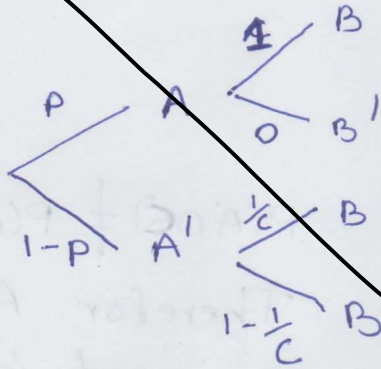


① A - Event of knowing the answer

B - Answer is correct

$$P(A|B) = ? \quad P(A) = P$$

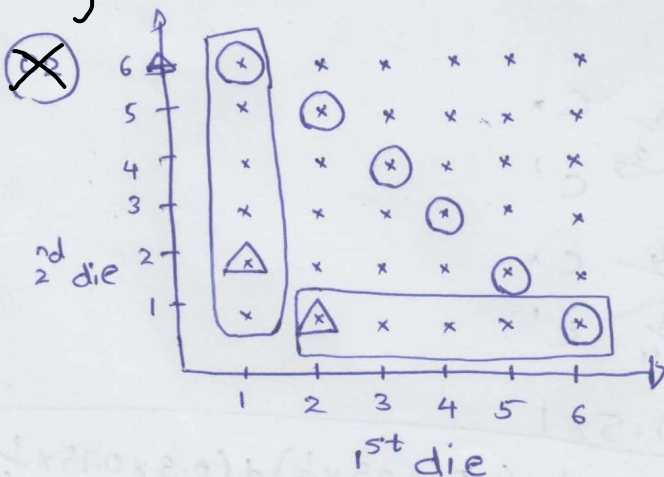


$$P(A \cap B) = P(A) \cdot P(B|A) \\ = P \times 1 = \underline{P}$$

$$P(B) = P \times 1 + (1-P) \times \frac{1}{c} \\ = P + \frac{1}{c} - \frac{P}{c} \\ = \frac{Pc + 1 - P}{c}$$

$$P(A|B) = \frac{P(A \cap B)}{P(B)} \\ = \frac{Pc}{Pc + 1 - P}$$

01)



A - Sum of 2 dice equal 3

B - " " " " " 7

C - at least one of the dice shows 1

Δ - A

O - B

□ - C

$$a) P(A|C) = \frac{P(A \cap C)}{P(C)}$$

$$= \frac{2/36}{11/36} = \underline{\underline{\frac{2}{11}}}$$

$$b) P(B|C) = \frac{P(B \cap C)}{P(C)}$$

$$= \frac{\frac{2}{36}}{\frac{11}{36}} = \frac{2}{11}$$

$$c) A \nsubseteq C$$

$$P(A \cap C) = \frac{2}{36}$$

$$P(A) \times P(C) = \frac{2}{36} \times \frac{11}{36}$$

$$P(A \cap C) \neq P(A) \times P(C)$$

Therefore A & C
are not independent

02

$$P(A) = 0.4 \quad P(B) = 0.3 \quad P((A \cup B)^c) = 0.42$$

$$P(A \cup B) = 1 - P((A \cup B)^c) = 1 - 0.42 \\ = 0.58$$

$$P(A \cap B) = P(A) + P(B) - P(A \cup B) \\ = 0.4 + 0.3 - 0.58 \\ = \underline{\underline{0.12}}$$

$$P(A) \times P(B) = 0.4 \times 0.3 = \underline{\underline{0.12}}$$

$$P(A \cap B) = P(A) \times P(B)$$

$\therefore A$ & B are independent.

03

A - First check point is busy

B - 2nd checkpoint is busy

$$P((A \cup B)^c) = 1 - P(A \cup B) \\ = 1 - [P(A) + P(B) - P(A \cap B)] \\ = 1 - [0.4 + 0.2 - 0.08] \\ = \underline{\underline{0.48}}$$

04

A - Event that rating is very good

B - Event that rating is good

$$P(A) = 0.22 \quad P(B) = 0.35$$

$$\begin{aligned} a) \quad P(A^c) &= 1 - P(A) \\ &= 1 - 0.22 = \underline{\underline{0.78}} \end{aligned}$$

$$\begin{aligned} b) \quad P(A \cup B) &= P(A) + P(B) \quad (\text{Since two events are mutually exclusive}) \\ &= 0.22 + 0.35 \\ &= \underline{\underline{0.57}} \end{aligned}$$

$$c) \quad P(A \cap B) = 0$$

05

A - Event that a student fails in maths.

B - " " " " " English.

$$P(A) = 0.2$$

$$P(B) = 0.15$$

$$P(A \cap B) = 0.03$$

$$\begin{aligned} P(A \cup B) &= P(A) + P(B) - P(A \cap B) \\ &= 0.20 + 0.15 - 0.03 \\ &= \underline{\underline{0.32}} \end{aligned}$$

06

A - Drawing a king

B - " " Diamond

NO. These two events are not mutually exclusive. These two events have an intersection, ex: Diamond king.

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$= \frac{4}{52} + \frac{13}{52} - \frac{1}{52} = \frac{16}{52}$$

07

R - Event of getting a red ball

Y - " " " " Yellow "

G - " " " " green "

$$P(R) = \frac{4}{18} \quad P(Y) = \frac{8}{18} \quad P(G) = \frac{6}{18}$$

These three events are mutually exclusive.

$$\therefore P(R \cup G) = P(R) + P(G) = \frac{4}{18} + \frac{6}{18} = \frac{10}{18} = \frac{5}{9}$$

09 R-2, b-4, w-5

R - Getting a Red ball

B - " " blue ball

W - " " White "

$$a) P(R) = \frac{2}{11}$$

c) these three events are mutually exclusive.

$$b) P(R') = \frac{9}{11}$$

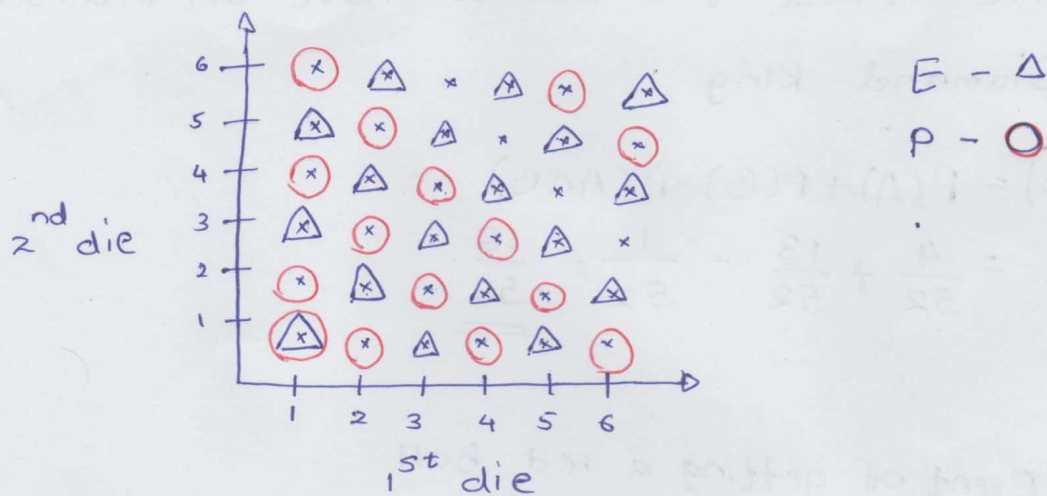
$$P(R \cup B) = P(R) + P(B)$$

$$= \frac{2}{11} + \frac{4}{11} = \frac{6}{11}$$

10

E - Event of rolling a sum that is an even number

P - Event of rolling a sum that is a prime number.



$$P(P \cup E) = P(P) + P(E) - P(P \cap E)$$

$$= \frac{15}{36} + \frac{18}{36} - \frac{1}{36}$$

$$= \frac{32}{36}$$

12 G - Event of watching gymnastic
B = " " " base ball
S = " " " soccer

$$P(G) = 0.28, P(B) = 0.29, P(S) = 0.19,$$

$$P(G \cap B) = 0.14, P(B \cap S) = 0.12, P(G \cap S) = 0.1$$

$$P(G \cap B \cap S) = 0.08$$

$$P(G \cup B \cup S) = 1 - P(G \cap B \cap S)$$

$$\text{We know, } P(G \cup B \cup S) = P(G) + P(B) + P(S) - P(G \cap B) - P(G \cap S) - P(B \cap S) + P(G \cap B \cap S)$$

$$P(\text{GUBUS}) = 0.28 + 0.29 + 0.19 - 0.14 - 0.1 - 0.12 + 0.08$$

$$= \underline{\underline{0.48}}$$

$$P(\text{GUBUS})' = 1 - 0.48 = \underline{\underline{0.52}}$$

- ⑬ S - Event that the visit is for specialist
L : " " " " " " Lab work

$$P(\text{SUL})' = 0.35$$

$$P(S) = 0.3$$

$$P(L) = 0.4$$

$$\begin{aligned} P(S \cap L) &= P(S) + P(L) - P(\text{SUL})' \\ &= P(S) + P(L) - [1 - P(\text{SUL})'] \\ &= 0.3 + 0.4 - [1 - 0.35] \\ &= \underline{\underline{0.05}} \end{aligned}$$

⑭ $P(A \cup B) = 0.7$
 $P(A \cup B^c) = 0.9$



$$\therefore P(A) = 0.7 - 0.1 = \underline{\underline{0.6}}$$

Q8) we know $P(A \cup B) \leq 1$

$$P(A) + P(B) - P(A \cap B) \leq 1$$

$$P(A) + P(B) - 1 \leq P(A \cap B).$$

$$\therefore P(A \cap B) \geq P(A) + P(B) - 1$$

Q11)

$$P(A) = 0.8, P(B) = 0.9$$

if A & B are mutually exclusive,

$$P(A) + P(B) = P(A \cup B)$$

here,

$$P(A) + P(B) = 0.8 + 0.9 = 1.7$$

But $P(A \cup B) \neq 1$. Therefore, there should be an intersection.

\therefore A & B are not mutually exclusive.

15)

Q14)

A - Event that a patient visits chiropractor

B - " " " " " physical therapist

$$P(A \cap B) = 0.22, P(A \cup B) = 0.12, P(B) = a, P(A) = 0.14a$$

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$[1 - 0.12] = 0.14a + a - 0.22$$

$$0.88 = 1.14a - 0.22$$

$$1.1 = 1.14a$$

$$a = 0.9649$$

$$\therefore P(B) = 0.9649$$

Corrected Answer for Third Question in Tutorial 03

03)

Let X - Student knows the answer

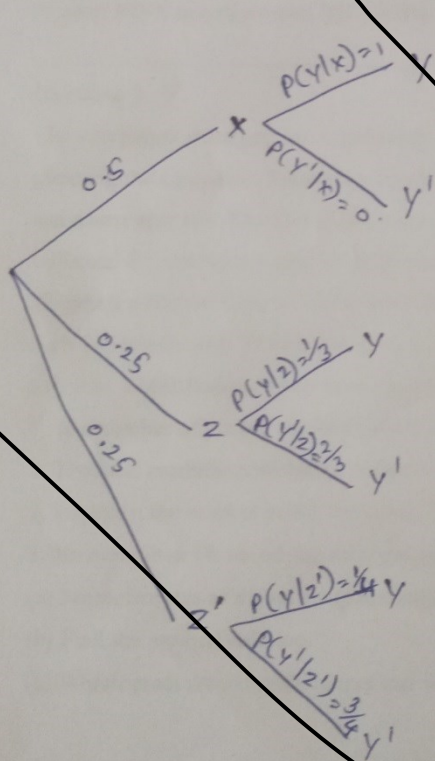
Y - The answer is correct.

Z - Student eliminate one choice.

Given that, $P(X) = 0.5$, $P(Z) = 0.25$

$P(Y|X) = 1$, $P(Y|Z) = \frac{1}{3}$, $P(Y|Z') = \frac{1}{4}$.

If we draw tree diagram,



~~$P(X|Y)$~~

$$P(X|Y) = \frac{P(X \cap Y)}{P(Y)}$$

$$= \frac{P(X \cap Y)}{P(X \cap Y) + P(Z \cap Y) + P(Z' \cap Y)}$$

$$= \frac{P(Y|X) \cdot P(X)}{P(Y|X) \cdot P(X) + P(Y|Z) \cdot P(Z) + P(Y|Z') \cdot P(Z')}$$

$$= \frac{1 \times 0.5}{(1 \times 0.5) + (\frac{1}{3} \times 0.25) + (\frac{1}{4} \times 0.25)}$$

$$= \underline{\underline{0.7742}}$$

(Here, X , Z , and Z' are mutually exclusive & collectively exhaustive events)