References

References:

The material in this handout is collected from the following references:

- Sections 2.3.1 and 6.2.2 of the text book C++ Primer.
- Section 7.7 of <u>C++ Programming Language</u>.
- Section 8.5 of <u>Programming: Principles and Practice Using C++</u>.

Types, objects, and variables

Every name and every expression has a type that determines the operations that may be performed on it.

- A *type* defines a set of possible values and a set of operations that can be applied on these values.
- An *object* is some memory that holds a value of some type.
- A value is a set of bits interpreted according to a type.
- A variable is a named object.
- A *declaration* is a statement that introduces a name to the compiler. It specifies a type associated with that name. The following statements are declarations (but not definitions):

```
1 extern int mile; // declaration of an external (or global) variable
2 int add(int, int); // declaratinon (or prototype)
```

A definition is a special kind of declaration that causes memory to be reserved for a variable
and initializes the memory with an optional set of values. The following statements are
definitions (and also declarations):

```
int mile;
int add(int left, int right) {
  return left + right;
}
```

Review of pointers and memory [from C]

Each variable in a program stores its contents in the computer's memory, and each byte-sized chunk of the memory has an address number. The size of the memory chunk or the number of bytes associated with a variable is determined by the variable's type. For example, an <code>int</code> variable requires 4 bytes of memory while a <code>double</code> variable requires 8 bytes of memory. This is the notation that will be used when talking about variables in memory:



In the picture above,

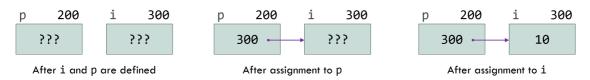
- variable refers to a named object.
- address refers to the arbitrary address number associated with the starting byte of the
 memory chunk where the variable is given storage. Note that the actual addresses are
 determined at program startup but using specific values would be useful for discussion
 purposes.
- contents refers to the value stored at this location; ??? means the value is unspecified.

Conceptually, a pointer variable itself does not directly contain a value like an <code>int</code> or a <code>double</code>, but it contains the address in memory of another variable or function. When the <code>int</code> or <code>double</code> value is accessed through the pointer variable, then that value is accessed indirectly.

We can declare pointer variables easily:

```
1
   void foo() {
2
     int i; // i can only store integer values
3
             // the value of i is unspecified at this point
4
     int *p; // p can only store the address of an integer
5
             // the value of p is unspecified at this point
6
     p = &i; // the value of p is now the address of variable i
7
     i = 10; // the value of i is now 10
   }
8
```

Visualizing the code in function foo:



From the pictures, you can see that it is possible to modify variable is value in two different ways:

• directly through the variable i:

```
1 | i = 20; // value of i is now 20
```

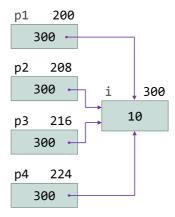
- indirectly through the pointer variable p. The * operator is called the *dereference* or *indirection* operator and it indirectly allows us to access the int value stored at the variable that the pointer p is pointing to. The compiler will evaluate expression *p in the following manner:
 - 1. The compiler will read the value stored in variable p and treat it as a memory address where an int value is stored.
 - 2. Next, the compiler will reference the four-byte sized memory chunk starting at this address to retrieve the integer stored there. In the following statement, we're indirectly assigning value 30 to variable $\boxed{\mathbf{x}}$:

```
1 | *p = 30; // value of i is now 30
```

Expression *p = 30 takes integer value 30 and stores it at memory address stored in variable p. Since p contains address 300, value 30 will then be stored at memory address 300, thus indirectly changing the value of variable i from 10 to 30.

The pointer and the variable it is pointing to are distinct and independent objects. Assigning a new value to i doesn't affect point p - it will continue to point to i; assigning p the address of a different int variable doesn't affect variable i. In fact, we can have any number of pointers pointing to i:

```
1 int i {10};
2 int *p1 {&i}, *p2 {p1}, *p3 {p2}, *p4 {p3};
```



Each of these pointers can be used to modify i. In addition, each pointer variable can be modified to point at some other int variable.

An important thing that you learnt in C is that every program object (variable or function) can only be associated with one address. That is, once you name a memory location, that name cannot be used for another memory location in the same scope. In other words, once you *bind* a name to a memory location, you can't unbind it.

```
int i {1}; // i is the name of a four byte-sized memory chunk in the
2
               // .data region of program memory
   void f() {
3
4
      int i;
               // OK: i is the name of a four byte-sized memory chunk in the
5
                // .stack region of program memory
6
                // This local (internal) variable i has a different memory chunk
7
                // then the global (external) variable i
      double d; // OK: d is name of 8 byte-sized memory chunk
8
9
      float d; // ERROR: trying to rename another memory chunk to d
10
      // other code here ...
11
   }
```

C++ introduces *references* which conceptually allow multiple names to be associated with one address.

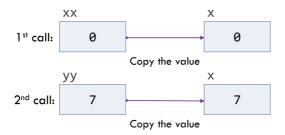
Motivation for references

Pointers are useful in two contexts: to *efficiently pass large amounts of data* to a function and to pass an address to a function so that the function *modifies the original* and not the copy.

The simplest way of passing an argument to a function is to give the function a copy of the value you use as the argument. A parameter of a function <code>foo()</code> is a local variable in <code>foo()</code> that's initialized each time <code>foo()</code> is called with the value that the argument evaluates to. For example:

```
4
    return x;
 5
    }
 6
 7
    int main() {
 8
      int xx {0};
 9
      std::cout << foo(xx) << '\n'; // write: 1</pre>
10
      std::cout << xx << '\n'; // write 0; foo doesn't change xx
11
      int yy {7};
12
13
      std::cout << foo(yy) << '\n'; // write: 8
14
      std::cout << yy << '\n'; // write 7: foo doesn't change yy
15
    }
```

Since a copy is passed, expression x = x + 1 in foo() only increments local copies of xx and yy passed in the two calls. This kind of communication between functions is called *pass-by-value* or *call-by-value*. We can illustrate a pass-by-value communication like this:



Pass-by-value is a pretty straightforward and its cost is the cost of copying the value. Pass-by-value can be used to pass around pointers. For example, a function to swap or exchange the values of two variables can be authored like this:

```
void swap(double *lhs, double *rhs) {
double tmp {*lhs};
   *lhs = *rhs;
   *rhs = *tmp;
}
```

A pointer allows us to pass potentially large amounts of data around between functions at a low cost – instead of copying the data we simply copy a pointer to the data. That is, we pass a function the address where the data is stored as a pointer value. The type of the pointer determines what can be done to the data through the pointer. For example:

```
// compute the sum of the elements of a potentially large array
int accumulate(int const *p, int size) {
  int sum {*p};
  for (int i {1}; i < size; ++i) {
    sum += *(p + i);
  }
  return sum;
}</pre>
```

Using a pointer differs from using the name of an object in a few ways:

- We use a different syntax, for example, *p instead of obj and (*p).m or p->m rather than obj.m.
- We can make a pointer point to different objects at different times.

• We must be more careful when using pointers than when using an object directly: a pointer may be a nullptr or point to an object that wasn't the one we expected.

These differences can be annoying.

- For example, some programmers find foo(&x) ugly compared to foo(x).
- Worse, managing pointer variables with varying values and protecting code against the possibility of nullptr can be a significant burden.
- Finally, when we want to overload an operator, say +, we want to write x+y rather than &x+&y.

The mechanism in C++ addressing these concerns is called a <u>lvalue reference</u>. Recall that lvalue is an expression representing an object whose address you can take.

- Like a pointer, a lvalue reference is an *alias* for an object. That is, a lvalue reference is an *alternative name* for an object.
- A lvalue reference is usually implemented to hold the machine address of an object.
- A Ivalue reference does not impose performance overhead compared to pointers.

But a lvalue reference differs from a pointer in that:

- You access a lvalue reference with exactly the same syntax as the name of an object.
- A Ivalue reference always refers to the object to which it was initialized.
- There is no *null lvalue reference* and we may assume that a lvalue reference will always refer to an object.

The main use of Ivalue references is to do what pointers do:

- efficiently pass large amounts of data to a function, and
- pass a lvalue reference to a function that can be used by the function to modify the variable being referenced

while avoiding the annoying syntax of pointers and without the possibility of dealing with null pointers.

Syntax for defining and using Ivalue references

A lvalue reference is a construct that allows a user to declare a new name for an object, *an alias*. In a type name, the notation T& means "lvalue reference to T." Since int& means a lvalue reference to an int object, we can write:

```
int var {1}; // var is name of 4 byte-sized memory chunk with value 1
int &r {var}; // r is lvalue reference or alias to var
int x = r; // x is another int variable with a different 4 byte-sized
// memory that is initialized with the value of var
```

The symbol r doesn't represent a new variable nor a new storage location; it is just simply another name for var. What we've done is bind the name r to the memory location known as var. Conceptually, think of r and var as just aliases for the same memory location. That is, any use of r is really a use of var. r can be used anywhere that var is used and in the exact same way. Anywhere variable var can be used in an expression, it can be replaced with its alias:

```
1 | var = 2; // var is (directly) assigned 2
2  r = 4; // var becomes through an alias r 4
3 | std::cout << r << " | " << var << '\n'; // write: 4 | 4</pre>
```

A Ivalue reference is just an alternative name or alias for a variable.

To ensure that a lvalue reference is a name for something (that is, that it is bound to an object), we must *initialize the lvalue reference*. For example:

```
int var {1};
int &r1 {var}; // OK: r1 initialized
int &r2; // ERROR: initializer missing
extern int &r3; // OK: r3 initialized elsewhere
```

Initialization of a lvalue reference is trivial when the initializer is an lvalue (an object whose address you can take):

```
int var {10};
int &r {var}; // OK: r is initialized as alias to var
int &rr {10}; // ERROR: initializer to reference rr is not an lvalue!!!
int &rrr {var+10}; // ERROR: initializer to reference rrr not an lvalue!!!
```

The definition of \mathbf{r} as a reference to \mathbf{var} is legal in line 1 since \mathbf{var} is addressable. Expression 10 represents an rvalue expression and thus the definition in line 2 is illegal. The expression $\mathbf{var}+10$ on line 4 is an rvalue expression and therefore the definition on line 3 is also illegal.

An Ivalue reference must be initialized with the initializer for a "plain" $\top \&$ being an Ivalue of type \top .

Once initialized, a lvalue reference cannot refer an other variable. This means that the initialization of a lvalue reference is something quite different from assignment to it:

```
int var1 {10}, var2 {20};
int &r {var1}; // OK: r initialized to alias var1
r = var2; // OK: var1 is assigned value of var2
```

On line 2, \mathbf{r} is initialized to reference int variable var1. The assignment expression $\mathbf{r} = var2$ on line 3 is not making \mathbf{r} be an alias to a different int variable var2. Instead, the value stored in variable var2 is being assigned to the variable var1 that \mathbf{r} is aliasing. Consequently, the value of a lvalue reference cannot be changed after initialization; it always refers to the object it was initialized to denote. Thus, the obvious implementation of a lvalue reference is as a *read-only* pointer initialized to point to an object that is dereferenced each time it is used. Since the pointer is read-only, it can never point to another object. It is ok to think about lvalue references that way, as long as one remembers that a lvalue reference isn't an object that can be manipulated the same way a pointer is.

Once initialized, a Ivalue reference cannot alias another variable.

Despite appearances, no operator operates on a lvalue reference:

```
1 int var {10};
2 int &rr {var}; // OK: rr can never alias anything else other than var
3 ++rr; // var is incremented to 11
```

Here, ++rr doesn't increment lvalue reference rr; rather, ++ is applied to the int to which rr refers, that is, to var.

Operators don't operate on a Ivalue reference; they operate on the referenced variable.

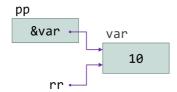
Applying the & operator on a lvalue reference doesn't give a pointer to a lvalue reference but gives a pointer to the object aliased by the lvalue reference:

```
1 int var {10};
2 int &r {var};
3 int *p {&r}; // p points to object aliased by r, that is, var
```

Both Ivalue references and pointers provide an alternative way to access an existing variable: pointers through the variable's address, and Ivalue references through another name for that variable. Since a Ivalue reference can be thought of as an *alias* for another variable, a Ivalue reference, unlike a pointer, does not take up any additional memory.

```
int var {10}; // var is 4 byte-sized memory chunk with value 10
int *pp {&var}; // pp is 8 byte-sized memory chunk having address of var
int &rr {var}; // rr is lvlaue reference or alias to var
```

The following picture makes it clear that a pointer and Ivalue reference are different entities:



The picture shows that rr is not a new variable [like a pointer] with memory storage reserved for it; it is just another name for var. In some cases, the compiler will optimize away a lvalue reference so that there is no object representing that lvalue reference at run time.

You can see that var and rr do, in fact, represent the same memory chunk with pointer pp pointing to that memory chunk:

```
1 | var: 10 | rr: 10 | *pp: 10
2 | &var: 0x7ffd5b702c34 | &rr: 0x7ffd5b702c34 | pp: 0x7ffd5b702c34
```

An Ivalue reference does not have an address and is therefore not an object. Therefore, there can be no Ivalue references to Ivalue references, no pointers to Ivalue references, nor an array of Ivalue references.

Lvalue references to constants

Initialization of a Ivalue reference is trivial when the initializer is an Ivalue [an object whose address you can take]. The initializer for a "plain" T& must be an Ivalue of type T.

```
1 int var {10};
2 int &r1 {var}; // OK: var is an lvalue
3 int &r2 {20}; // ERROR: 20 is not an lvalue
```

The initializer for a T const& need not be an Ivalue or even of type T. In such cases:

- First, implicit type conversion to T is applied if necessary.
- Then, the resulting value is placed in a temporary variable of type T.
- Finally, this temporary variable is used as the value of the initializer.

Consider the following code fragment:

```
double &dr {1}; // ERROR: lvalue needed as initializer to reference double const &rcd {1}; // OK
```

The interpretation of the initialization might be:

```
double temp = double {1.0}; // first, create a temporary with right value double const &rcd {temp}; // then use the temporary as cdr's initializer
```

The temporary created to hold a lvalue reference initializer persists until the end of its lvalue reference's scope.

Main use of references

The main uses of Ivalue references is to do what pointers do:

- efficiently pass large amounts of data to a function,
- pass a lvalue reference to a function that can be used by the function to modify the variable being referenced, and
- return values by Ivalue reference

while avoiding the annoying syntax of pointers and without the possibility of dealing with null pointers.

Pass-by-const-Ivalue-reference

<u>Pass-by-value</u> is simple, straightforward, and efficient when we pass small values such as an <u>int</u> or a <u>double</u>. But what if the value is large, such as an image consisting of several million bytes, a large table of values consisting of thousands of integers, or a lengthy string consisting of thousands of characters. Then, copying can be costly. For example, we could write a function to print out a <u>vector</u> of floating-point numbers like this:

```
void print(std::vector<double> v) { // is pass-by-value appropriate?

std::cout << "{";

for (int i {0}, len {v.size()}; i < len; ++i) {

   std::cout << v[i] << (i != len-1 ? ", " : "}\n");
}

}
</pre>
```

We could use function print() for vectors of all sizes. For example:

```
void f(int x) {
1
2
     std::vector<double> vd1(10);
                                       // small vector
3
     std::vector<double> vd2(1'000'000); // large vector
4
     std::vector<double> vd3(x); // vector of unknown size
     // fill vd1, vd2, and vd3 will values
5
6
     print(vd1);
7
     print(vd2);
8
     print(vd3);
9
  }
```

This code works, but the first call to print() has to copy ten double s, the second has to copy a million double s, and we don't know how much the third call has to copy. The intent of print() is to just print the vector s, not to make copies of their elements. One way to pass a variable to a function without copying it is to provide print() a pointer to the vector variable:

```
void print(std::vector<double> const *pv) { // pass-by-const-pointer
std::cout << "{";
for (int i {0}, len {pv->size()}, i < len; ++i) {
    std::cout << (*pv).[i] << (i != len-1 ? ", " : "}\n");
}
print(&vd2);</pre>
```

The parameter declaration <code>vector<double> const *pv</code> means <code>pv</code> is a pointer to <code>read-only vector</code> of <code>double</code> s with the <code>const</code> enabling the compiler to prevent changes to the container. The major disadvantage of pointers is that there is no test in <code>print()</code> for a <code>nullptr</code>. The programmer probably decided to reduce the overhead of a test to make the function more efficient. A second albeit minor disadvantage is the awkward and cumbersome syntax on lines 3, 4, and 8.

We've learnt that another way to pass a variable to a function without copying is to provide function print() an *lvalue reference* to the vector variable:

```
void print(std::vector<double> const &v) { // pass-by-const-lvalue-reference
std::cout << "{";
for (int i {0}; i < v.size(); ++i) {
    std::cout << v[i] << (i != v.size()-1 ? ", " : "}\n");
}
</pre>
```

The & means "reference" and the const is there to stop print() from inadvertently modifying its argument. Apart from the change to the parameter declaration, all is the same as before; the only change is that instead of operating on a copy, print() 's parameter now refers back to the argument through the reference. Note the phrase "refer back"; such parameters are called references because they "refer" to objects defined elsewhere. We can call this print exactly as before:

```
void f(int x) {
1
2
     std::vector<double> vd1(10); // small vector
3
     std::vector<double> vd2(1'000'000); // large vector
4
     std::vector<double> vd3(x); // vector of unknown size
     // fill vd1, vd2, and vd3 will values
5
     print(vd1);
6
7
     print(vd2);
8
     print(vd3);
9
  }
```

Pass-by-const-reference is an useful and popular mechanism because a test for *null reference* is not required and unlike pointers, the syntax is similar to pass-by-value semantics. More importantly, a const reference has the useful property that we can't accidentally modify the object passed. For example, if we inadvertently tried to assign to an element from within print(), the compiler would catch it:

```
void print(std::vector<double> const &v) { // pass-by-const reference
// ...
v[i] = 7; // ERROR: v is a const and therefore is not mutable
// ...
}
```

As a second example, consider a function <code>my_find()</code> that searches for a <code>string</code> in a <code>vector</code> of <code>string</code> s:

```
1 | int my_find(std::vector<std::string> vs, std::string s);
```

Pass-by-value is unnecessarily costly. If the container contains thousands of string s, the time spent even on a fast computer would be noticeable. So, we could improve my_find() by making it take its parameters by const reference:

```
int my_find(std::vector<std::string> const &vs, std::string const &s) {
1
2
     for (int i {0}, len {vs.size()}; i < len; ++i) {
3
       if (vs[i] == s) {
         return i;
4
5
       }
     }
6
7
     return -1;
   }
8
```

We can also specify *references to arrays*:

```
int accumulate(int const (&ra)[N]) {
  int sum{}; // zero out sum
  for (int elem : ra) { // this is range-for statement
    sum += elem;
}
return sum;
}
```

Pass-by-Ivalue-reference

But what if we did want a function to modify its parameters? Sometimes, that's a perfectly reasonable thing to wish for. For example, we might want a function <code>init()</code> that assigns values to vector elements:

```
void init(std::vector<double> &v) { // pass-by-reference
     for (int i {0}, len {v.size()}; i < len; ++i) v[i] = i;
 3
   }
4
 5 void g(int x) {
    std::vector<double> vd1(10);  // small vector
6
    std::vector<double> vd2(1'000'000); // large vector
7
8
    std::vector<double> vd3(x);
                                  // vector of unknown size
    // fill vd1, vd2, and vd3 will values
9
     init(vd1);
10
11
    init(vd2);
12
    init(vd3);
13 }
```

Here, we wanted <code>init()</code> to modify the <code>vector</code> argument <code>vd1</code> (and <code>vd2</code> and <code>vd3</code>), so we did not copy [did not use pass-by-value] or declare the lvalue reference <code>const</code> [did not use pass-by-const lvalue reference] but simply passed a plain lvalue reference to each of the <code>vectors</code>.

The key property of Ivalue references, that a Ivalue reference can be a convenient shorthand for some object, is what makes them useful as parameters. Useful because a Ivalue reference can be used to specify a function parameter so that the function can change the value of an object passed to it. For example:

```
int increment(int &aa) {
 2
     ++aa;
 3
      return aa;
 4
    }
 5
 6 int main() {
 7
    int xx {0};
     std::cout << increment(xx) << "\n"; // write: 1</pre>
8
 9
     std::cout << xx << "\n";  // write: 1
10
11
     int yy {7};
    std::cout << increment(yy) << "\n"; // write: 8</pre>
12
      std::cout << yy << "\n";</pre>
13
                                          // write: 8
14 }
```

The semantics of argument passing are defined to be those of initialization, so when called, increment() 's parameter as becomes another name for xx in the first call to increment() and as becomes another name for yy in the second call to increment().

Pass-by-Ivalue-reference is clearly a very powerful mechanism: we can have a function operate directly on any object to which we pass a reference. For example, swapping two values is an important operation in many algorithms, such as sorting. Using Ivalue references, we can write a function that swaps <code>doubles</code> like this:

```
void my_swap(double &lhs, double &rhs) {
2
     double tmp {lhs};
3
     lhs = rhs;
4
     rhs = tmp;
5
   }
6
7 int main() {
8
    double x {10}, y {20};
9
    std::cout << "Before swap: x = " << x << " | y == " << y << "\n";
10
    my_swap(x, y);
    std::cout << "After swap: x = " << x << " | y == " << y << "\n";
11
12
```

my_swap() 's parameters 1hs and rhs - both of type lvalue reference to double - refer back to arguments x and y, respectively.

Note: When you pass a parameter by reference, you are actually passing an address to the function. Roughly speaking, you get pass-by-address semantics with pass-by-value syntax. The compiler is doing all of the necessary dereferencing for you behind the scenes.

The standard library provides function swap() for every type that you can copy that possibly looks like this:

```
template <typename T>
void swap(T& lhs, T& rhs) {
   T tmp = lhs;
   lhs = rhs;
   rhs = tmp;
}
```

This is called a *template function*. We'll discuss this topic later in the semester and is provided here in case you were wondering how the standard library implements the swap function for a variety of types.

Output-only Ivalue reference parameters

Suppose we wish to author a function to compute and "return" the two roots of a quadratic equation:

$$ax^2 + bx + c = 0$$

$$\Longrightarrow egin{cases} x_1 = rac{-b + \sqrt{b^2 - 4ac}}{2a} \ x_2 = rac{-b - \sqrt{b^2 - 4ac}}{2a} \end{cases}$$

It is well known that functions can return a single object. However, the quadratic solution function must output two values. One way for the function to output two values to the function caller is to use "output-only" lvalue reference parameters. In the following code fragment, lvalue reference parameter r1 and r2 are examples of parameters specified only to output values from the function to the function caller.

```
double discriminant(double a, double b, double c) { // helper function
return b * b - 4 * a * c;
}
```

```
4 // r1 and r2 are output-only lvalue reference parameters
5 void quadratic(double a, double b, double c, double &r1, double &r2) {
      double sq_disc {std::sqrt(discriminant(a, b, c))};
7
     double den \{2.0 * a\};
8
      r1 = (-b + sq_disc) / den; // r1 and r2 were passed in as references
9
      r2 = (-b - sq\_disc) / den;
10 }
11
12 | int main() {
13
      double a {1.0}, b {4.0}, c {2.0}, root1, root2;
      quadratic(a, b, c, root1, root2);
14
15
      std::cout << "a = " << a << ", b = " << b << ", c = " << c << "\n";
16
      std::cout << "root1 = " << root1 << " | root2 = " << root2 << "\n";
17
18
   }
```

Pass-by-value vs. pass-by-lvalue-reference

When should you use pass-by-value, pass-by-reference, and pass-by-const-lvalue-reference? Consider first a technical example:

```
void f(int a, int &r, int const &cr) {
    ++a; // change the local a
    ++r; // change the object referred to by r
    ++cr; // ERROR: cr is read-only!!!
}
```

If you want to change the value of the object passed, you must use a non-const lvalue reference: pass-by-value gives you a copy and pass-by-const -lvalue-reference prevents you from changing the value of the object passed.

For the simplest, least error-prone, and most efficient code, the rules of thumb are:

- 1. Use pass-by-value to pass *very small* objects. By very small, we mean one or two ints, one or two doubles, or something similar.
- 2. Use pass-by-const -lvalue-reference to pass large objects that you don't need to modify.
- 3. Return a result rather than modifying an object through a lvalue reference parameter.
- 4. Use pass-by-lvalue-reference only when you have to. This happens when you want to manipulate containers such as vector's and other large objects and for functions that change several objects.

The third rule reflects that you've a choice when you want to use a function to change the value of a variable. Consider:

```
int incr1(int a) { return a+1; } // return new value as the result
void incr2(int &a) { return ++a; } // modify object passed as reference

int x = 7;
x = incr1(x); // pretty obvious what is going on here
incr2(x); // pretty obscure: could be pass-by-value or pass-by-reference
```

incr2(x) notation doesn't give a clue to the reader that x's value is being modified, the way x = incr1(x) does. Consequently, "plain" Ivalue references should be used only where the name of the function gives a strong hint that the Ivalue reference argument is modified.

Return-by-Ivalue-reference

Lvalue references can also be used as return types. This is mostly used to define functions that can be used on both the left-hand and right-hand sides of an assignment. Returning Ivalue references is especially useful for overloaded operators that can be used on both the left-hand and right-hand sides of an assignment. The most common examples are member functions std::vector::operator[]() and std::string::operator[]().

```
std::vector<int> v(10); // create an int vector of size 10
v[5] = 10; // v[5] evaluates to int&
int x = v[5]; // v[5] evaluates to int&

std::string s("tomorrow");
s[0] = 'T'; // s[0] evaluates to char&
char ch = s[2]; // evaluates to char&
```