

Problem Solving and

19/2

Representation of Knowledge

* Problem Solving Agents: Goal-Based

 \Rightarrow They are goal-based agents. \Rightarrow One of the goal \rightarrow to maximize performance measures. \Rightarrow Goal formation \Rightarrow Problem formulation \Rightarrow Search

* Problem formulation is the process of deciding what actions and state to consider given a goal.

* The process of looking for sequence of actions that leads an agent to the goal is known as search.

 \Rightarrow Search Algorithm takes a problem as input and returns soln having sequence of actions. \Rightarrow Problem Formulation :-

- Initial state - the starting state

- Action

- Transition model - description of action results

- Goal test - Is Goal?

- Path cost - The funⁿ returns heuristic value used to estimate the performance measures.

* Problem Formulation of Vacuum Cleaner World.

1) States : $2 \times 2^2 = 8$

(total)



- 2) Initial state: Any state from the available states
- 3) Actions: Shift left, shift right, suck the dirt
- 4) Transition model:
- 5) Goal Test:
- 6) Path Cost: 1

* 8 - Puzzle Problem (Problem Formulation)

7	2	4
5		6
8	3	1

Start state

	1	2
3	4	5
6	7	8

Goal state

* 8 - Puzzle Problem

States :- 81

Initial :- All possible state with no ^{two} queen in same row, column or diagonal

Actions :- Moving queen to different col in its row

Transitional model :- stage change when queen is moved to new position

Goal Test :- check no two queen can attack each other.

Path cost :- No. of steps to reach solution.



Root finding Problem

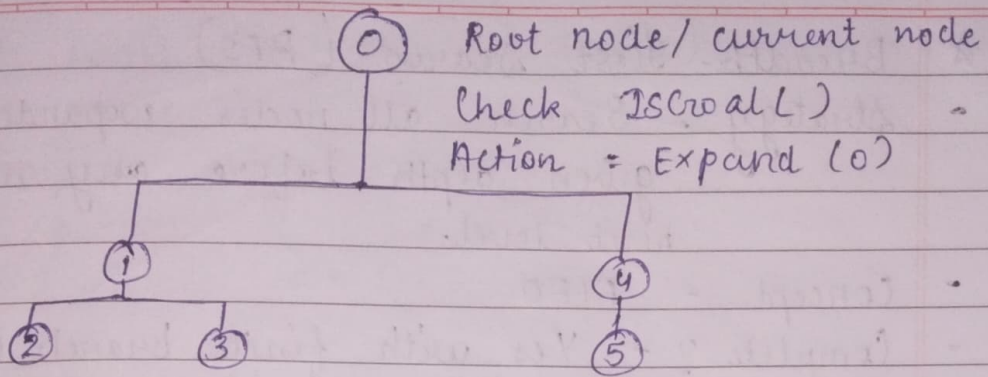
- 1> States :- Diff. values of x
- 2> Initial state :- selection of x
- 3> Actions :- Adjusting the guess for x based on finding method.
- 4> Transitional model :- How the value of x is updated.
- 5> Goal Test :- Root is found
- 6> Path cost :- No. of iterations or steps to reach the root.

Robot Navigation

- 1> States :-
- 2> Initial state :- Starting position of robot in environment.
- 3> Actions :- The movements that robot can make.
- 4> Transition model :- How robot's state change upon actions.
- 5> Goal Test :- Checking if robot has reached its destination.
- 6> Path cost :- Cumulative cost to reach goal.

★ Searching for Solution

- Solution? (Sequence of actions)
- Select Initial state
- Apply action & generate new state
- Check for goal & repeat
- return solution



Measures :-

- Completeness (Is the solⁿ guaranteed?)
- Optimality (Optimal solⁿ?)
- Time Complexity
- Space Complexity

Searching for Solⁿ (Search strategies)

Blind Search

- Breadth First Search
- Depth First Search

Heuristic Search

- A* Algo
- Greedy BFS

* Blind Search :- It is also known as uninformed search categories strategies.

- It traverse the search space until goal node is found.

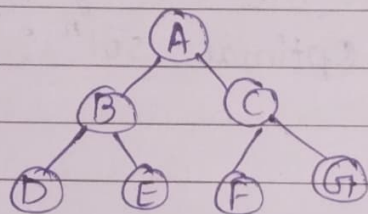
* Heuristic :- Also known as informed search strategies.

- Search Process takes place by traversing search space with applied rules / information.



★ Breadth-First Search (BFS)

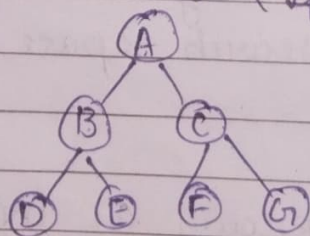
- Strategy - Search all nodes expanded at given depth before any node at next level.
- Concept - FIFO
- Complete? - Yes with finite branch (b)
- Space - Keep every node in memory
- Optimal? - Yes (If cost = 1)



Path :- ~~A-E-B-F-G-C-A~~ A-B-C-D-E-F-G

★ DFS

- Strategy - Search all nodes expanded at given depth before any node at deepest path.
- Concept - FILO
- Complete? - ~~Yes~~^{No} with infinite branch (b)
- Space - Keep every node in memory
- Optimal? - ~~Yes~~^{No} (If cost = 1)



Path :- A-B-D-E-C-F-G

★ Depth Limited Search (DLS)

- => DLS is DFS with a depth limit L
- => Nodes at depth limit are treated as leaves

→ depth limit ? (how to decide)

→ Performance ?

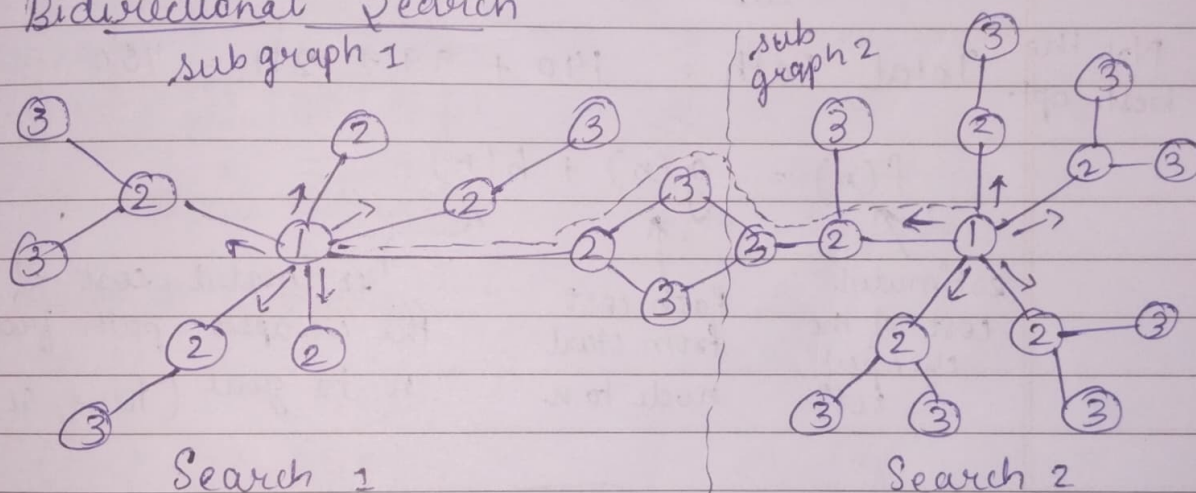
Incomplete if $L < d$

Non Optimal if $L > d$

Time & Space \leq DFS

★ ID - DFS (Iterative Deepening DFS)
Same as BFS

★ Bidirectional Search



⇒ It performs two search simultaneously one from the initial state to the goal state, the other from goal to initial state

⇒ It stops searching when either search reaches a state i.e. in middle of the other state.

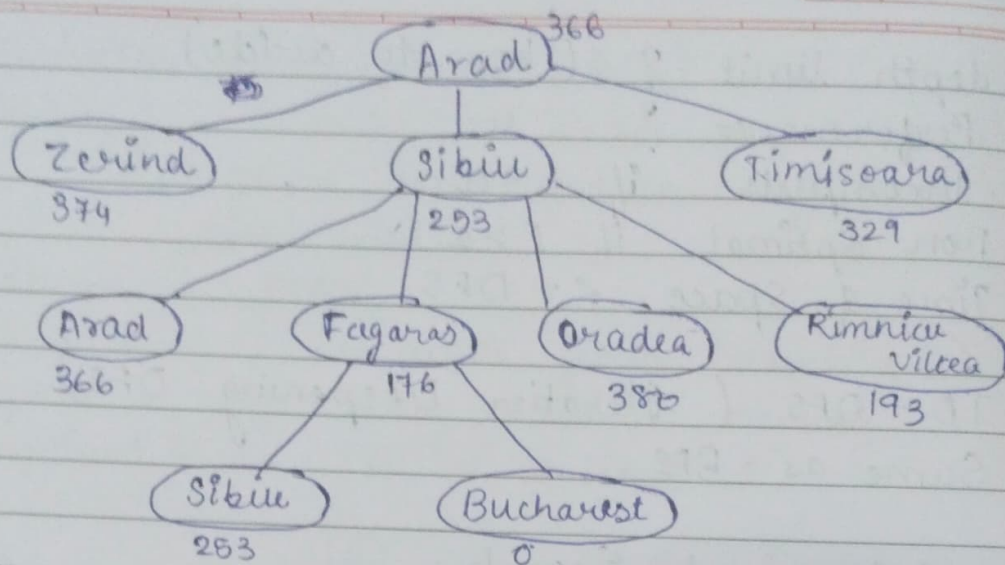
⇒ It provides complete & optimal solⁿ if both searches are BFS.

★ Informed Search strategies

Eg: $h(n)$ heuristic

$$f(n) = h(n)$$

Greedy Best-First Search

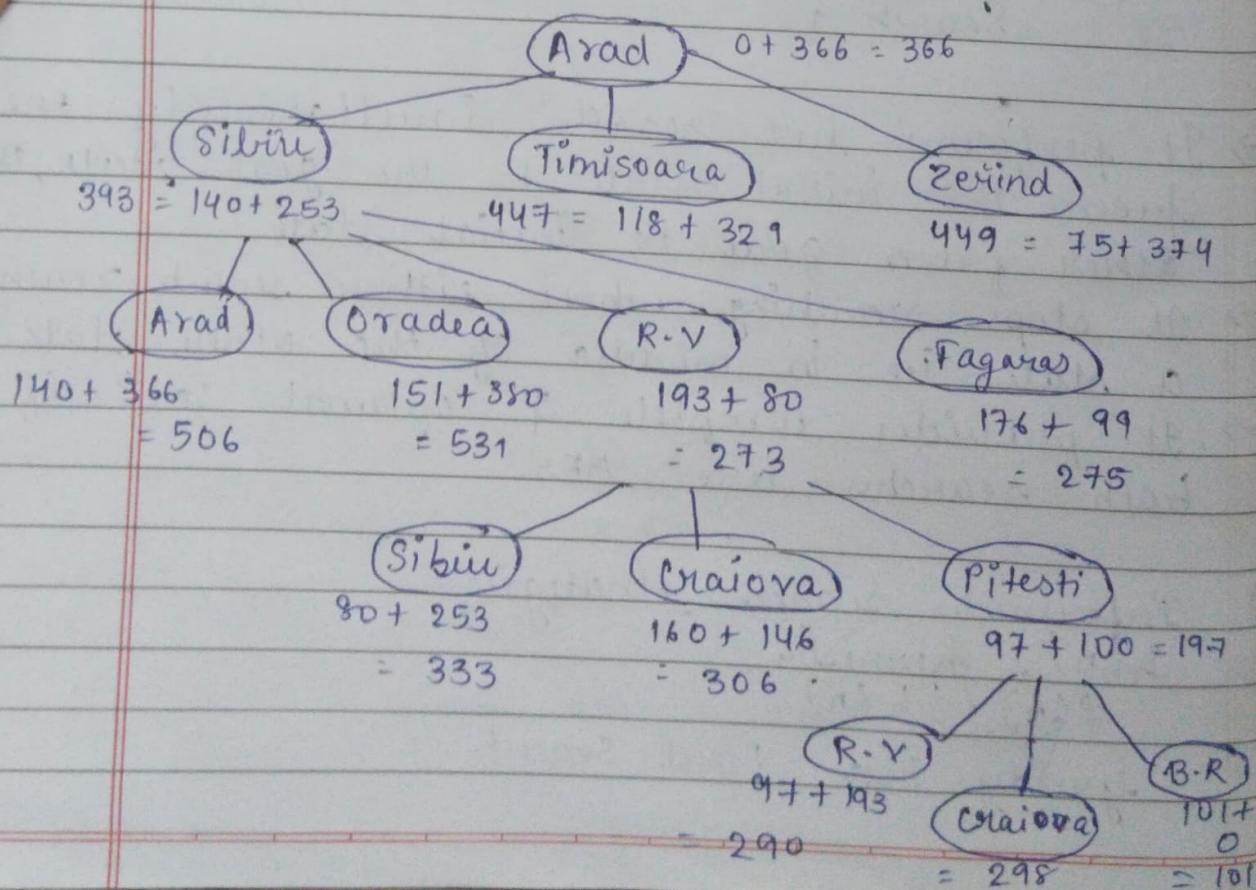
Eg: ~~#~~

Not the best opt.

$$\text{Total Path} = 140 + 99 + 211 = 450$$

$$f(n) = g(n) + h(n)$$

$f(n)$: estimated cost of the cheapest solⁿ
 $g(n)$: path cost from start node to n
 $h(n)$: estimated cost of the cheapest path from n to goal (here, SLD)














Total Path cost = 418 (140 + 80 + 97 + 101)

Informed Search (heuristic search)

- Greedy Best First Search ($f(n) = h(n)$)
- A* - search (A* - algo)
 $f(n) = h(n) + g(n)$

Wumpus world Problem

(1,4) 4			}}} (Breeze)	
(1,3) 3		☆ (Treasure)		}}} (Breeze)
(1,2) 2			}}} (Breeze)	
(1,1) 1		}}} (Breeze)		}}} (Breeze)
	1	2	3	4
	(1,1)	(2,1)	(3,1)	(4,1)

 Pit
 Wumpus
 ☆ - Treasure
 Agent
 }}} - Breeze
 Stench

PEAS @ Solution :-

- 1) (1,1) → (2,1)
- 2) (2,1) → (1,1)
- 3) (1,1) → (1,2)
- 4) (1,2) → (2,2)

Step: 1 Move to block [2,1] where agent smells breeze indicating adjacent block might have pit.

Step: 2 Agent moves back to [1,1]

Step: 3 Agent moves to [1,2] where agent feels stench indicating adjacent block might have wumpus

Step: 4 Agent notices the difference in blocks [2,1] and [1,2] and notices block [2,2] is safe.

Step: 5 Agent has now two opts either [3,2] or [2,3]



★

Logic :-

Syntax - (Well formed sentence)

Semantics - meaning of sentences

model - possible world (logically mathematical abstraction)

logical entailment -

e.g.

If a sentence α is true in model m we say that m satisfies α or m is a model of α

 $M(\alpha) \leftarrow$ set of all models of α

- Logical entailment - Logical entailment b/w sentences is the idea that a sentence follows logically from another sentence.

e.g.

 $\alpha \models B$ Sentence α entails the sentence B .

- Logical Inference is the process of deriving new sentences from the old one.

\Rightarrow Sound Inference algorithms derive only sentences that are entailed, complete algorithms derive all sentences that are entailed.

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Propositional Logic :-