





**UNIVERSIDAD ESTATAL DE MILAGRO U.N.E.M.I.**

**FACULTAD DE CIENCIAS A LA INGENIERÍA**

**PRIMER SEMESTRE DE INGENIERÍA DE SOFTWARE**

**ASIGNATURA: " CALCULO"**

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**TEMA:**

**METODO DE LAS CAPAS**

**DOCENTE:**

**ING. ARISTIDES BASCARDI**

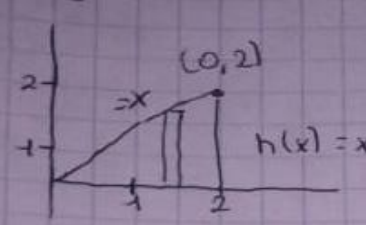
**CURSO:**

**AULA B1**

**Fecha de entrega:07/03/2021**

EN LOS EJERCICIOS 1 A 4 USAR EL METODO DE LAS CAPAS PARA FORMULAR Y EVALUAR LA INTEGRAL QUE EL VOLUMEN DEL SOLIDO GENERADO AL GIRAR LA REGION PLANA ALREDEDOR DEL EJE Y.

1)  $y = x$



Formula:  $V = 2\pi \int_0^2 p(x) h(x) dx$

$$V = 2\pi \int_0^2 (x) x dx$$

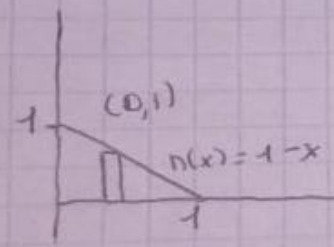
$$V = 2\pi \int_0^2 x^2 dx$$

$$V = 2\pi \left. \frac{x^3}{3} \right|_0^2$$

$$V = 2\pi \frac{8}{3}$$

$$V = \frac{16\pi}{3}$$
  

2)  $y = 1 - x$



Formula:  $V = 2\pi \int_a^b p(x) h(x) dx$

$$V = 2\pi \int_0^1 (1-x) x dx$$

$$V = 2\pi \int_0^1 x - x^2 dx$$

$$V = 2\pi \left( \int_0^1 x dx - \int_0^1 x^2 dx \right)$$

$$V = 2\pi \left( \frac{x^2}{2} - \frac{x^3}{3} \right) \Big|_0^1$$

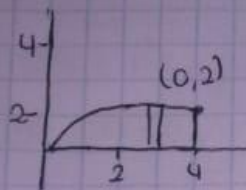
$$V = 2\pi \left( \frac{1}{2} - \frac{1}{3} \right)$$

$$V = 2\pi \times \frac{1}{6}$$

$$V = \pi \times \frac{1}{3}$$

$$V = \frac{\pi}{3}$$

3)  $y = \sqrt{x}$



Formula:  $U = 2\pi \int_a^b p(x) h(x) dx$

$$U = 2\pi \int_0^2 (\sqrt{x}) x dx$$

$$U = 2\pi \int x^{\frac{1}{2}} \cdot x dx$$

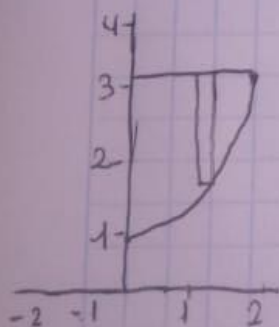
$$= 2\pi \int x^{\frac{3}{2}} dx$$

$$= 2\pi \left. \frac{2x^{\frac{5}{2}} \sqrt{x}}{5} \right|_0^2$$

$$= 2\pi \frac{8\sqrt{2}}{5}$$

$$= \frac{16\pi\sqrt{2}}{5}$$

4)  $y = \frac{1}{2}x^2 + 1$



Formula:  $U = 2\pi \int_a^b p(x) h(x) dx$

$$U = 2\pi \int_1^3 \left( \frac{1}{2}x^2 + 1 \right) x dx$$

$$= 2\pi \int_1^3 \frac{1}{2}x^3 + x dx$$

$$= 2\pi \left( \int \frac{1}{2}x^3 dx + \int x dx \right)$$

$$= 2\pi \left( \frac{x^4}{8} + \frac{x^2}{2} \right) \Big|_1^3$$

$$= 2\pi \cdot 14$$

$$= 28\pi$$