

Reason To use :

- If a nuisance variable cannot be controlled, then we need to block it. In this case, we will use blocking design.
- If each treatment in blocking design contains at least one unit, then we say we have a complete blocking design.
- If we have setup blocking policy and then randomly assign experiment unit to each treatments, then we have randomized complete blocking design.

Model:

- The model will similar to factorial design with no interaction term because blocking is not real factor or interest.

$$\rightarrow y_{ijk} = \mu_1 + \alpha_j + \beta_k + \epsilon_{ijk} ; \epsilon_{ijk} \stackrel{iid}{\sim} N(0, \sigma^2)$$

y_{ijk} := represents the i th response value of j th level of factor A and k th group of blocking.

μ_1 := represents the grand mean.

α_j := represents the main effect of j th level of factor A.

β_k := represents the blocking effect of k th level of blocking.

ϵ_{ijk} := represents the random error.

Note: RCB is two-ways ANOVA without interaction.

Analysis:

- If we find out the model of RCB have related small MSE_{RCB} than MSE without RCB, then we want to choose RCB model.

This is not sure. Need to ask.

$$\hookrightarrow RE(MSE_{CR}, MSE_{RCB}) = \frac{MSE_{CR}}{MSE_{RCB}}$$

↑ There is a formula to estimate this without using MSE_{CR} .

Question:

When do we choose RCB?

↳ Interpretation: RCB design is more efficiency than CR design in reducing the experimental error.

ANOVA :

	df	SS	MS	F _{obs}
Treatment	a-1	SSA	$\frac{SSA}{a-1}$	$\frac{MSA}{MSE}$
Block	B-1	SSB	$\frac{SSB}{B-1}$	
Error	N-a-b+1	SSE	$\frac{SSE}{N-a-b+1}$	
Total	N-1	SST	$\frac{SST}{N-1}$	

$$SSA = \sum_{k=1}^b \sum_{j=1}^a n_{jk} (\bar{y}_{.j} - \bar{y}_{..})^2$$

$\bar{y}_{.j}$:= represents the jth row mean.

$$SSB = \sum_{j=1}^a \sum_{k=1}^b n_{jk} (\bar{y}_{0k} - \bar{y}_{..})^2$$

\bar{y}_{0k} := represents the kth column mean.

$$SST = \sum_{j=1}^a \sum_{k=1}^b \sum_{i=1}^{n_{jk}} (y_{ijk} - \bar{y}_{..})^2$$

$$SSE = SST - SSA - SSB$$