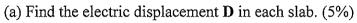
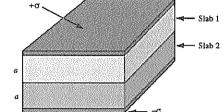
## 2018 Fall PHYS2310 電磁學 (Electromagnetism) Midterm [Griffiths Chs. 4-7.1] 2019/01/10, 10:10am - 12:00am, 教師:張存續

(double sides)

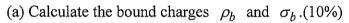
1. The space between the planes of a parallel-plate capacitor is filled with two slabs of linear dielectric material. Each slab has thickness a, so the total distance between the plates is 2a. Slab 1 has a dielectric constant of 9, and slab 2 has a dielectric constant of 4. The free charge density on the top plate is  $\sigma$  and on the bottom plate  $-\sigma$ .



- (b) Find the polarization P in each slab. (5%)
- (c) Find the potential difference between the metal plates. (5%)
- (d) Find the location and amount of all bound charges (  $\rho_b$  and  $\sigma_b$  ). (5%)



2. A sphere of radius R carries a polarization  $P(\mathbf{r}) = k\hat{\mathbf{z}}$ , where k is a constant and  $\hat{\mathbf{z}}$  is the unit vector.



(b) Find the electric potential and field inside the sphere. (10%)

[Hint: 
$$V = \frac{1}{4\pi\varepsilon_0} \oint_S \frac{\sigma_b}{v} da' + \frac{1}{4\pi\varepsilon_0} \int_V \frac{\rho_b}{v} d\tau'$$
]

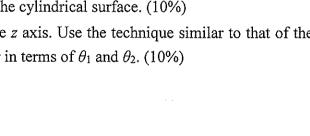
Jus - JXM

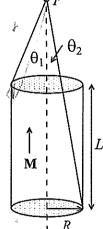
Kb= Mxn



- 3. A bar magnet of radius R and length L is magnetized with a uniform magnetization M in the z axis as shown in the figure.
  - (a) Find the bound volume current  $J_b$  inside the magnet as well as the bound surface currents  $K_b$  on both ends and the cylindrical surface. (10%)
  - (b) Find the magnetic field along the z axis. Use the technique similar to that of the solenoid and express you answer in terms of  $\theta_1$  and  $\theta_2$ . (10%)

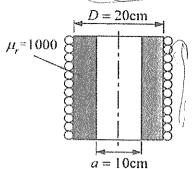
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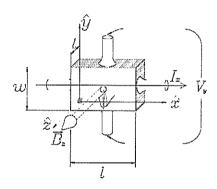


- 4. An *infinite* long magnetic material tube ( $\mu_r = 1000$ ) of inner diameter a = 10 cm and outer diameter D = 20 cm is tightly wrapped with thin solenoid of 30 turns per unit cm, as shown in the figure. The current per turn I is 1 A [Hint:  $\mu_0 = 4\pi \times 10^{-7}$  H/m]
  - (a) Find the auxiliary field **H** at the following three regions  $0 \le r \le a/2$ ,  $a/2 \le r \le D/2$ , and  $r \ge D/2$ . (7%)
  - (b) Find the magnetic field **B** at the following three regions  $0 \le r \le a/2$ ,  $a/2 \le r \le D/2$ , and  $r \ge D/2$ . (7%)
  - (a) Explain why the magnetic field **B** is discontinuous at the boundary r = a/2. (6%) [Hint: Use the boundary condition for **B** field.]

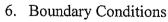




- 5. Consider a conducting slab as shown below with length l in the x direction, width w in the y direction and thickness t in the z direction. The conductor has charge carrier of charge q and charge carrier drift velocity  $v_x$  when a current  $I_x$  flows in the positive x direction. The conductor is placed in a magnetic field perpendicular to the plane of the slab  $\mathbf{B} = B_z \hat{\mathbf{z}}$ .
  - (a) When steady state is reached, there will be no net flow of charge in the y direction. Find the relation between  $(E_y)$ ,  $(F_z)$  and  $(F_y)$  and  $(F_y)$  (7%)
  - (b) Find the resulting potential difference  $V_y$  (the **Hall voltage**) between the top and bottom of the slab, in terms of  $B_z$ ,  $v_x$ , and the relevant dimensions of the slab. (7%)
    - (c) How do you determine the sign of the mobile charge carriers in a material? (6%) [Hint: n denotes the number of carriers per unit volume]







- (a) Write down the normal boundary condition  $E^{\perp}$  and the tangential boundary conditions  $\mathbf{E}^{\parallel}$ . [Hint:  $\nabla \cdot \mathbf{E} = \rho/\varepsilon_0$  and  $\nabla \times \mathbf{E} = 0$ ] (5%)
- (b) Write down the normal boundary condition  $D^{\perp}$  and the tangential boundary conditions  $\mathbf{D}^{\parallel}$ . [Hint:  $\nabla \cdot \mathbf{D} = \rho_f$  and  $\nabla \times \mathbf{D} = \nabla \times \mathbf{P}$ ] (5%)
- (c) Write down the normal boundary condition  $B^{\perp}$  and the tangential boundary conditions  $\mathbf{B}^{\parallel}$ . [Hint:  $\nabla \cdot \mathbf{B} = 0$  and  $\nabla \times \mathbf{B} = \mu_0 \mathbf{J}$ ] (5%)
- (d) Write down the normal boundary condition  $H^{\perp}$  and the tangential boundary conditions  $\mathbf{H}^{\parallel}$ . [Hint:  $\nabla \cdot \mathbf{H} = -\nabla \cdot \mathbf{M}$  and  $\nabla \times \mathbf{H} = \mathbf{J}_f$ ] (5%)