

# 2301 COL 202 Tutorial 3.4

Anubhav Pandey

TOTAL POINTS

**2 / 2**

QUESTION 1

1 Problem for Group 4 **2 / 2**

+ 1 pts Partially Correct

✓ + 2 pts *Correct solution*

+ 0 pts Wrong solution

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# COL 202 TUTORIAL

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## Tutorial 3, Group 4

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Group 4

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**SOLUTION : Problem 4**

Proof using the well-ordering principle. First we note that,

$$8 = 5 + 3;$$

$$9 = 3 \times 3;$$

$$10 = 5 \times 2;$$

Which, means that 8,9,10 can be represented as a sum of non-negative integer multiples of 3 and 5.

Now let's assume that there exists a non-empty subset  $C ::= \{x: x \text{ greater than } 10 \text{ \& } x \neq 3a + 5b, \text{ where } a, b \text{ are non-negative integer} \}$

So by well-ordering principle, there exists a  $s$  belongs to  $C$ , and  $s$  is the smallest element of  $C$ .

So,  $s-3$  does not belong to  $C$ , as  $s$  is the smallest element.

Which means we can find  $a, b$  in whole numbers such that

$$s-3 = 3a+5b$$

but it would mean that:

$$s = 3(a+1)+5b$$

This is a contradiction, therefore  $C$  is empty.

Therefore all elements greater than or equal to 8 can be written as the sum of non negative integral multiples of 3 and 5.

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