# **Statistics Homework 06**

B08705034 施芊羽 資管二

# 81

## **Chapter 7**

```
In [1]: import seaborn as sns
   import pandas as pd
   import numpy as np
   import scipy.stats as stats
   import statsmodels.api as sm
   import statsmodels.stats.api as sms
   import statsmodels.formula.api as smf
   import math as math
   import statistics
   from matplotlib import pyplot as plt
   %matplotlib inline
   from numpy import random
   from scipy.stats import binom
   plt.rcParams["figure.dpi"] = 100
```



Suppose P(n) represents the probability of a university graduate is offered n job(s) while n is from 0 to 3.(P(0) stands for no jobs is received.)

A graduate is offered fewer than two jobs: P(0) + P(1) = 5% + 43% = 48%

b.

A graduate is offered more than one job:P(2) + P(3) = 31% + 21% = 52%



	x	P(x)
0	0	0.22
1	5	0.29
2	10	0.12

Processing math: 100%

```
<sup>⊥</sup> 3 15 0.09
```

- 4 20 0.08
- **5** 25 0.05
- 6 30 0.04
- **7** 40 0.04
- **8** 50 0.03
- **9** 75 0.03
- **10** 100 0.01

a.

```
In [12]: P = 0
    for i in range(df_c07_27["x"].shape[0]):
        if(df_c07_27["x"][i] >= 20):
            P = P + df_c07_27["P(x)"][i]

print("P(X >= 20) = ", P)

P(X >= 20) = 0.28
```

 $P(X \ge 20) = .08 + .05 + .04 + .04 + .03 + .03 + .01 = .28$ 

b.

```
In [3]: P = 0
    for i in range(df_c07_27["x"].shape[0]):
        if(df_c07_27["x"][i] == 60):
            P = df_c07_27["P(x)"][i]
            break;

print("P(X = 20) = ", P)

P(X >= 20) = 0
```

There's no x = 60 in the given data, so P(X = 60) = 0.

C.

P(X > 50) = .03 + .01 = .04

d.

There's no probability of X > 100 in the given data, so P(X > 100) = 0



```
In [25]: df_c07_35 = pd.read_excel("Xr07-35.xlsx")
    display(df_c07_35)

mean = (df_c07_35["x"] * df_c07_35["P(x)"]).sum()
    var = (pow((df_c07_35["x"] - mean), 2) * df_c07_35["P(x)"]).sum()
    std = np.sqrt(var)

print("Mean = ", mean)
    print("Standard Deviation = ", std)
```

```
x P(x)

0 0 0.10

1 1 0.20

2 2 0.25

3 3 0.25

4 4 0.20

Mean = 2.25

Standard Deviation = 1.2599603168354152
```

The mean of the given data is 2.25 customers and the standard deviation is 1.26 customers(round it to the nearest hundredth).



Y\X	0	1
1	0.04	0.16
2	0.08	0.32
3	0.08	0.32



The data on the textbook is wrong (the sum of the probability on the table  $\neq$  1). Therefore, the following data are all from the given excel dataset "Xr07-59.xlsx"

	Unnamed: 0	Carbon Monoxide Detector: 0	Carbon Monoxide Detector: 1	Carbon Monoxide Detector: 2
0	Smoke Detector: 0	0.42	0.03	0.00
1	Smoke Detector: 1	0.15	0.07	0.01
2	Smoke Detector: 2	0.06	0.10	0.05
3	Smoke Detector: 3	0.05	0.04	0.02

a.

The proportion of homes have no carbon monoxide detectors and two smoke detectors is 0.06

The proportion of homes have no carbon monoxide detectors and two smoke detectors is 0.06.

b.

The proportion of homes have two carbon monoxide detectors and no smoke detectors is  $0.0\,$ 

The proportion of homes have two carbon monoxide detectors and no smoke detectors is 0.

C.

```
In [20]: p = 0

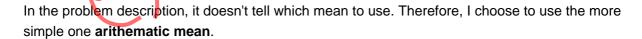
for i in range(1 , 4, 1):
    p = p + df_c07_59["Carbon Monoxide Detector: 1"][i]
    p = p + df_c07_59["Carbon Monoxide Detector: 2"][i]

print("The proportion of homes have at least one carbon monoxide detector and at least one smoke detector is ", p)
```

The proportion of homes have at least one carbon monoxide detector and a t least one smoke detector is 0.29

The proportion of homes have at least one carbon monoxide detector and at least one smoke detector is .07 + .10 + .04 + .01 + .05 + .02 = .29

7.79



```
In [2]: df_c07_79 = pd.read_excel("Xr07-NYSE.xlsx")

def geomean(rate):
    r = rate
    geo_m = np.round(math.exp(np.log(r).mean()), 6)
    return geo_m
```

```
In [3]: ## Mean of the four stocks
        \#GE = geomean(df_c07_79["GE"] + 1) - 1
        \#JNJ = geomean(df_c07_79["JNJ"] + 1) - 1
        \#MCD = geomean(df_c07_79["MCD"] + 1) - 1
        \#MRK = geomean(df_c07_79["MRK"] + 1) - 1
        GE = df_c07_79["GE"].mean()
        JNJ = df c07 79["JNJ"].mean()
        MCD = df_c07_79["MCD"].mean()
        MRK = df_c07_79["MRK"].mean()
        ## Calculation for variation
        var_GE = statistics.variance(df_c07_79["GE"])
        var_JNJ = statistics.variance(df_c07_79["JNJ"])
        var_MCD = statistics.variance(df_c07_79["MCD"])
        var_MRK = statistics.variance(df_c07_79["MRK"])
        ## Display the statistics in a dataframe
        df_c07_79_stat = pd.DataFrame()
        df_c07_79_stat["GE"] = [GE, var_GE]
        df_c07_79_stat["JNJ"] = [JNJ, var_JNJ]
        df_c07_79_stat["MCD"] = [MCD, var_MCD]
        df c07 79 stat["MRK"] = [MRK, var MRK]
        ## Calculation for the covariance
        cov_mat1 = np.cov(df_c07_79[['GE', 'JNJ']].values rowvar = False)
        cov_mat2 = np.cov(df_c07_79[['GE', 'MCD']].values, rowvar = False)
        cov_mat3 = np.cov(df_c07_79[['GE', 'MRK']].values, rowvar = False)
        cov_mat4 = np.cov(df_c07_79[['MRK', 'JNJ']].values, rowvar
        cov_mat5 = np.cov(df_c07_79[['MCD', 'JNJ']].values, rowvar = False)
        cov_mat6 = np.cov(df_c07_79[['MRK', 'MCD']].values, rowvar = False)
        cov_ge_jnj = cov_mat1[0][1]
        cov_ge_mcd = cov_mat2[0][1]
        cov\_ge\_mrk = cov\_mat3[0][1]
        cov_mrk_jnj = cov_mat4[0][1]
        cov_mcd_jnj = cov_mat5[0][1]
        cov_mrk_mcd = cov_mat6[0][1]
```

display(df\_c07\_79\_stat)

	GE	JNJ	MCD	MRK
0	0.010524	0.012687	0.012042	0.011273
1	0.003090	0.001388	0.001326	0.002157

a.

Mean of GE: 25% + JNJ: 25% + MCD: 25% + MRK: 25% = 0.011631337567666475 Standard Deviation of GE: 25% + JNJ: 25% + MCD: 25% + MRK: 25% = 0.0309 64874957958792

b.

Mean of GE: 5% + JNJ: 30% + MCD: 40% + MRK: 25% = 0.011967230262297799 Standard Deviation of GE: 5% + JNJ: 30% + MCD: 40% + MRK: 25% = 0.03096 4874957958792

C.

```
In [9]: meanC = GE * 0.1 + JNJ * 0.5 + MCD * 0.3 + MRK * 0.1
    stdC = np.sqrt(var_GE * 0.1 * 0.1 + var_JNJ * 0.5 * 0.5 + var_MCD * 0.3
    * 0.3 + var_MRK * 0.1 * 0.1 +
        2 * 0.1 * 0.5 * cov_ge_jnj + 2 * 0.1 * 0.3 * cov_ge_mcd + 2 * 0.1 *
        0.1 * cov_ge_mrk +
        2 * 0.3 * 0.5 * cov_mrk_jnj + 2 * 0.1 * 0.5 * cov_mcd_jnj + 2 * 0.1
        * 0.3 * cov_mrk_mcd)

print("Mean of GE: 10% + JNJ: 50% + MCD: 30% + MRK: 10% = ", meanC)
    print("Standard Deviation of GE: 10% + JNJ: 50% + MCD: 30% + MRK: 10% =
", stdC)
```



Mean of GE: 10% + JNJ: 50% + MCD: 30% + MRK: 10% = 0.012135638250193525 Standard Deviation of GE: 10% + JNJ: 50% + MCD: 30% + MRK: 10% = 0.0322 5932359442462

d.

A gambler will choose the c. portfolio since it has the highest mean of return rate.

e.

```
In [10]: print("Covariance of GE: 25% + JNJ: 25% + MCD: 25% + MRK: 25% = ", stdA/meanA)
    print("Covariance of GE: 5% + JNJ: 30% + MCD: 40% + MRK: 25% = ", stdB/meanB)
    print("Covariance of GE: 10% + JNJ: 50% + MCD: 30% + MRK: 10% = ", stdC/meanC)

    Covariance of GE: 25% + JNJ: 25% + MCD: 25% + MRK: 25% = 2.838510897632 9265
    Covariance of GE: 5% + JNJ: 30% + MCD: 40% + MRK: 25% = 2.5874721451221 83
    Covariance of GE: 10% + JNJ: 50% + MCD: 30% + MRK: 10% = 2.658230488529 121
```

A risk-averse investor will choose **b.** is because that even though its mean of return rate is lowest of all, its covariance is the smallest among all. As a risk-averse investor, he(or she) will rather choose the one that's stable while still profitable.

7.89

In the problem description, it doesn't tell which mean to use. Therefore, I choose to use the more simple one **arithematic mean**.

```
In [12]: df_c07_89 = pd.read_excel("Xr07-TSE.xlsx")
In [13]: ## Mean of the four stocks
         BMO = df_c07_89["BMO"].mean()
         MG = df_c07_89["MG"].mean()
         POW = df c07 89["POW"].mean()
         RCLB = df_c07_89["RCL.B"].mean()
         ## Calculation for variation
         var_BMO = statistics.variance(df_c07_89["BMO"])
         var_MG = statistics.variance(df_c07_89["MG"])
         var_POW = statistics.variance(df_c07_89["POW"])
         var_RCLB = statistics.variance(df_c07_89["RCL.B"])
         ## Display the statistics in a dataframe
         df_c07_89_stat = pd.DataFrame()
         df_c07_89_stat["BMO"] = [BMO, var_BMO]
         df_c07_89_stat["MG"] = [MG, var_MG]
         df_c07_89_stat["POW"] = [POW, var_POW]
         df_c07_89_stat["RCL.B"] = [RCLB, var_RCLB]
```

```
## Calculation for the covariance
cov_mat1 = np.cov(df_c07_89[['BMO', 'MG']].values, rowvar = False)
cov_mat2 = np.cov(df_c07_89[['BMO', 'POW']].values, rowvar = False)
cov_mat3 = np.cov(df_c07_89[['BMO', 'RCL.B']].values, rowvar = False)
cov_mat4 = np.cov(df_c07_89[['RCL.B', 'MG']].values, rowvar = False)
cov_mat5 = np.cov(df_c07_89[['POW', 'MG']].values, rowvar = False)
cov_mat6 = np.cov(df_c07_89[['RCL.B', 'POW']].values, rowvar = False)

cov_bmo_mg = cov_mat1[0][1]
cov_bmo_pow = cov_mat3[0][1]
cov_bmo_rclb = cov_mat3[0][1]
cov_rclb_mg = cov_mat4[0][1]
cov_rclb_pow = cov_mat5[0][1]
display(df_c07_89_stat)
```

	вмо	MG	POW	RCL.B
0	0.008698	0.013680	0.006309	0.009613
1	0.001201	0.006967	0.002689	0.002274

### a.

, n

Mean of BMO: 25% + MG: 25% + POW: 25% + RCL.B: 25% = 0.0095747512462921 86 Standard Deviation of BMO: 25% + MG: 25% + POW: 25% + RCL.B: 25% = 0.03 527484125644567

### b.

```
In [16]: meanB = BMO * 0.2 + MG * 0.6 + POW * 0.1 + RCLB * 0.1
    stdB = np.sqrt(var_BMO * 0.2 * 0.2 + var_MG * 0.6 * 0.6 + var_POW * 0.1
    * 0.1 + var_RCLB * 0.1 * 0.1 +
        2 * 0.2 * 0.6 * cov_bmo_mg + 2 * 0.2 * 0.1 * cov_bmo_pow + 2 * 0.2
    * 0.1 * cov_bmo_rclb + 2 * 0.1 * 0.6 * cov_rclb_mg +
        2 * 0.1 * 0.6 * cov_pow_mg + 2 * 0.1 * 0.1 * cov_rclb_pow)

print("Mean of BMO: 20% + MG: 60% + POW: 10% + RCL.B: 10% = ", meanB)
    print("Standard Deviation of BMO: 20% + MG: 60% + POW: 10% + RCL.B: 10%
    = ", stdB)
Mean of BMO: 20% + MG: 60% + POW: 10% + RCL.B: 10% = 0.0115394531058301
```

Standard Deviation of BMO: 20% + MG: 60% + POW: 10% + RCL.B: 10% = \ 0/05

40755346331138

C.

```
In [17]: meanC = BMO * 0.1 + MG * 0.2 + POW * 0.3 + RCLB * 0.4
    stdC = np.sqrt(var_BMO * 0.1 * 0.1 + var_MG * 0.2 * 0.2 + var_POW * 0.3
    * 0.3 + var_RCLB * 0.4 * 0.4 +
        2 * 0.1 * 0.2 * cov_bmo_mg + 2 * 0.1 * 0.3 * cov_bmo_pow + 2 * 0.1
    * 0.4 * cov_bmo_rclb + 2 * 0.4 * 0.2 * cov_rclb_mg +
        2 * 0.3 * 0.2 * cov_pow_mg + 2 * 0.4 * 0.3 * cov_rclb_pow)

print("Mean of BMO: 10% + MG: 20% + POW: 30% + RCL.B: 40% = ", meanC)
    print("Standard Deviation of BMO: 10% + MG: 20% + POW: 30% + RCL.B: 40%
    = ", stdC)
```



Mean of BMO: 10% + MG: 20% + POW: 30% + RCL.B: 40% = 0.0093434869878015 54 Standard Deviation of BMO: 10% + MG: 20% + POW: 30% + RCL.B: 40% = 0.03 600705443257263

d.

A gambler will choose the **b.** portfolio since it has the highest mean of return rate.

e.

```
In [18]: print("Covariance of BMO: 25% + MG: 25% + POW: 25% + RCL.B: 25% = ", std
A/meanA)
print("Covariance of BMO: 20% + MG: 60% + POW: 10% + RCL.B: 10% = ", std
B/meanB)
print("Covariance of BMO: 10% + MG: 20% + POW: 30% + RCL.B: 40% = ", std
C/meanC)

Covariance of BMO: 25% + MG: 25% + POW: 25% + RCL.B: 25% = 3.6841522405
196505
Covariance of BMO: 20% + MG: 60% + POW: 10% + RCL.B: 10% = 4.6861436271
87393
Covariance of BMO: 10% + MG: 20% + POW: 30% + RCL.B: 40% = 3.8537062747
111284
```

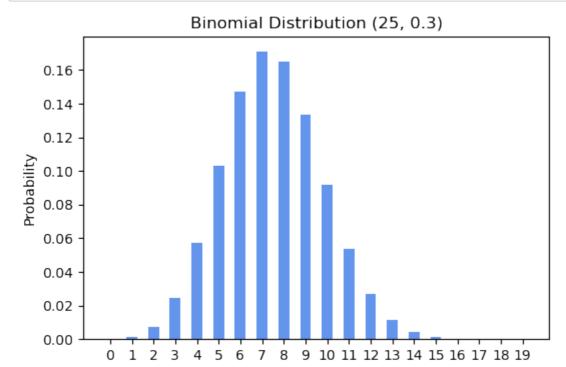
A risk-averse investor will choose **a.** is because that even though its mean of return rate is not the highest, its covariance is the smallest of the three. As a risk-averse investor, he(or she) will rather choose the one that's stable while profitable.

7.109

All answers of this problem are rounded to the nearest thousandth

```
In [20]: def factor(n):
    ans = 1
    for i in range(1 , n + 1):
        ans = ans * i
    return ans
```

```
x = np.arange(20)
hh = stats.binom(25, 0.3)
y = hh.pmf(x)
fig_hh, ax_hh = plt.subplots()
rect_hh = ax_hh.bar(x, y, width=0.5, bottom=None, align='center', color=
'cornflowerblue')
plt.ylabel('Probability')
plt.title('Binomial Distribution (25, 0.3)')
plt.xticks(x)
plt.show()
```



### a.

```
In [47]: p = 0
    for i in range(11):
        p = p + np.power(0.3 , i) * np.power((1 - 0.3) , 25 - i) * factor(25
        ) /factor(i)/factor(25 - i)

    print("The probability that 10 or fewer customers chose the leading bran d is ", p)
```

The probability that 10 or fewer customers chose the leading brand is 0.9021999888782667

The probability that 10 or fewer customers chose the leading brand is  $\sum_{10i=1}^{25!i!(25-i)!}(0.3)^i(1-0.3)^{25-i} \qquad 0.902.$ 

### b.

```
In [49]: p = 0
    for i in range(11, 26):
        p = p + np.power(0.3 , i) * np.power((1 - 0.3) , 25 - i) * factor(25
        ) /factor(i)/factor(25 - i)
```

```
print("The probability that 11 or more customers chose the leading bra
nd is", p)
```

The probability that 11 or more customers chose the leading brand is 0 .09780001112173187

The probability that 11 or more customers chose the leading brand is  $\sum_{25i=11}^{25!i!(25-i)!}(0.3)^{i}(1-0.3)^{25-i} \quad 0.098.$ 

C.

```
In [21]: p = 0
    p = p + np.power(0.3 , 10) * np.power((1 - 0.3) , 25 - 10) * factor(25)
    /factor(10)/factor(25 - 10)
    print("The probability that 10 customers chose the leading brand is", p)
```

The probability that 10 customers chose the leading brand is 0.091636012 38321353

The probability that 10 customers chose the leading brand is  $25!10!(25-10)!(0.3)^{1}0(1-0.3)^{(25-10)}$  0.0916



All answers of this problem are round to the nearest thousandth

```
In [119]: x = np.arange(100)
hh = stats.binom(100, 0.53)
y = hh.pmf(x)
fig_hh, ax_hh = plt.subplots()
rect_hh = ax_hh.bar(x, y, width=0.5, bottom=None, align='center', color=
'cornflowerblue')
plt.ylabel('Probability')
plt.title('Binomial Distribution (100, 0.53)')
plt.xticks(np.arange(0, 100, 5), np.arange(0, 100, 5), fontsize=10)
plt.show()
```

# 0.08 - 0.07 - 0.06 - 0.05 - 0.03 - 0.02 - 0.01 - 0.01 - 0.01 - 0.01 - 0.05 - 0.01 - 0.01 - 0.01 - 0.05 - 0.01 - 0.01 - 0.01 - 0.01 - 0.01 - 0.02 - 0.01 - 0.01 - 0.02 - 0.01 - 0.02 - 0.01 - 0.02 - 0.01 - 0.02 - 0.01 - 0.02 - 0.01 - 0.02 - 0.01 - 0.02 - 0.01 - 0.02 - 0.01 - 0.02 - 0.01 - 0.02 - 0.01 - 0.02 - 0.01 - 0.02 - 0.01 - 0.02 - 0.01 - 0.02 - 0.01 - 0.02 - 0.01 - 0.02 - 0.01 - 0.02 - 0.01 - 0.02 - 0.02 - 0.01 - 0.02 - 0.

a.

0.00

```
In [57]: p = 0
    for i in range(51, 101):
        p = p + np.power(0.53 , i) * np.power((1 - 0.53) , 100 - i) * facto
        r(100) /factor(i)/factor(100 - i)

    print("The probability that more than half say that Congress is doing a
    poor or bad job is", p)
```

The probability that more than half say that Congress is doing a poor or bad job is 0.6921991139282937

5 10 15 20 25 30 35 40 45 50 55 60 65 70 75 80 85 90 95

The probability that more than half say that Congress is doing a poor or bad job is  $\sum_{100i=51}^{100!i!(100-i)!(0.53)}i(1-0.53)^{(100-i)} \qquad 0.692$ 

b.

```
In [58]: p = 0
    for i in range(61, 101):
        p = p + np.power(0.53 , i) * np.power((1 - 0.53) , 100 - i) * facto
        r(100) /factor(i)/factor(100 - i)

    print("The probability that more than 60% say that Congress is doing a p
        oor or bad job is", p)
```

The probability that more than 60% say that Congress is doing a poor or bad job is 0.06592297187070088

The probability that more than 60% say that Congress is doing a poor or bad job is  $\Sigma_{100i=61}^{100!i!(100-i)!(0.53)^{i}(1-0.53)^{(100-i)}} \quad 0.066$ 

C.

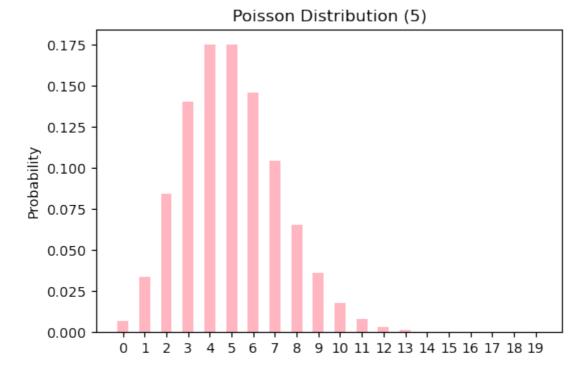
Since it's a Binomial Distribution, we can know that the expected number of American adults in the sample would say that Congress is doing a poor or bad job is np while n represents for the number of trials and p represents the succeess rate(in this case, is that 53% believed that Congress is doing a poor or bad job). Hence the expected number of American adults in the sample would say that Congress is doing a poor or bad job is  $100 \times 53\% = 53$ .

Therefore, it's expected that 53 adults out of the 100 will say that Congress is doing a poor or bad job.

7.133

All the answers to this quesion are rounded off to the 6th decimal place.

```
In [121]: x = np.arange(20)
    pp = stats.poisson(5)
    y = pp.pmf(x)
    fig_pp, ax_pp = plt.subplots()
    rect_pp = ax_pp.bar(x, y, width=0.5, bottom=None, align='center', color=
    'lightpink')
    plt.ylabel('Probability')
    plt.title('Poisson Distribution (5)')
    plt.xticks(x)
    plt.show()
```



a.

```
In [61]: pp = stats.poisson(5)
  print("p(mu = 5,", "x>=", 10, ")=", 1 - pp.cdf(9))
  p(mu = 5, x>= 10 )= 0.03182805730620486
```

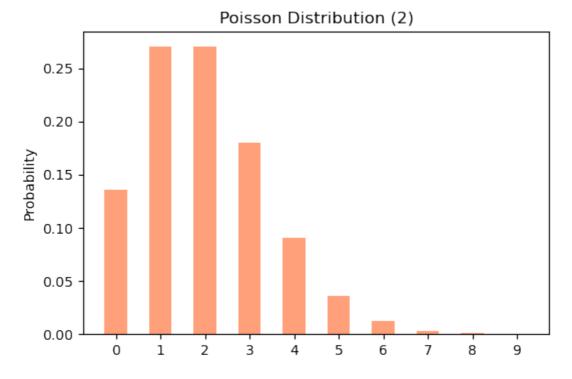
The probability that the site gets 10 or more hits in a week is 0.031828 after using solving it through the poisson functions in python.

b.

The probability that the site gets 20 or more hits in two weeks is 0.003454 after using solving it through the poisson functions in python.



All the answers to this quesion are rounded off to the 6th decimal place.



a.

```
In [70]: pp = stats.poisson(2)
print("p(mu = 2,", "x = ", 0, ")=", pp.pmf(0))
```

```
p(mu = 2, x = 0) = 0.1353352832366127
```

The probability that a golfer loses no golf balls is 0.135335.

b.

In the description, I don't know what's the meaning of "A golfer **loses 4 or more no golf balls**"; therefore, I predicted that the 'no' is accidentally typed. Hence, I answered this question with the thinking that the problem is asking "A golfer **loses 4 or more golf balls**".

The probability that a golfer **loses 4 or more golf balls** is 0.142877.

C.

The probability that a golfer loses 2 or fewer golf balls is 0.676676.