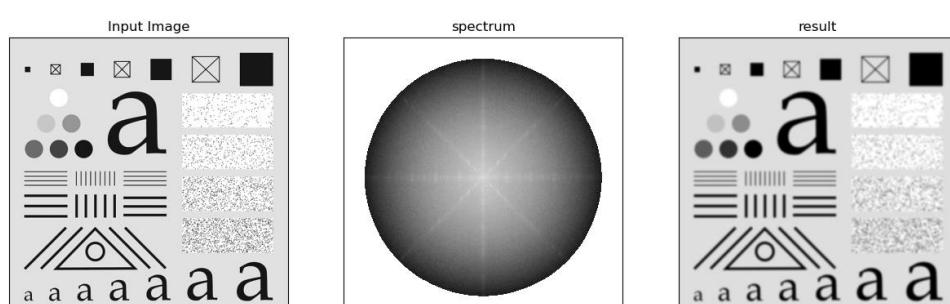
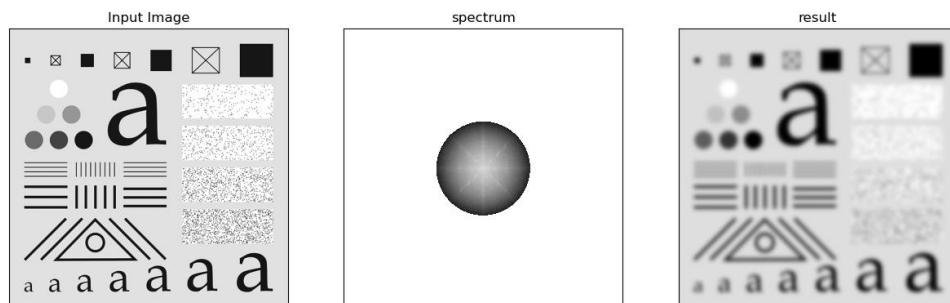
$$D_0 = 50$$



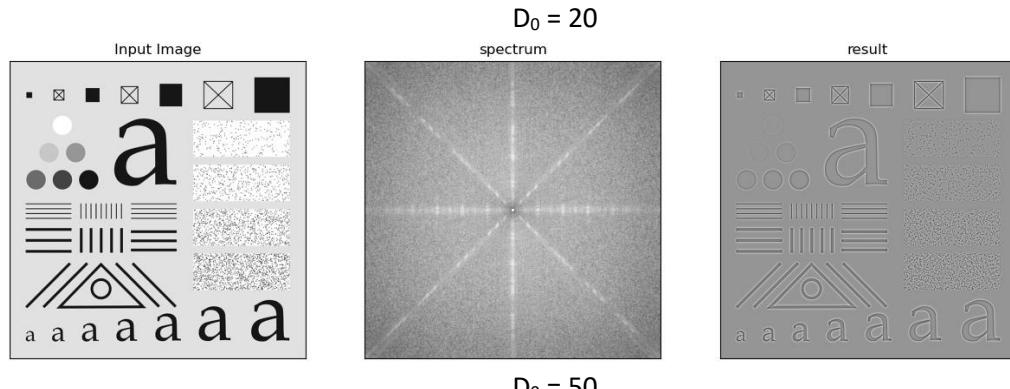
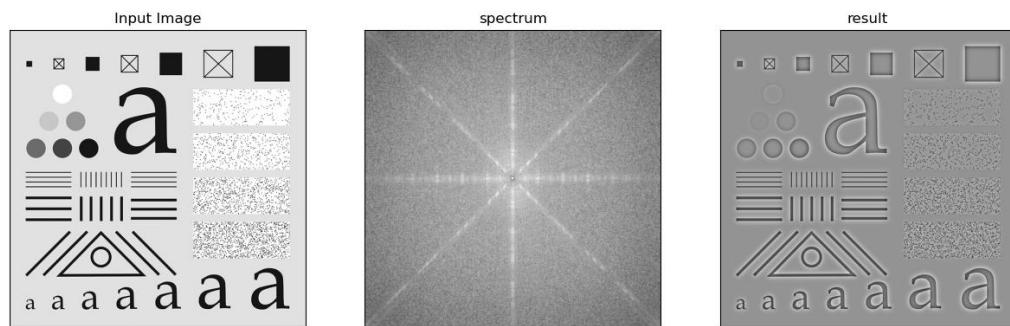
$$D_0 = 100$$

2. Gaussian filter :

(a) Lowpass filter : D_0 越小則經遮罩運算之結果影像越模糊，反之越大則越清晰。

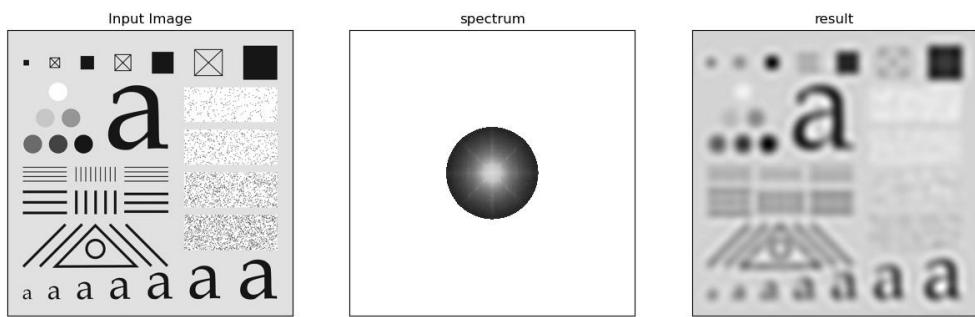


(b) Highpass filter : D_0 越小則遮罩運算結果的圖案較清楚，反之則較不清楚。

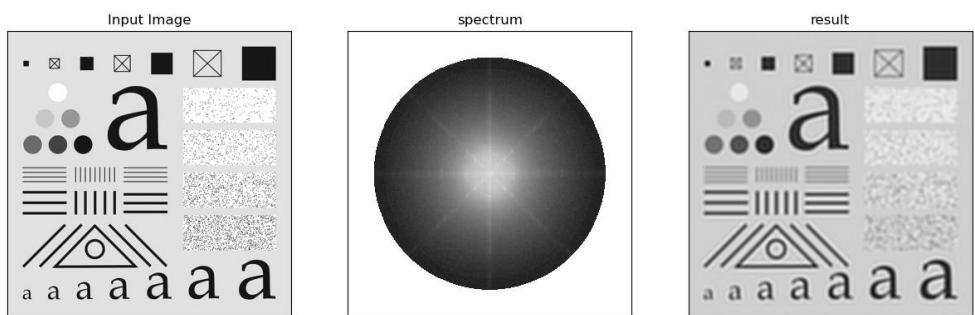


3. Butterworth filter :

(a) Lowpass filter : D_0 越小則經遮罩運算之結果影像越模糊，反之越大則越清晰。

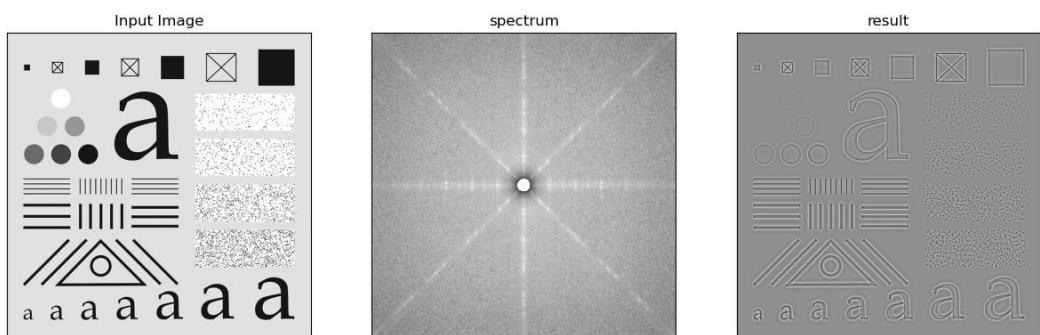


$D_0 = 20$

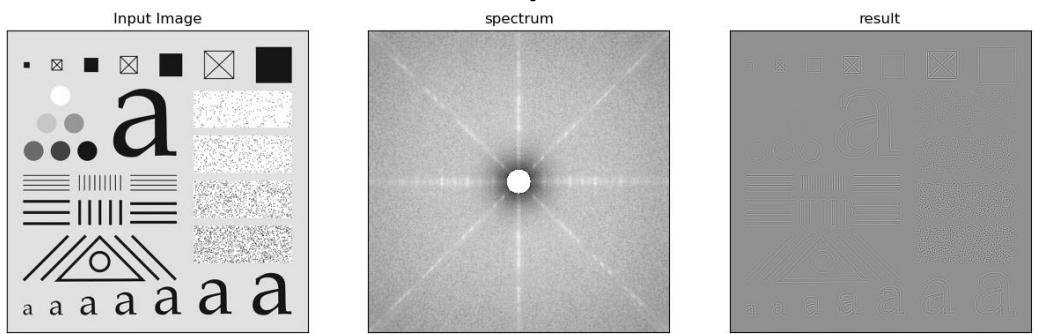


$D_0 = 50$

(c) Highpass filter : D_0 越小則遮罩運算結果的圖案輪廓較清楚，反之則較不清楚。



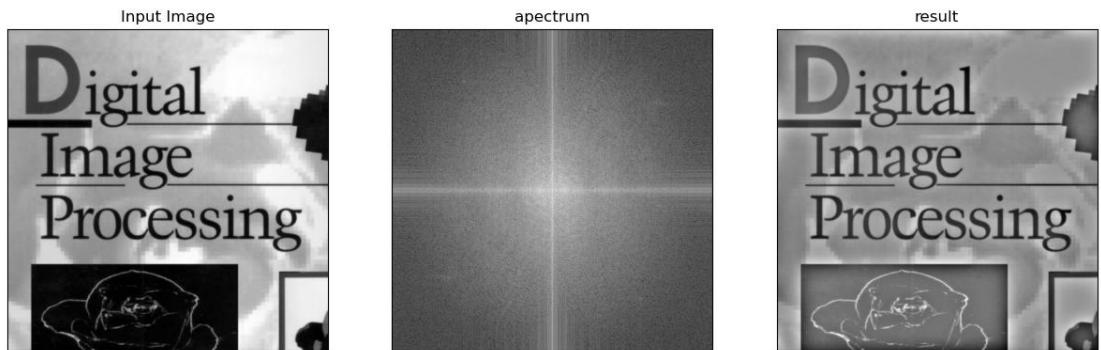
$D_0 = 50$



$D_0 = 100$

Part3 :

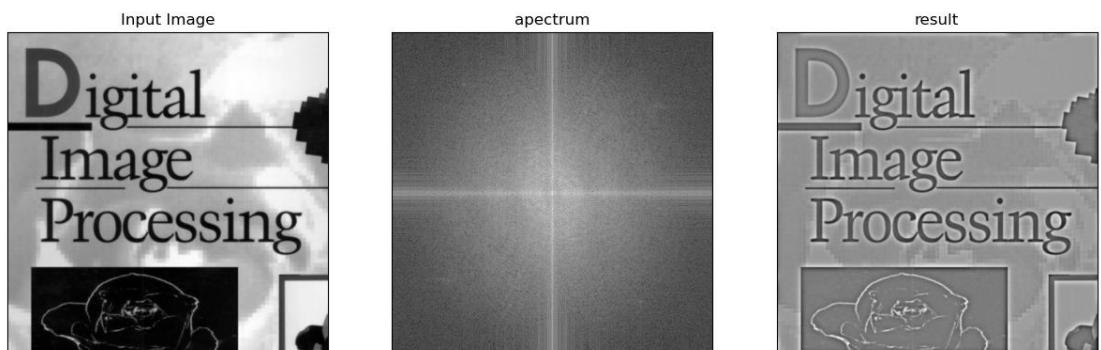
使用 `button_clicked_input3()` 取得影像路徑，原始影像經 `homomorphic_filter()` 可得遮罩運算後頻譜圖。而參數 D_0 增加時影像對比度增加，反之減少； γ_H 的增減只有些微的亮度差異； γ_H 增加時則有似光暈的效果。



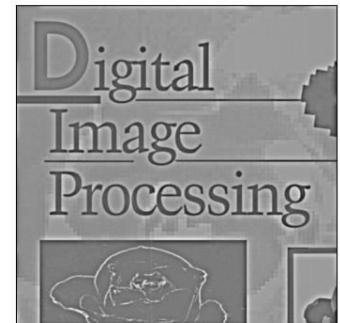
result



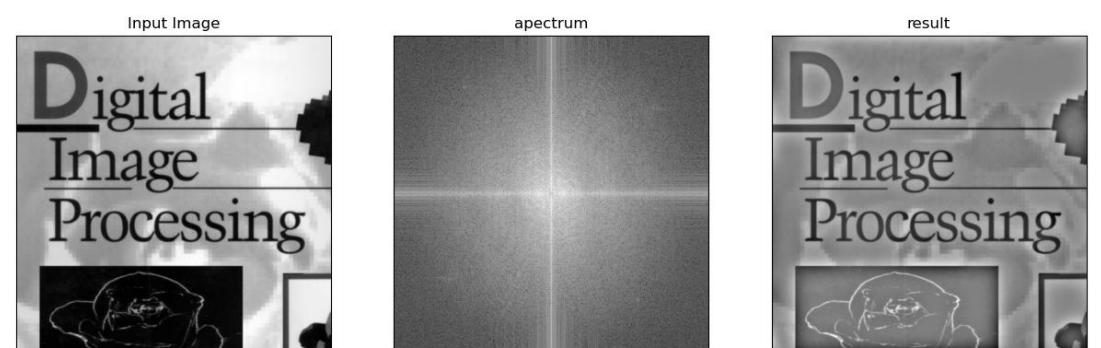
$$D_0 = 20, \gamma_H = 3, \gamma_H = 0.4$$



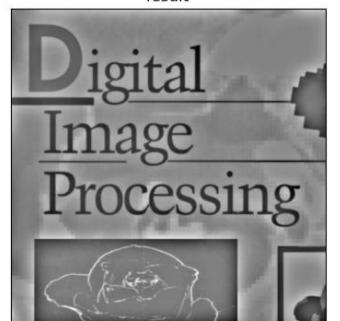
result



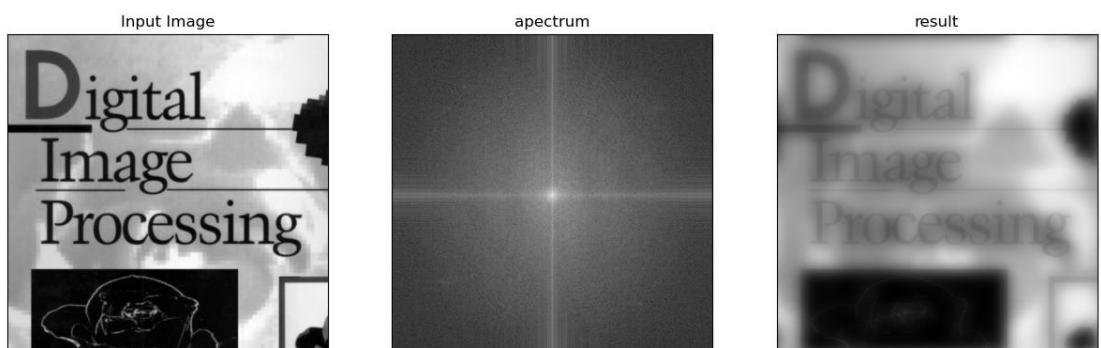
$$D_0 = 60, \gamma_H = 3, \gamma_H = 0.4$$



result



$$D_0 = 20, \gamma_H = 100, \gamma_H = 0.4$$



result



$$D_0 = 20, \gamma_H = 3, \gamma_H = 40$$

Part4 :

對於 motion blurred 之影像，wiener 有較清晰的 de-blurring 結果。

