On the Synthesis of Discrete Controllers

On the Synthesis of Discrete Controllers for Timed Systems

An Extended Abstract

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Introduction[']

This paper presents algorithms for the automatic synthesis of the real time controllers by finding a winning strategy for certain games defined by the timed automata of Alur and Dill.

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—Abstract

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Introduction

Consider a dynamical system P, whose presentation describes all its possible behaviours. A subset of the plant's behaviours, satisfying some criterion is defined as good or acceptable.

A controller C is another system which can interact with P in a certain manner by observing the state of P and by issuing control actions that influence the behaviour of P.

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—The problem

Consider a dynamical system P, whose presentation describe all its possible behaviours. A subset of the plant's behaviours satisfying some criterion is defined as good or acceptable !i.

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Introduction

The synthesis problem is then, to find out whether, for a given P, there exists a realizable controller C such that their interaction will produce only good behaviours.

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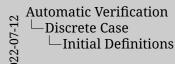
Definition 1 (Plant)

A plant automaton is a tuple $\mathcal{P} = (Q, \Sigma_c, \delta, q_0)$ where Q is a finite set of states, Σ_c is a set of controller commands, δ : $Q \times \Sigma_c \longmapsto 2^Q$ is the transition function and $g_0 \in Q$ is an initial state.

Definition 2 (Controllers)

A controller (strategy) for a plant specified by $\mathcal{P} = (Q, \Sigma_c, \delta, q_0)$ is a function $C: Q^+ \mapsto \Sigma_c$. A simple controller is a controller that can be written as a function $C: Q \longrightarrow \Sigma_c$.





We are interested in the simpler cases of controllers that base their decisions on a finite memory.

Definition 3 (Trajectories)

Let \mathcal{P} be a plant and let $C: Q^+ \longmapsto \Sigma_c$ be a controller. An infinite sequence of states $\alpha: q[0], q[1], \ldots$ such that $q[0] = q_0$ is called a trajectory of \mathcal{P} if

$$q[i+1] \in \bigcup_{\sigma \in \Sigma_c} \delta(q[i], \sigma)$$

and a C-trajectory if $q[i+1] \in \delta(q[i], C[\alpha[0..i]])$ for every $i \ge 0$. The corresponding sets of trajectories are denoted by $L(\mathcal{P})$ and $L_{\mathcal{C}}(\mathcal{P})$.

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For every infinite trajectory $\alpha \in L(\mathcal{P})$:

- $ightharpoonup Vis(\alpha)$ denote the set of all states appearing in α
- Inf(α) denote the set of all states appearing in α infinitely many times

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Vis(a) denote the set of all states appearing in a
 Inf(a) denote the set of all states appearing in a

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Definition 4 (Acceptance Condition)

Let $\mathcal{P} = (Q, \Sigma_c, \delta, q_0)$ be a plant. An acceptance condition for \mathcal{P} is

$$\Omega \in \{(F, \square), (F, \lozenge), (F, \lozenge \square), (F, \square \lozenge), (\mathcal{F}, \mathcal{R}_n)\}$$

where $\mathcal{F} = \{(F_i, G_i)\}_{i=1}^n$ and F, F_i and G_i are certain subsets of Q referred as the good states. The set of sequences of \mathcal{P} that are accepted according to Ω is defined as follows:

$$\begin{array}{ll} L(\mathcal{P}, F, \square) & \{\alpha \in L(\mathcal{P}) : \textit{Vis}(\alpha) \subseteq F\} \\ L(\mathcal{P}, F, \lozenge) & \{\alpha \in L(\mathcal{P}) : \textit{Vis}(\alpha) \cap F \neq \emptyset\} \\ L(\mathcal{P}, F, \lozenge \square) & \{\alpha \in L(\mathcal{P}) : \textit{Inf}(\alpha) \subseteq F\} \\ L(\mathcal{P}, F, \square \lozenge) & \{\alpha \in L(\mathcal{P}) : \textit{Inf}(\alpha) \cap F \neq \emptyset\} \\ & \{\alpha \in L(\mathcal{P}) : \exists i\alpha \in L(\mathcal{P}, F, \mathcal{R}_n) & L(\mathcal{P}, F_i, \square \lozenge) \cap L(\mathcal{P}, G_i, \lozenge \square)\} \end{array}$$



Automatic Verification —Discrete Case —Initial Definitions

nition 4 (Acceptance Condition)

P is $\Omega \in \{(F, \square), (F, \lozenge), (F, \lozenge \square), (F, \square \lozenge), (F, \mathcal{R}_n)\}$ where $F = \{(F_i, G_i)_{i=1}^n\}$ and F_i, F_i and G_i are certair of Q referred as the good states. The set of seques that are accepted accordig to Q is defined as follow

 $L(P, F, \Box)$ { $\alpha \in L(P) : V_{\mathfrak{S}}(\alpha) \subseteq L(P, F, \Diamond)$ } { $\alpha \in L(P) : V_{\mathfrak{S}}(\alpha) \cap L(P, F, \Diamond \Box)$ } { $\alpha \in L(P) : \inf(\alpha) \subseteq L(P, F, \Box \Diamond)$ } { $\alpha \in L(P) : \inf(\alpha) \cap \{\alpha \in L(P) : \exists i \alpha \in L(P) : \exists i \alpha$

- 1. α always remains in F
- 2. α eventually visits F
- 3. α eventually remains in F
- 4. α visits F infinitely often
- 5. α visits F_i infinitely often and eventually stays in G_i

Definition 5 (Controller Synthesis Problem)

For a plant \mathcal{P} and an acceptance condition Ω , the problem $\textbf{Synth}(\mathcal{P}, \Omega)$ is: Find a controller C such that $L_C(\mathcal{P}) \subseteq L(\mathcal{P}, \Omega)$ ot otherwise show that such a controller does not exists.

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Definition 5 (Controller Synthesis Problem)

For a plant P and an acceptance condition Ω , the problem P is: Find a controller C such that $L_C(P) \subseteq L$



Definition 6 (Controllable Predecessors)

Let $\mathcal{P} = (Q, \Sigma_c, \delta, q)$ be a plant and a set of states $P \subseteq Q$. The controllable predecessors of P is the set of states from which the controller can "force" the plant into P in one step:

$$\{q:\exists\sigma\in\Sigma_{c}$$
 , $\delta(q,\sigma)\subseteq P\}$

We define a function $\pi: 2^Q \longmapsto 2^Q$, mapping a set of states $P \subseteq Q$ into the set of its Controllable predecessors:

$$\pi(P) = \{q : \exists \sigma \in \Sigma_c \cdot \delta(q, \sigma) \subseteq P\}$$

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Definition 6 (Controllable Predece

Let $\mathcal{P} = (Q, \Sigma_c, \delta, q)$ be a plant and a

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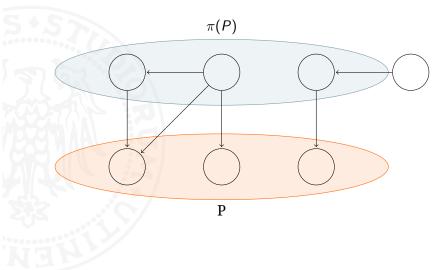
 $\{q: \exists \sigma \in \Sigma_c : \delta(q, \sigma) \subseteq P\}$

We define a function $\pi: 1^Q \longrightarrow 1^Q$, mapping a set of stat $P \subseteq Q$ into the set of its Controllable predecessors:

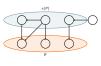
 $\pi(P) = \{q : \exists \sigma \in \Sigma_c . \delta(q, \sigma) \subseteq P\}$







Automatic Verification -Discrete Case -Controllable Predecessors



Theorem 1

For every $\Omega \in \{(F, \square), (F, \lozenge), (F, \lozenge \square), (F, \square \lozenge), (\mathcal{F}, \mathcal{R}_n)\}$, the problem **Synth**(\mathcal{P}, Ω) is solvable. Moreover, if (\mathcal{P}, Ω) is controllable then it is controllable by a simple controller.

For a plant $\mathcal{P} = (Q, \Sigma_c, \delta, q_0)$ and an acceptance condition Ω , we denote $W \subseteq Q$ as the set of winning states, namely, the set of states from which a controller can enforce good behaviors according to Ω .

Automatic Verification Discrete Case -Theorem

We can characterize this states by the following fixed-point expressions:

$$\square \ \nu W(F \cap \pi(W))$$

$$\Diamond \ \nu W(F \cup \pi(W))$$

$$\Diamond \Box \ \mu W \nu H \Big(\pi(H) \cap \big(F \cup \pi(W) \big) \Big)$$

$$\Box \Diamond \ \nu W \mu H \Big(\pi(H) \cup \big(F \cap \pi(W) \big) \Big)$$

$$\mathcal{R}_1 \ \mu W \bigg\{ \pi(W) \cap \nu Y \mu H.W \cup G \cap \Big(\pi(H) \cup \big(F \cap \pi(Y) \big) \Big) \bigg\}$$

Then the plant is controllable iff $q_0 \in W$

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We can characterize this states by the following fixed expression: $\Box \nu W(F \cap \pi(W))$ $\circ \nu W(F \cup \pi(W))$ $\circ \nu W(F \cup \pi(W))$ $\Box \nu \nu W_{B}H(\pi(H) \cap (F \cup \pi(W)))$ $\Box \nu \nu W_{B}H(\pi(H) \cup (F \cap \pi(W)))$ $\Re_{+} \mu W_{A}(W) \circ \nu \nu_{B}H W \cup G \cap (\pi(H) \cup (F \cap \pi(Y)))$ $\Re_{+} \mu W_{A}(W) \circ \nu \nu_{B}H W \cup G \cap (\pi(H) \cup (F \cap \pi(Y)))$

Then the plant is controllable iff on G W

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\nu greatest \mu least
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Let see in more details how this works. Consider the case ◊:

$$egin{aligned} &W_0 := \emptyset \ & W_0 := \emptyset \ & \text{for } i := 0, 1, \dots \ & ext{repeat} \end{aligned} \qquad egin{aligned} &W_1 := F \cup \pi(W_0) = F \cup \pi(W_0) = F \ & W_{i+1} := F \cup \pi(W_i) \end{aligned} \qquad egin{aligned} &W_2 := F \cup \pi(W_1) = F \cup \pi(F) \ & \text{until } W_{i+1} = W_i \end{aligned} \qquad \dots$$

finally:
$$W_n := F \cup \pi(W_{n-1}) = F \cup \pi(F \cup \pi(...(F \cup \pi(F))))$$

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Theorem

ee in more details how this works. Consider the case 0: $=\emptyset$ $W_1 := \emptyset$ $W_2 := \emptyset$ $i := 1, 1, \dots$ repeat $W_1 := F \cup \pi(W_1) = F \cup \pi(W_2)$ $W_2 := F \cup \pi(W_1) = F \cup \pi(F)$

 $W_{i+1} := F \cup \pi(W_i)$ $W_i := F \cup \pi(W_i) = F \cup \pi(F)$ until $W_{i+1} = W_i$...

finally: $W_a := F \cup \pi(W_{a-1}) = F \cup \pi(F \cup \pi(\cdots F \cup \pi(F)))$

In the process of calculating W_{i+1} , whenever we add a state q to W_i , there must be at least one action $\sigma \in \Sigma_c$ such that $\delta(q, \sigma) \subseteq W_i$.

So we define the controller at q as $C(q) = \sigma$.

When the process terminates, the controller is synthesized for all the winning states.

It can be seen that if the process fails, that is $q_0 \notin W$, then for every controller command there is a possibly bad consequence that will put the system outside F, and no controller, even an infinite state one, can prevent this.

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Automatic Verification └─Discrete Case └─Conclusions

In the process of calculating W_{i+1} , whenever we add a state q to W_i , there must be at least one action $\sigma \in \Sigma_c$ such that $\delta(q, \sigma) \subseteq W_i$. So we define the controller at σ as $C(\sigma) = \sigma$.

When the process terminates, the controller is synthesize

for all the winning states. It can be seen that if the process fails, that is $q_i \notin W$, then for every controller command there is a possibly bad consequence that will put the system outside F_i and no controller, even an infinite state one, can prevent that

Let T denote \mathbb{R}^+ and let $X = T^d$.

The elements of X are $x = (x_1, \dots, x_d)$ and the d-dimensional unit vector is $\mathbf{1} = (1, \dots, 1)$

Definition 7 (Reset functions)

Let F(X) denote the class of functions $f: X \mapsto X$ that can be written in the form $f(x_1, ..., f_d) = (f_1, ..., f_d)$ where each f_i is either x_i or 0.

Automatic Verification -Real Time Case -Initial Definitions

Let T denote \mathbb{R}^+ and let $X = T^d$. The elements of X are y = (y y) and the d-dimensional unit vector is 1 - (1, ..., 1)

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Definition 8 (*k polyhedral sets*)

Let k be a positive integer constant. We associate with k three subsets of 2^{X} :

- \triangleright \mathcal{H}_k : the set of half-spaces consisting of all sets having one of the following forms
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for some $\# \in \{<, \leq, >, \geq\}$ and $c \in \{0, \ldots, k\}$

- \blacktriangleright \mathcal{H}_k^{\cap} : the set of convex sets consisting of intersections of elements of \mathcal{H}_k
- \mathcal{H}_k^* : the set of k-polyhedral sets containing all sets obtained from \mathcal{H}_k via union intersection and complementation

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Let k be a positive integer constant. We associate with k
three subsets of 1 x :

- ► H_k: the set of half-spaces consisting of all sets having one of the following forms
- ∅ {x ∈ X : x,#c} {x ∈ X : x, -x,#c}
- {x ∈ X : x₁ − x₁#c} for some # ∈ {<, ≤, >, ≥} and c ∈ {1,..., k}
- H_i: the set of convex sets consisting of intersections elements of H_k
 - ► H_k: the set of k-polyhedral sets containing all sets obtained from H_k via union intersection and complementation

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- Q a finite set of discrete states
- ightharpoonup X a clock domain $X = (\mathbb{R}^+)^d$ for some d > 0
- \triangleright Σ an input alphabet (including a single environment action e)
- ▶ $I: Q \mapsto \mathcal{H}^{\cap}_{k}$ as the state invariant function
- $ightharpoonup R \subseteq Q \times \Sigma \times \mathcal{H}_{k}^{\cap} \times F(X) \times Q$ is a set of transition relations each of the form $\langle q, \sigma, g, f, q' \rangle$ where:
 - ightharpoonup q, q'inQ
 - $\sigma \in \Sigma$
 - $proof g \in \mathcal{H}^{\cap}_{k}$
 - $ightharpoonup f \in F(X)$

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A timed automaton is a tunle $T = (O \times \Sigma \mid R \Leftrightarrow)$ consisting

- Q a finite set of discrete states

- g ∈ H_k
 f ∈ F(X)

Definition 10 (Steps and Trajectories)

A step of (T) is a pair of configurations ((q,x),(q',x')) such that either:

- ▶ q = q' and for some $t \in T, x' = x + 1t, x \in I_q$ and $x' \in I_q$. In this case we say that (q', x') is a t-successor of (q, x) and that ((q, x), (q', x')) is a t-step.
- ► There is some $r = \langle q, \sigma, g, f, q' \rangle \in R$ such that $x \in g$ and x' = f(x). In this case we say that (q', x') is a σ -successor of (q, x) and that ((q, x), (q', x')) is a σ -step

A trajectory of \mathcal{T} is a sequence $\beta = (q[0], x[0]), (q[1], x[1]), \ldots$ of configurations such that for every i, ((q[i], x[i]), (q[i+1], x[i+1])) is a step.



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Definition 10 (Steps and Trajectories)

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- In this case we say that (q', x') is a t-successor and that ((q, x), (q', x')) is a t-step. There is some $t = (q, \sigma, g, \ell, q') \in R$ such that $x \in R$
- There is some r = (q, σ, g, f, q') ∈ R such that x ∈ g and x' = f(x). In this case we say that (q', x') is a σ-successo of (q, x) and that ((q, x), (q', x')) is a σ-step

A trajectory of T is a sequence $\beta = (q[1], x[1]), (q[1], x[1]), ...$ of configurations such that for every i, ((q[i], x[i]), (q[i+1], x[i+1])) is a step.

Definition 11 (Real time Controller)

A simple real time controller is a function $C: Q \times X \mapsto \Sigma_c \cup \bot$

According to this function the controller chooses at any configuration (q, x) whether to issue some enabled transition σ or to do nothing and let time go by. We denote by Σ_c^{\perp} the range of controller commands $\Sigma_c \cup \bot$. We also require that the controller is k-polyhedral, i.e., for every $\sigma \in \Sigma_c^{\perp}$, $C^{-1}(\sigma)$ is a k-polyhedral set.

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Definition 11 (Real time Controller)

A simple real time controller is a function $C: Q \times X$

According to this function the controller chooses at any configuration (q, x) whether to issue some enabled transition or or to do nothing and let time go by. We denote by $\Sigma_{\varepsilon}^{\perp}$ the range of controller commands $\Sigma_{\varepsilon} \cup \bot$. We also require that the controller is k-polyhedral, i.e., for every $\sigma \in \Sigma_{\varepsilon}^{\perp}$, $C^{-1}(\sigma)$ is a k-nolyhedral yet Given a simple controller C, a pair ((q,x),(q',x')) of config*urations is a C-step if it is either:*

- ► an e step
- ightharpoonup a σ step such that $C(q,x) = \sigma \in \Sigma_c$
- ightharpoonup a t- step for some $t\in T$ such that for every t', $t' \in [0, t), C(q, x + 1t') = \perp$

A C-trajectory is a trajectory consisting of C-steps. We denote the set of *C*-trajectories of \mathcal{T} by $L_{\mathcal{C}}(\mathcal{T})$.

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Definition 13 (Real time Controller Synthesis)

Given a timed automaton \mathcal{T} an a acceptance condition Ω , the problem RT-Synth (\mathcal{T}, Ω) is: Construct a real-time controller C such that $L_C(\mathcal{T}) \subseteq L(\mathcal{T}, \Omega)$

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efinition 13 (Real time Controller Synthesis) iven a timed automaton T an a acceptance condition roblem RT-Synth(T, Ω) is: Construct a real-time consuch that $L_C(T) \subseteq L(T, \Omega)$



In order to tackle the real time controller synthesis problem we introduce the following definitions:

Definition 14 ((t, σ) – successor)

For $t \in T$ and $\sigma \in \Sigma$, the configuration (q', x') is defined to be a (t, σ) – successor of the configuration (q, x) if there exists an intermediate configuration (\hat{q}, \hat{x}) such that (\hat{q}, \hat{x}) is a t – successor of (q, x) and (q', x') is a σ – successor of (\hat{q}, \hat{x}) .

Then we define a function $\delta: (Q \times X) \times (T \times \Sigma_c^{\perp}) \mapsto 2^{Q \times X}$ where $\delta((q, x), (t, \sigma))$ stands for all the possible consequences of the controller attempting to issue the command $\sigma \in \Sigma_c^{\perp}$ after waiting t time units starting at configuration (q, x)



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of the controller attempting to issue the command $\sigma \in \Sigma_{\sigma}^{\perp}$

Note that this covers the case of (q', x') being simply a σ – successor of (q, x) by viewing it as a $(0, \sigma)$ – successor of (q, x).

Definition 15 (Extended Transition Function)

For every $t \in T$ and $\sigma in \Sigma_c$, the set $\delta((q, x), (t, \sigma))$ consists of all the configurations (q', x') such that:

- \triangleright (q', x') is a (t, σ) successor of (q, x)
- (q', x') is a (t, e) successor of (q, x) for some $t' \in [0, t]$



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Definition 15 (Extended Transition Function) For every $t \in T$ and $\sigma in \Sigma_{t}$, the set $\delta((q, x), (t, \sigma))$ consist all the configurations (q', x') such that: (q', x') is a (t, σ) - successor of (q, x)(q', x') is (t, σ) - successor of (q, x) for some $t' \in [1, T]$

This definition covers successor configurations that are obtained in one of two possible ways:

some configurations result from the plant waiting patiently at state q for t time units, and then taking a σ -labeled transition according to the controller recommendation,

the second possibility is of configurations obtained by taking an environment transition at any time $t' \le t$

This is in fact the crucial new feature of real-time games - there are no turns and the adversary need not wait for the player's next move.

Definition 16 (Controllable Predecessors)

The controllable predecessors function $\pi: 2^Q \times 2^X \mapsto 2^Q \times 2^X$ is defined for every $K \subseteq Q \times X$ by

$$\pi(K) = \{(q, x) : \exists t \in T \exists \sigma \in \Sigma_c \ \delta((q, x), (t, \sigma)) \subseteq K\}$$



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Definition 16 (Controllable Predecessors)

The controllable predecessors function $\pi: \mathbb{T}^Q \times \mathbb{T}^K \mapsto \mathbb{T}^Q$ is defined for every $K \subseteq Q \times X$ by $\pi(K) = \{(q, x): \exists t \in T \exists \sigma \in \Sigma_c \ \delta((q, x), (t, \sigma)) \subseteq K\}$

As in the discrete case, we define a predecessor function that indicates the configurations from which the controller can force the automaton into a given set of configurations

Theorem 2 (Control Synthesis for Timed ystems)

Given a timed automaton \mathcal{T} and an acceptance condition

$$\{(F,\Box),(F,\Diamond),(F,\Diamond\Box),(F,\Box\Diamond),(\mathcal{F},\mathcal{R}_n)\}$$

the problem **RT-Synth**(\mathcal{T}, Ω) is solvable

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Theorem 2 (Control Synthesis for Timed

 $\{(F, \Box), (F, \Diamond), (F, \Diamond \Box), (F, \Box \Diamond), (F, \mathcal{R}_{\alpha})\}$ the problem RT-Synth (T, Ω) is solvable



Sketch of Proof

We have just shown that $2^Q \times \mathcal{H}_{k}^*$ is closed under π .

Any of the iterative processes for the fixed point equations (1) – (5) starts with an element of $2^Q \times \mathcal{H}_{\nu}^*$.

For example, the iteration for \Diamond starts with $W_0 = Q \times F$.

Each iteration consists of applying Boolean set-theoretic operations and the predecessor operation, which implies that every W_i is also an element of $2^Q \times \mathcal{H}_k^*$ - a finite set.

Thus, by monotonicity, a fixed point is eventually reached.



Sketch of Proof We have just shown that $1^Q \times H^*$ is closed under π

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Any of the iterative processes for the fixed point equation (1) - (5) starts with an element of 1 Q × H2. For example, the iteration for \Diamond starts with $W_1 = Q \times F$ Each iteration consists of applying Boolean set-theoretic operations and the predecessor operation, which implies that every W: is also an element of 1 Q × H1 - a finite set.

Thus, by monotonicity a fixed point is eventually reached

The strategy is extracted in a similar manner as in the discrete case. When ever a configuration (q, x) is added to W, it is due to one or more pairs of the form $([t_1, t_2], \sigma)$ indicating that within any $t, t_1 < t < t_2$ issuing σ after waiting t will lead to a winning position. Hence by letting $C(q,x) = \perp$ when $t_1 > 0$ and $C(q,x) = \sigma$ when $t_1 = 0$ we obtain a k-polyhedral controller.

Citations



Automatic Verification —Citations

