

Calculus II Quiz 5

110/05/31

請在空白紙上依序寫出各題 3 個答案, 計算過程請另紙處理、**不要**寫在答案紙上。

每人限交 A4 大小答案紙一頁, 右上角請務必寫上學號姓名。

((a)寫出可以真正算出的 iterated integral(含各個變數的上下限), 化簡為一個變數的積分寫在(b), 再將整理後的答案寫在(c))

1. Find volume V of the solid lying inside the cylinder $x^2 + 4y^2 = 4$, above the xy -plane and below the plane $z = 2 + x$; $V = \underline{(1a)} = \underline{(1b)} = \underline{(1c)}$.

2. Find surface area A of paraboloid $z = 1 - x^2 - y^2$ in the first octant;
 $A = \underline{(2a)} = \underline{(2b)} = \underline{(2c)}$.

3. Find volume V of the solid enclosed by the cone $z = \sqrt{3(x^2 + y^2)}$ and sphere $x^2 + y^2 + z^2 = 1$; $V = \underline{(3a)} = \underline{(3b)} = \underline{(3c)}$.

4. $\int_0^2 \int_0^{\sqrt{2x-x^2}} x \, dydx = \underline{(4a)} = \underline{(4b)} = \underline{(4c)}$.

5. $\iiint_T \frac{1}{\sqrt{x^2 + y^2}} \, dV = \underline{(5a)} = \underline{(5b)} = \underline{(5c)}$, $T: 0 \leq x \leq \sqrt{9 - y^2}, 0 \leq y \leq 3, 0 \leq z \leq \sqrt{9 - (x^2 + y^2)}$.

6. $\int_0^1 \int_{\sqrt{x}}^1 \sin\left(\frac{y^3 + 1}{2}\right) \, dydx = \underline{(6a)} = \underline{(6b)} = \underline{(6c)}$.

7. $\iint_{\Omega} e^{x^2} \, dA = \underline{(7a)} = \underline{(7b)} = \underline{(7c)}$, Ω is the bounded region bounded by x -axis, $2y = x, x = 2$.