# Data Structures Chapter 4

- 1. Singly Linked List
- 2. Doubly Linked List
  - Revisit Singly Linked List
  - Doubly Linked List with Sentinels
  - Basic Operations
  - Advanced Operations



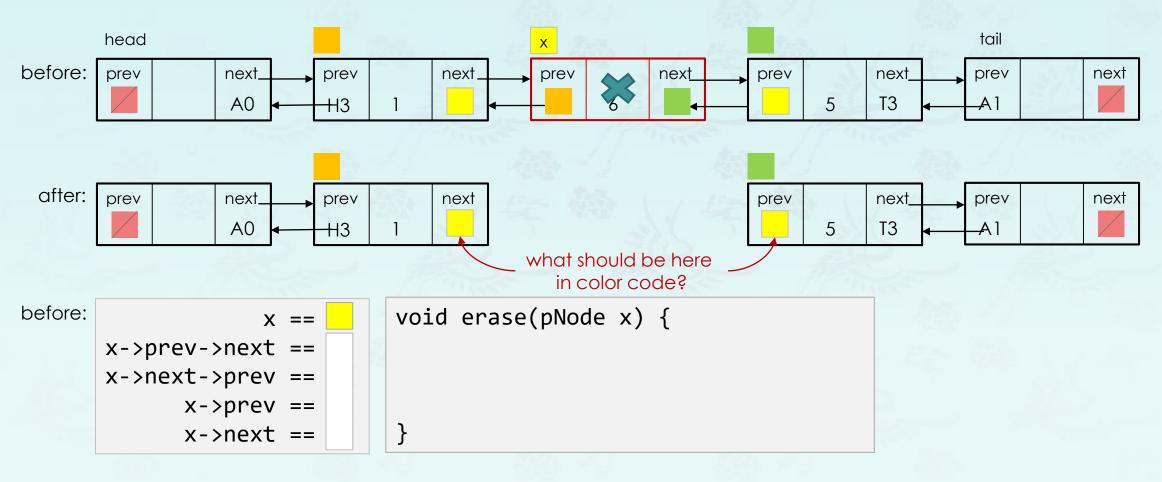
다윗은 당시에 하나님의 뜻을 따라 섬기다가 잠들어 그 조상들과 함께 묻혀 썩음을 당하였으되. 행13:36

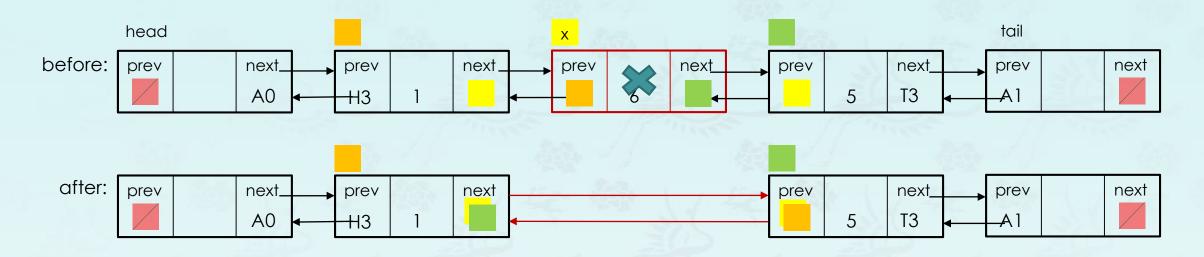
For when David had served God's purpose in his own generation, he fell asleep; he was buried with his fathers and his body decayed. Acts 13:36

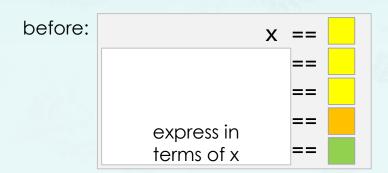
우리가 알거니와 하나님을 사랑하는 자 곧 그의 뜻대로 부르심을 입은 자들에겐 모든 것이 합력하여 선을 이루느니라 (롬8:28)

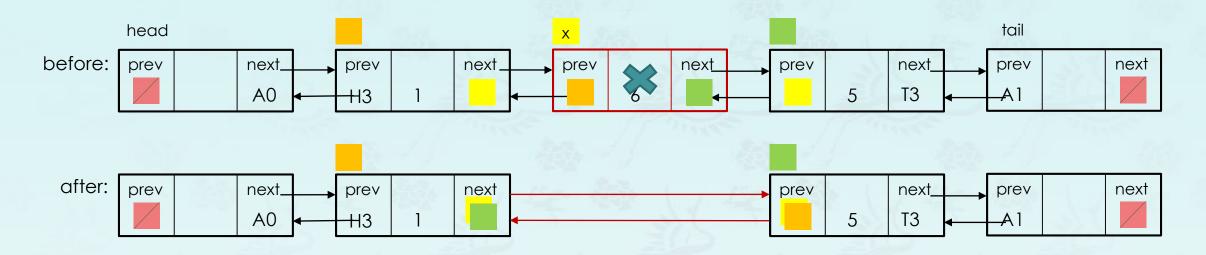
하나님이 우리를 구원하사 거룩하신 소명으로 부르심은 우리의 행위대로 하심이 아니요 오직 자기의 뜻과 영원 전부터 그리스도 예수 안에서 우리에게 주신 은혜대로 하심이라 (딤후1:9)

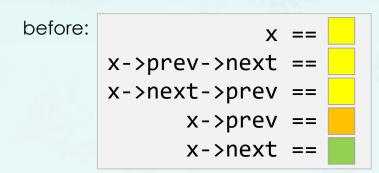
The node x is to be erased or removed. Then, which nodes are changed and where?

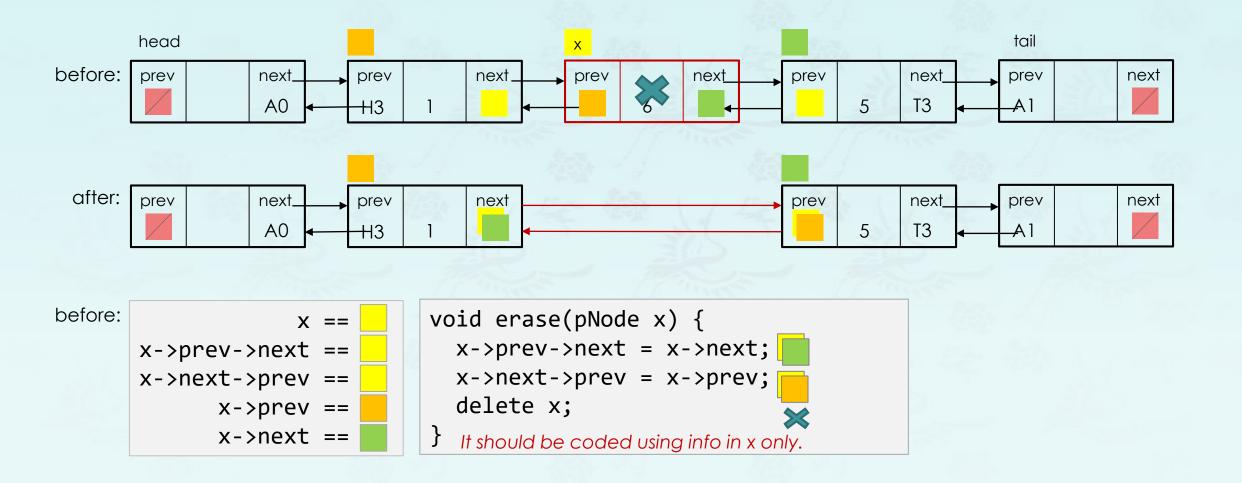






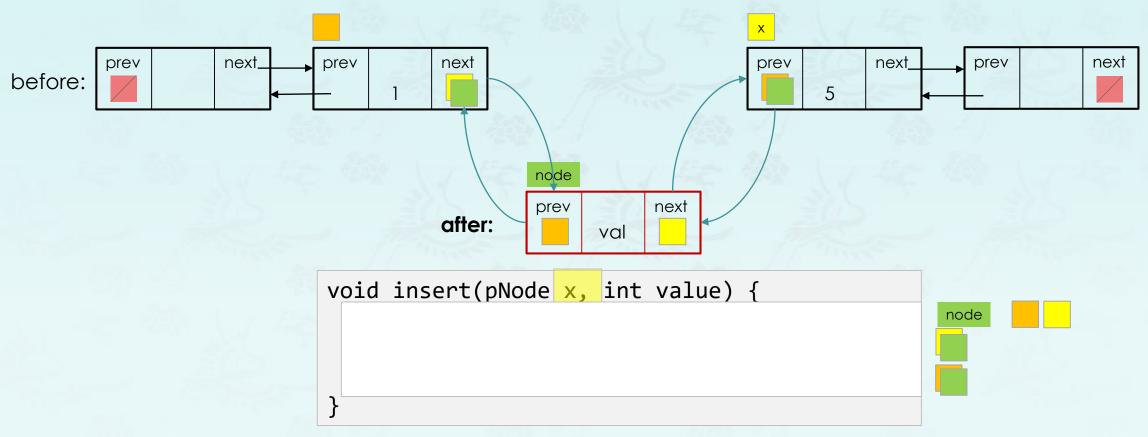




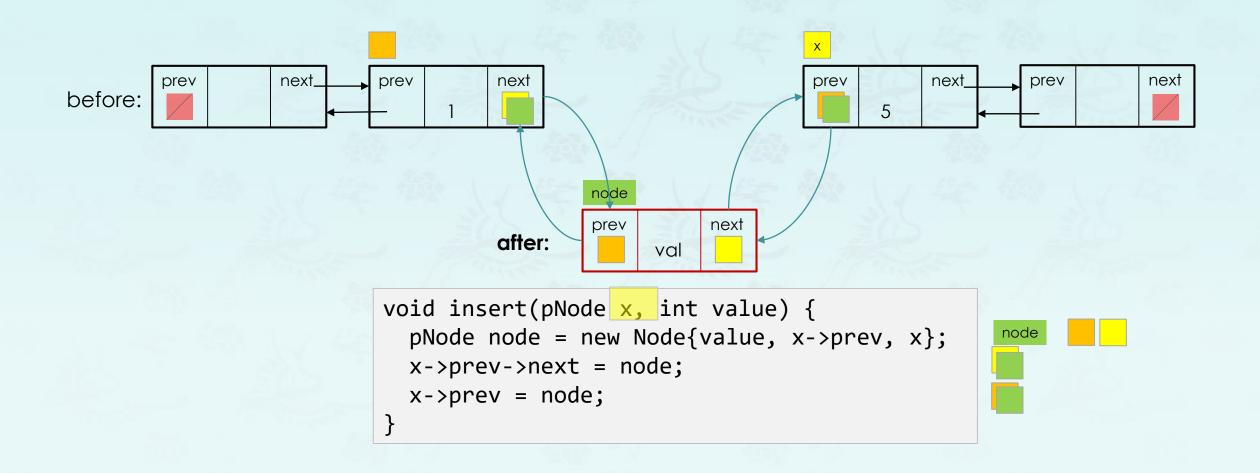


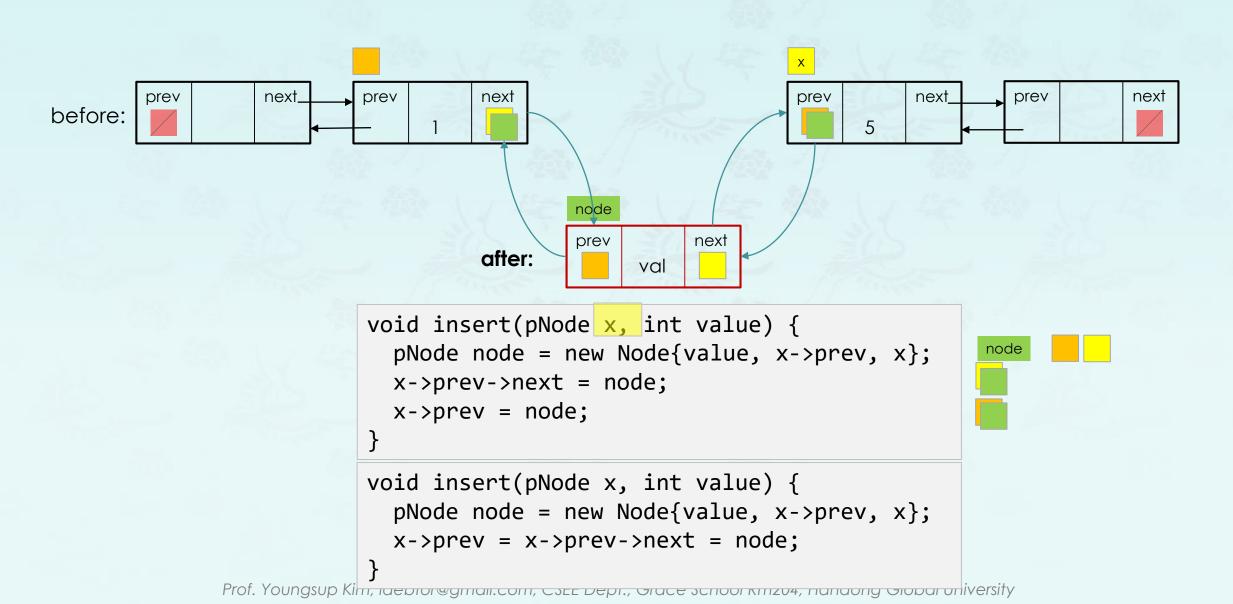
## Revisit - insert()

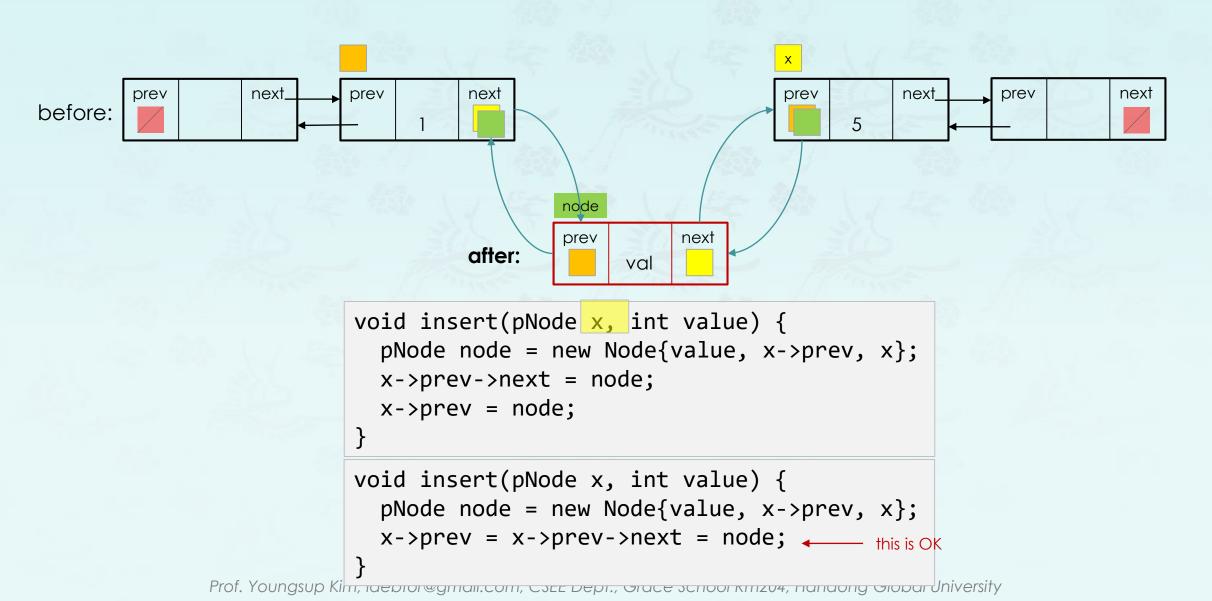
Identify where are to be changed or set?



It should be coded using value and info in x only.







#### push\_front()

```
// Inserts a new node at the beginning of the list, right before its
// current first node. The content of data item is copied(or moved) to the
// inserted node. This effectively increases the container size by one.
void push_front(pList p, int value) {
  insert(begin(p), value);
}
```



## pop\_front()

```
// Removes the first node in the list container, effectively reducing
// its size by one. This destroys the removed node.
void pop_front(pList p) {
  if (!empty(p)) erase(begin(p));
}
```



## Revisit: erase(), pop(), and find()

```
void erase(pNode x){
  x->prev->next = x->next;
  x->next->prev = x->prev;
  delete x;
void pop(pList p, int value){
  erase(find(p, value));
                                          Is this good enough?
       This code may not work some cases.
       How can you fix it?
void pop(pList p, int value){
  pNode node = find(p, value);
  if (node == p->tail || node == p->head) return;
  erase(node);
```

```
void erase(pList p, pNode x){
void erase(pNode x){
                                         if (x == end(p) \mid | x == p->head) return;
  x->prev->next = x->next;
                                         x \rightarrow prev \rightarrow next = x \rightarrow next;
  x->next->prev = x->prev;
  delete x;
                                         x->next->prev = x->prev;
                                         delete x;
void pop(pList p, int value){
  erase(find(p, value));
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  erase(node);
```

#### Revisit: erase(), pop(), and find()

```
void erase(pList p, pNode x){
void erase(pNode x){
                                      if (x == end(p) || x == p->head) return;
  x->prev->next = x->next;
                                      erase(x);
  x->next->prev = x->prev;
  delete x;
                                    void pop(pList p, int value){
void pop(pList p, int value){
  erase(find(p, value));
                                      erase(p, find(p, value));
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void pop(pList p, int value){
  pNode node = find(p, value);
  if (node == p->tail || node == p->head) return;
  erase(node);
```

Revisit: erase(), pop(), and find()

```
pNode find(pList p, int value){
  pNode x = begin(p);
  while(x != end(p)) {
    if (x->data == value) return x;
    x = x->next;
  }
  return x;
}
```

```
pNode find(pList p, int value){
  pNode x = begin(p);
  while(x != end(p) && x->data != value)
    x = x->next;
  return x;
}
```

- What does find() return if value not found?
   The "end" node which is not nullptr.
- Can we reduce the lines above by two?
- How about using for loop?

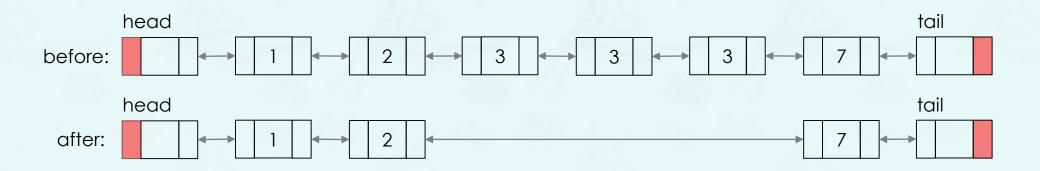
```
pNode find(pList p, int value){
  pNode x = begin(p);
  for (; x != end(p); x = x->next;)
    if (x->data == value) return x;
  return x;
}
```

### doubly linked list - pop\_all()\*

Write a pop\_all() which takes a list and deletes any nodes with a value given from the list. Ideally, the list should only be traversed once to have the time complexity, O(n).

```
void pop_all(pList p, int value) { // value = 3 in this example
  while (find(p, value) != end(p)) {
    pop(p, value);
  }
} // version.1
O(n)
O(n)
O(n)
```

The code above works, then what is the problem? What is the time complexity of each line and overall?

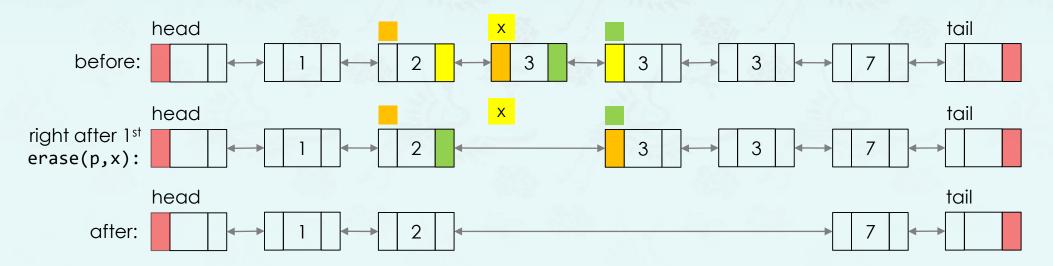


#### doubly linked list - pop\_all()\*

Write a pop\_all() which takes a list and deletes any nodes with a value given from the list. Ideally, the list should only be traversed once to have the time complexity, O(n).

```
void pop_all(pList p, int value) { // value = 3 in this example
  for (pNode x = begin(p); x != end(p); x = x->next)
   if (x->data == value) erase(p, x);
} // version.2 - fast, but buggy
```

- Does x point to the next node right after the first erase(p, x) call finishes? Are you sure?
- If you have not figured it out completely, you review erase() source code.
- Be able to answer why the code above may work in some machines or with small number of nodes.

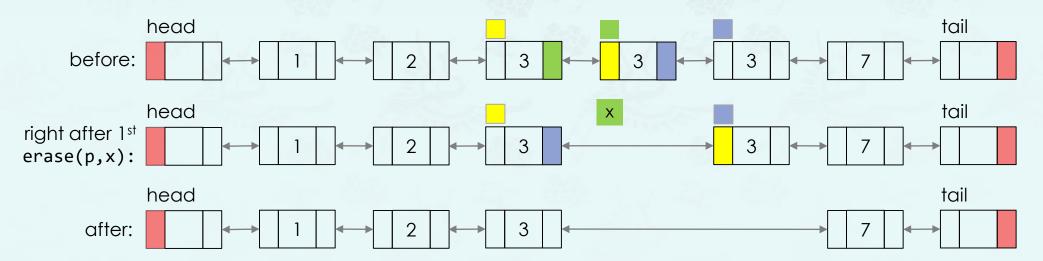


## doubly linked list - unique()\*

An unique() function removes extra nodes in sub-lists of equal value of nodes from the list. It removes all but the first node from every consecutive groups of equal nodes. This function is useful for sorted lists. The list should only be traversed once to have the time complexity, O(n).

```
void unique(pList p) {
  if (size(p) <= 1) return;
  for (pNode x = begin(p); x != end(p); x = x->next)
    if (x->data == x->prev->data) erase(p, x);
} // version.1 buggy - it may not work in some machines or for a large list.
```

We can proceed down the list and compare adjacent nodes. When adjacent nodes are the same, remove the second one. But you need to do something before and after the deletion. That is a tricky part of coding.



#### doubly linked list - sorted()

Implement two sorted() functions that returns true if a list is sorted and false otherwise.

- The one takes a list and a compare function pointer to compare two nodes.
   Using this function, the user can distinguish between an ascending list and a descending list.
- The other takes just a list and returns true if it is a sorted list, either ascending or descending.

```
bool sorted(pList p, int(*comp)(int a, int b)) {
   if (size(p) <= 1) return true;

int data = "set it to 1st node value"
   for (pNode x = "starts from second node"; x != end(p); x = x->next) {
     // your code here; return false as soon as out of order found
     // compare data and x->data
     data = x->data;
   }
   return true;
}
```

#### doubly linked list – helper functions

Write two compare functions which are used to invoke sorted().

```
int ascending (int a, int b) { return a - b; };
int descending(int a, int b) { return b - a; };
```

- Write two helper functions, more() and less() which are used to invoke push\_sorted().
   The more() or less() returns the node of which value is greater or smaller than a given value z firstly encountered, respectively.
- You may modify find() function to code these functions.

```
pNode more(pList p, int z) {
  pNode x = begin(p);
  // your code here

return x;
}

pNode less(pList p, int z) {
  pNode x = begin(p);
  // your code here

  return x;
}
```

```
pNode find(pList p, int value){
   pNode x = begin(p);
   while(x != end(p)) {
      if (x->data == value) return x;
      x = x->next;
   }
   return x;
}
```

### doubly linked list - push\_sorted()

Write push\_sorted function that inserts a node with value into a "sorted" list.

```
// inserts a new node with value in sorted order
void push_sorted(pList p, int value) {
  if sorted(p, "ascending_function_ptr")
    insert("find a node more() than value", value);
  else
    insert("find a node less() than value", value);
}
```

#### Note:

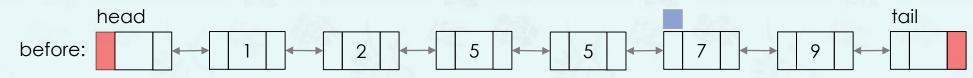
- If you use "using namespace std, the less() function may have a name conflict.
- Then use the scope resolution operator :: to access the function we defined.

#### doubly linked list - push\_sorted()

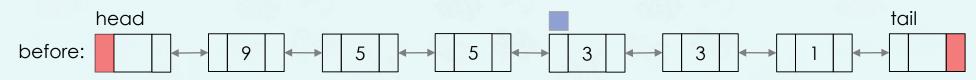
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}
```

Which node should be located to invoke insert() if value = 5?



Which node should be located to invoke insert() if value = 5?



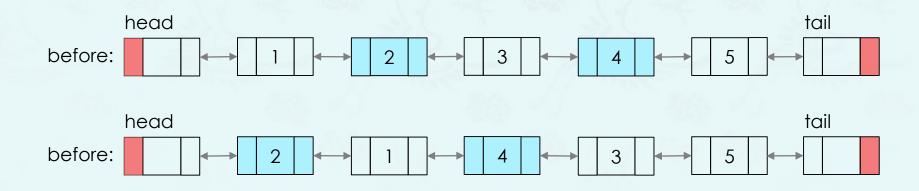
## doubly linked list - bubbleSort(), selectionSort(), insertionSort() and quickSort()

```
void bubbleSort(pList p, int(*comp)(int, int)) {
  if (sorted(p)) return reverse(p);

pNode x;
  pNode tail = end(p);
  for (pNode i = begin(p); i != end(p); i = i->next) {
    for (x = begin(p); x->next != tail; x = x->next) {
      if (comp(x->data, x->next->data) > 0)
            swap(x->data, x->next->data);
    }
    tail = x;
}
```

### doubly linked list - swap\_pairs()

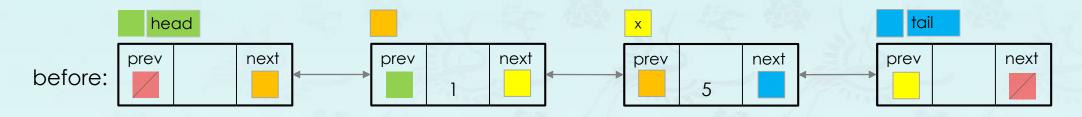
It swaps two values in adjacent nodes of the list. It does not swap the links, but the values only. If the list has an odd number of nodes, then the last one remains as it is. It goes through the list once, its time complexity is O(n).



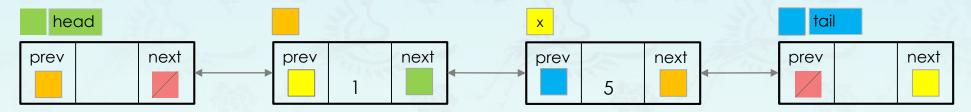
#### doubly linked list - reverse()

Write reverse() function that reverses the order of the nodes in the list. The entire operation does not involve the construction or destruction of any element. Nodes are not moved, but pointers are moved within the list. Its time complexity is O(n).

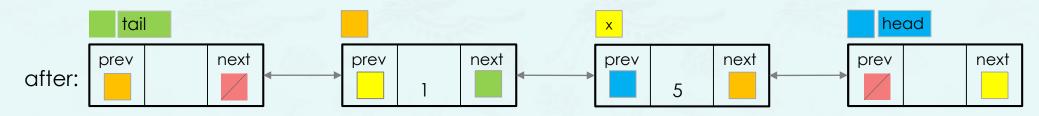
```
// reverses the order of the nodes in the list container. O(n)
void reverse(pList p) {
  if (size(p) <= 1) return;
  // hint: swap prev and next in every node including two sentinel nodes.
  // then, swap head and tail.
  // your code here
}</pre>
```



Step 1: swap prev and next in every node including two sentinel nodes.



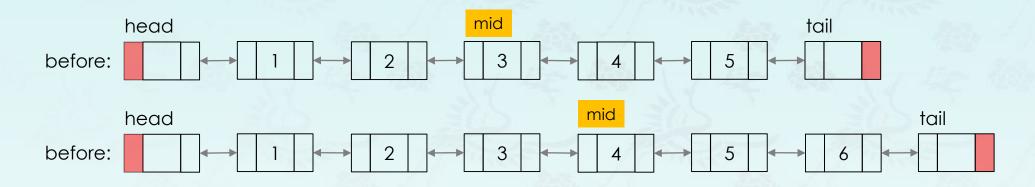
Step 2: swap head and tail node.



## doubly linked list - half()

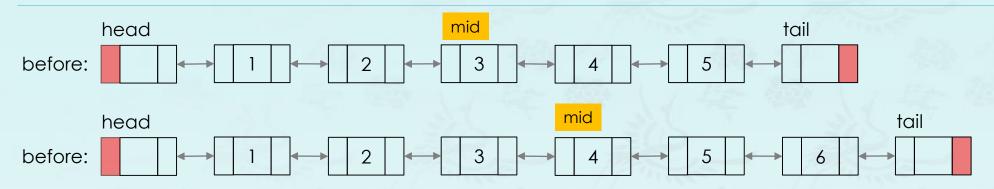
Write half() function that returns the mid node of the list.

- Even number of nodes, it returns the first node of the second half which is 6th node if there are ten nodes.
- If there are five (odd number) nodes in the list, it returns the third one (or middle one).



- **Method 1:** Get the size of the list O(n). Then scan to the halfway, breaking the last link followed.
- Method 2: It works by sending rabbit and turtle down the list: turtle moving at speed one, and
  rabbit moving at speed two. As soon as the rabbit hits the end, you know that the turtle
  is at the halfway point as long as the rabbit gets asleep at the halfway.

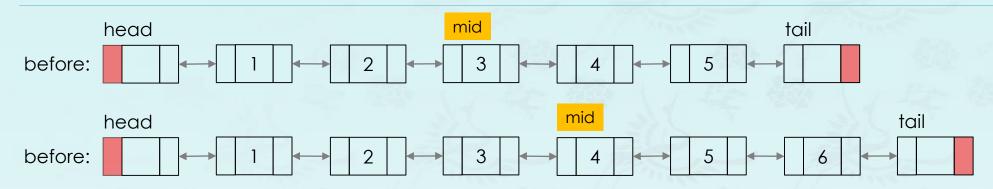
## doubly linked list - half()



- Method 1: Get the size of the list O(n). Then scan to the halfway, breaking the last link followed.
- If the list size n = 2 million nodes, What is T(n)?

```
pNode half(pList p) {
  int N = size(p);
  // go through the list and get the size
  // go through the list at the halfway
  // return the current pointer
}
```

## doubly linked list - half()



Method 2: It works by sending rabbit and turtle down the list: turtle moving at speed one, and
rabbit moving at speed two. As soon as the rabbit hits the end, you know that the turtle
is at the halfway point as long as the rabbit gets asleep at the halfway. O(n)

```
pNode half(pList p) {
  pNode rabbit = turtle = begin(p);
  pNode turtle = begin(p);
  while (rabbit != end(p)) {
    rabbit = rabbit->next->next;
    turtle = turtle->next;
  }
  return turtle;
} // buggy on purpose
• If the list size n = 2 million nodes, What is T(n)?
```

30

#### doubly linked list - randomize()

There are many ways to implement this function. The most well-known algorithm is called the Fisher-Yates shuffle. You may refer to Wikipedia or random.cpp for detail.

• This naive method we use here swaps each element with another element chosen randomly from all elements. Even though this is not the best approach, however, it is acceptable at this point.

```
void randomize(pList p) {
  int N = size(p);
  if (N <= 1) return;
  srand((unsigned)time(nullptr));

pNode curr = begin(p);
  while (curr != end(p)) {
    int x = rand_extended(N) % N; O(1)
    pNode xnode = find_by_index(p, x);
    swap(curr->data, xnode->data); O(1)
    curr = curr->next;
  }
}
```

- The time complexity of find\_by\_index(): \_\_\_\_\_
- The time complexity of randomize():

```
// a helper function
pNode find_by_index(pList p, int n_th) {
  int n = 0;
  pNode curr = begin(p);
  while (curr != end(p) && n_th != n)
    curr = curr->next;
  return curr;
}
```

#### doubly linked list - randomize()

Rewrite the randomize() such that it may have the time complexity of O(n).

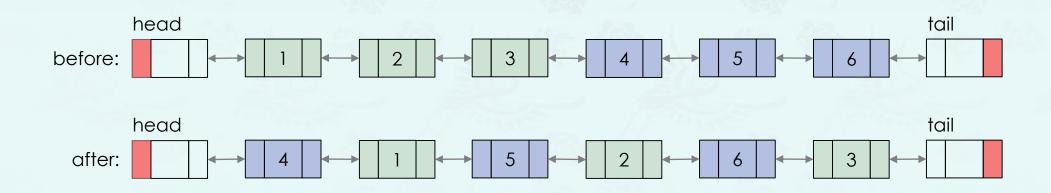
#### Hints:

- Rewrite the code such that it does not use find\_by\_index() of which the time complexity is O(n).
- How about extracting all the node values before while() loop and save them in an array?

```
void randomize(pList p) {
  int N = size(p);
  if (N <= 1) return;
  srand((unsigned)time(nullptr));
  // your code here
  pNode curr = begin(p);
  while (curr != end(p)) {
    int x = rand_extended(N) % N; O(1)
        pNode xnode = find_by_index(p, x);
        swap(curr->data, ...); O(1)
        curr = curr->next;
  }
}
```

- The time complexity of extracting values: \_\_\_\_\_
- The time complexity of randomize(): \_\_\_\_\_\_\_

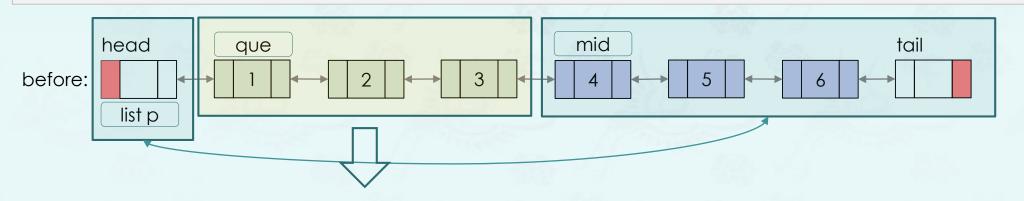
Implement shuffle()\*\* function that returns so called "perfectly shuffled" list. The first half and the second half are interleaved each other. The shuffled list begins with the second half of the original. For example, 1234567890 returns 6172839405.



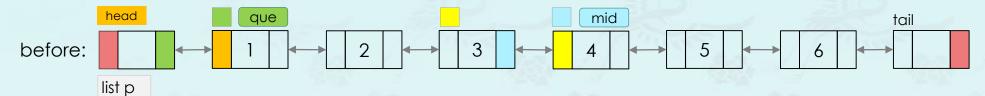
Implement shuffle()\*\* function that returns so called "perfectly shuffled" list. The first half and the second half are interleaved each other. The shuffled list begins with the second half of the original. For example, 1234567890 returns 6172839405.

#### Algorithm:

- 1) find the mid node of the list p to split it into two lists at the mid node.
- 2) remove the 1st half from the list p, and keep it as a list "que" to add.
- 3) set the list p head such that it points the "mid" of the list p.
- 4) keep on interleaving nodes until the "que" is exhausted.
  - save away next pointers of mid and que.
  - interleave nodes in the "que" into "mid" in the list of p. (insert the first node in "que" at the second node in "mid".)



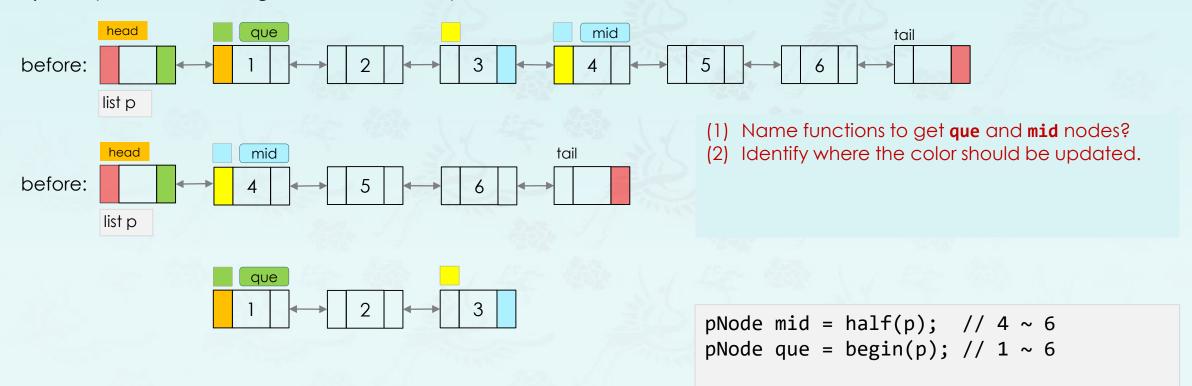
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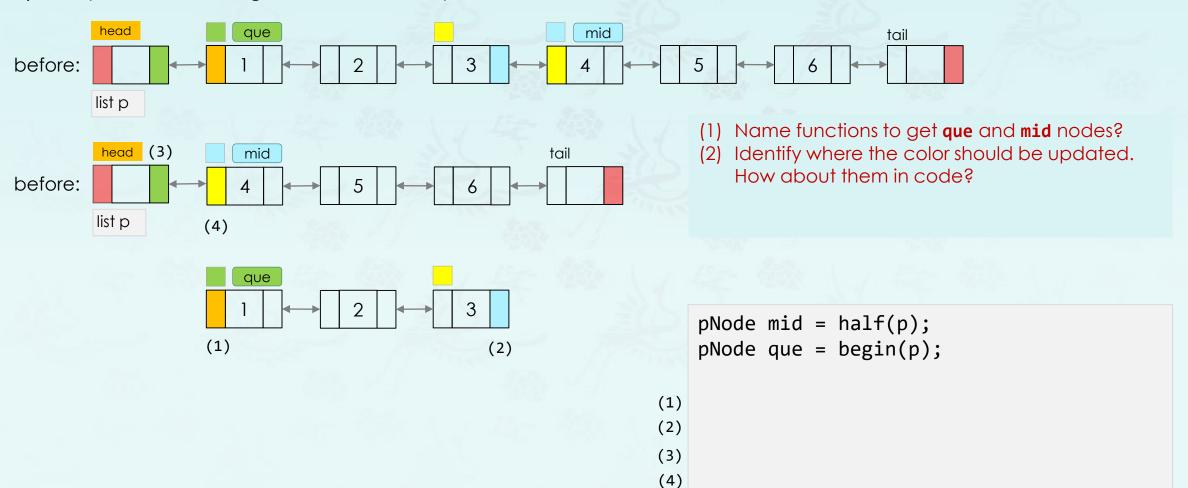
(1) Name functions to get que and mid nodes?

```
pNode mid = half(p); // 4 ~ 6
pNode que = begin(p); // 1 ~ 6
```

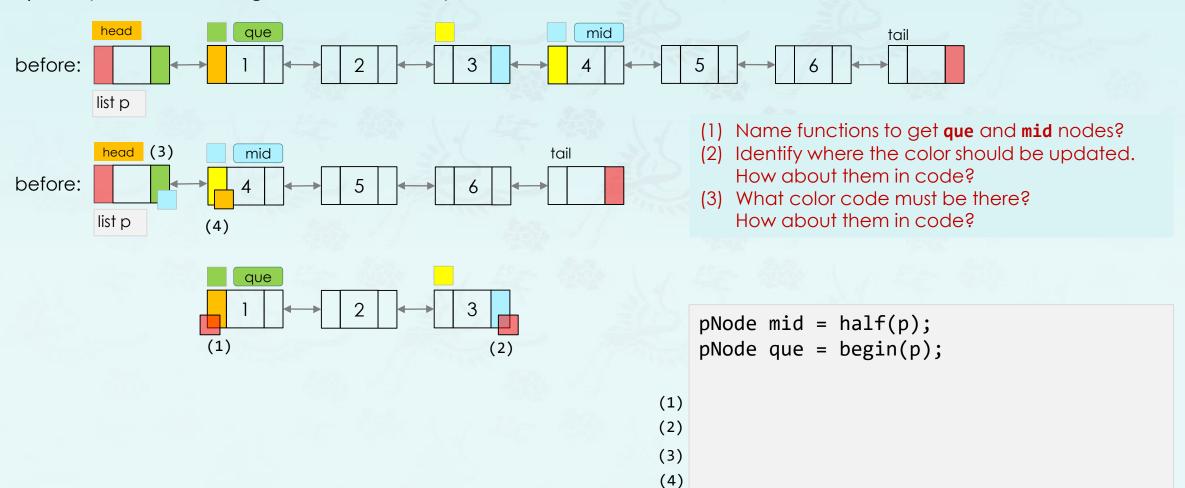
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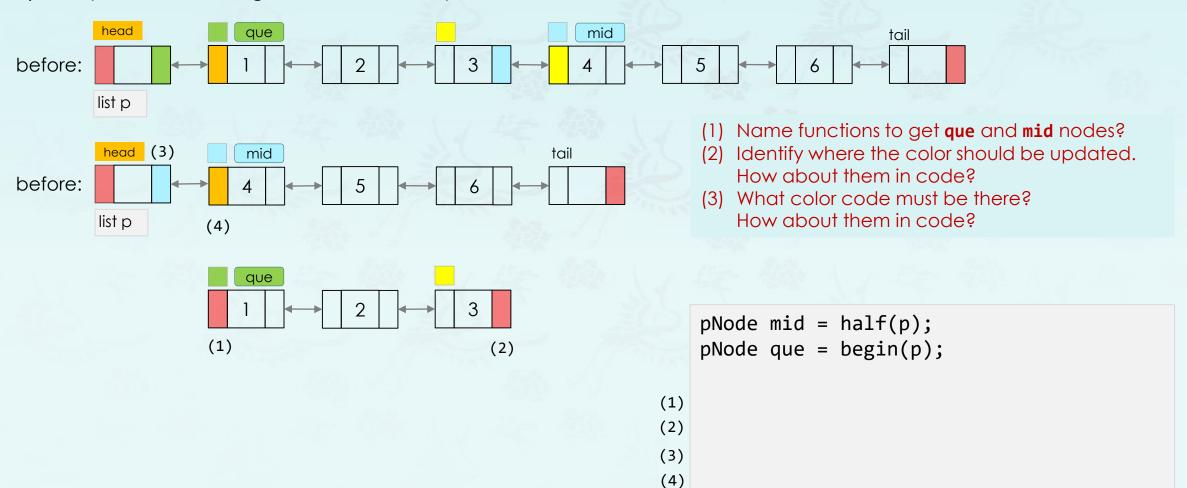
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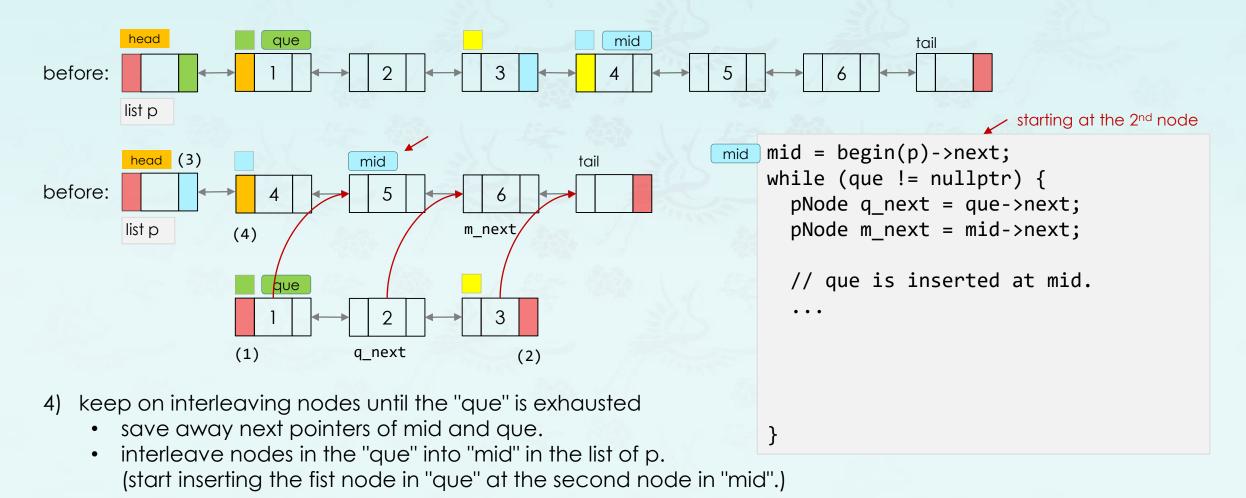
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# Summary & quaestio quaesti quaest

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