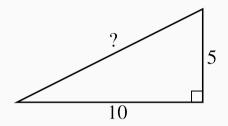
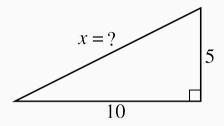
TRIGONOMETRY

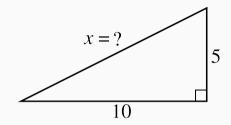
The Pythagorean Theorem

Practice Problems





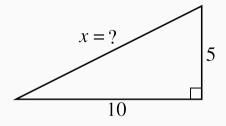




Solve for the unknown side.

Right triangle \Rightarrow Pythag. Thm:

$$a^2 + b^2 = c^2$$

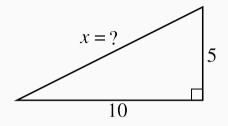


Solve for the unknown side.

Right triangle \Rightarrow Pythag. Thm:

$$a^2 + b^2 = c^2$$

 $c \Leftrightarrow \textbf{hypotenuse}$ (longest side)



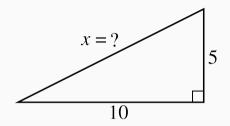
Solve for the unknown side.

Right triangle \Rightarrow Pythag. Thm:

$$a^2 + b^2 = c^2$$

 $c \Leftrightarrow \textbf{hypotenuse}$ (longest side)

 $a, b \Leftrightarrow \textbf{legs}$ (shorter sides)



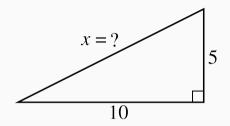
Right triangle \Rightarrow Pythag. Thm:

$$a^2 + b^2 = c^2$$

 $c \Leftrightarrow \textbf{hypotenuse}$ (longest side)

 $a, b \Leftrightarrow \textbf{legs}$ (shorter sides)

$$10^2 + 5^2 = x^2$$



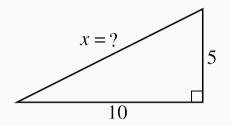
Right triangle \Rightarrow Pythag. Thm:

$$a^2+b^2=c^2$$

 $c \Leftrightarrow \textbf{hypotenuse}$ (longest side)

 $a, b \Leftrightarrow \mathbf{legs}$ (shorter sides)

$$10^2 + 5^2 = x^2$$
$$100 + 25 = x^2$$



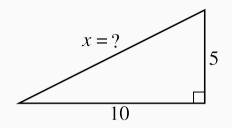
Right triangle \Rightarrow Pythag. Thm:

$$a^2 + b^2 = c^2$$

 $c \Leftrightarrow \textbf{hypotenuse}$ (longest side)

 $a, b \Leftrightarrow \mathbf{legs}$ (shorter sides)

$$10^2 + 5^2 = x^2$$
$$100 + 25 = x^2$$
$$125 = x^2$$



Right triangle \Rightarrow Pythag. Thm: $a^2 + b^2 = c^2$

 $c \Leftrightarrow \mathbf{hypotenuse}$ (longest side)

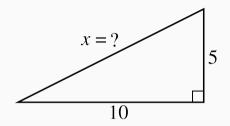
 $a, b \Leftrightarrow \mathbf{legs}$ (shorter sides)

$$10^{2} + 5^{2} = x^{2}$$

$$100 + 25 = x^{2}$$

$$125 = x^{2}$$

$$\sqrt{125} = x$$



Right triangle \Rightarrow Pythag. Thm: $a^2 + b^2 = c^2$

 $c \Leftrightarrow \mathbf{hypotenuse}$ (longest side) $a, b \Leftrightarrow \mathbf{legs}$ (shorter sides)

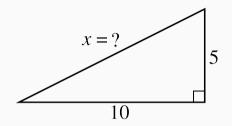
$$10^{2} + 5^{2} = x^{2}$$

$$100 + 25 = x^{2}$$

$$125 = x^{2}$$

$$\sqrt{125} = x$$

$$\sqrt{25 \cdot 5} = x$$



Right triangle \Rightarrow Pythag. Thm: $a^2 + b^2 = c^2$

 $c \Leftrightarrow \mathbf{hypotenuse}$ (longest side) $a, b \Leftrightarrow \mathbf{legs}$ (shorter sides)

$$10^{2} + 5^{2} = x^{2}$$

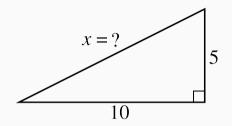
$$100 + 25 = x^{2}$$

$$125 = x^{2}$$

$$\sqrt{125} = x$$

$$\sqrt{25 \cdot 5} = x$$

$$5\sqrt{5} = x$$



Right triangle \Rightarrow Pythag. Thm: $a^2 + b^2 = c^2$

 $c \Leftrightarrow \mathbf{hypotenuse}$ (longest side) $a, b \Leftrightarrow \mathbf{legs}$ (shorter sides)

$$10^{2} + 5^{2} = x^{2}$$

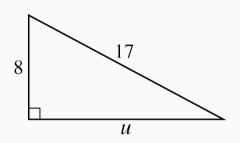
$$100 + 25 = x^{2}$$

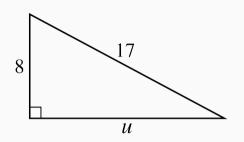
$$125 = x^{2}$$

$$\sqrt{125} = x$$

$$\sqrt{25 \cdot 5} = x$$

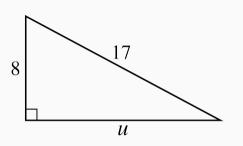
$$5\sqrt{5} = x$$





Right triangle \Rightarrow Pythag. Thm:

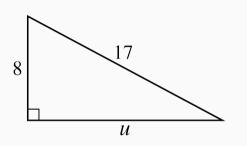
$$a^2 + b^2 = c^2$$



Right triangle \Rightarrow Pythag. Thm:

$$a^2 + b^2 = c^2$$

$$8^2 + u^2 = 17^2$$

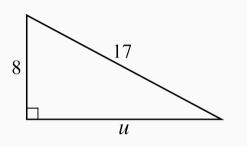


Right triangle \Rightarrow Pythag. Thm:

$$a^2 + b^2 = c^2$$

$$8^2 + u^2 = 17^2$$

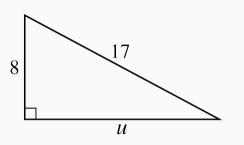
 $64 + u^2 = 289$



Right triangle \Rightarrow Pythag. Thm:

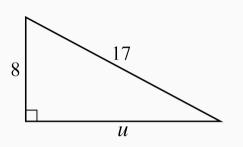
$$a^2 + b^2 = c^2$$

$$8^2 + u^2 = 17^2$$
$$64 + u^2 = 289$$
$$u^2 = 225$$



Right triangle \Rightarrow Pythag. Thm: $a^2 + b^2 = c^2$

$$8^{2} + u^{2} = 17^{2}$$
 $64 + u^{2} = 289$
 $u^{2} = 225$
 $u = \sqrt{225}$



Right triangle \Rightarrow Pythag. Thm: $a^2 + b^2 = c^2$

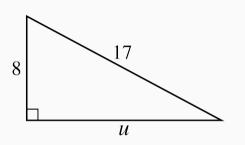
$$8^{2} + u^{2} = 17^{2}$$

$$64 + u^{2} = 289$$

$$u^{2} = 225$$

$$u = \sqrt{225}$$

$$u = \sqrt{15^{2}}$$



Right triangle \Rightarrow Pythag. Thm: $a^2 + b^2 = c^2$

$$8^{2} + u^{2} = 17^{2}$$

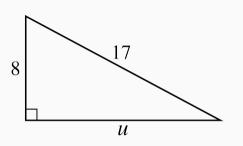
$$64 + u^{2} = 289$$

$$u^{2} = 225$$

$$u = \sqrt{225}$$

$$u = \sqrt{15^{2}}$$

$$u = 15$$



Right triangle \Rightarrow Pythag. Thm: $a^2 + b^2 = c^2$

$$8^{2} + u^{2} = 17^{2}$$

$$64 + u^{2} = 289$$

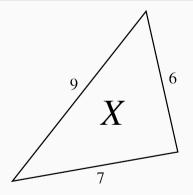
$$u^{2} = 225$$

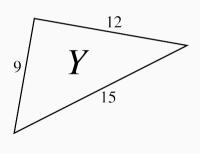
$$u = \sqrt{225}$$

$$u = \sqrt{15^{2}}$$

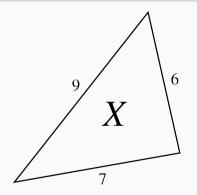
$$u = 15$$

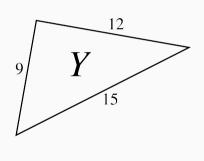
Which of the below are right triangles?





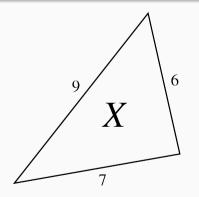
Which of the below are right triangles?

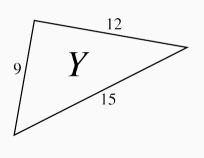




<u>If:</u> $a^2 + b^2 = c^2$; **Then:** Right triangle

Which of the below are right triangles?

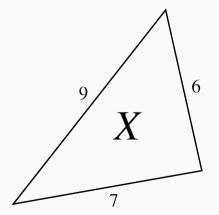




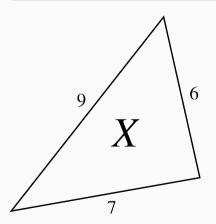
If: $a^2 + b^2 = c^2$; **Then:** Right triangle

(where c is longest side)

<u>If:</u> $a^2 + b^2 = c^2$; <u>Then:</u> Right triangle

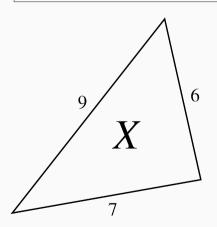


If:
$$a^2 + b^2 = c^2$$
; Then: Right triangle



$$7^2 + 6^2 \stackrel{?}{=} 9^2$$

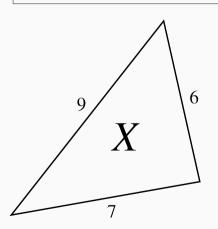
If: $a^2 + b^2 = c^2$; Then: Right triangle



$$7^2 + 6^2 \stackrel{?}{=} 9^2$$

 $49 + 36 \stackrel{?}{=} 81$

If: $a^2 + b^2 = c^2$; Then: Right triangle

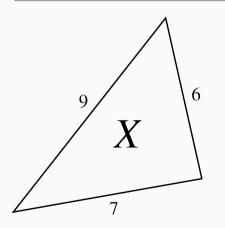


$$7^{2} + 6^{2} \stackrel{?}{=} 9^{2}$$

 $49 + 36 \stackrel{?}{=} 81$
 $85 \neq 81$

3, CONT.

If:
$$a^2 + b^2 = c^2$$
; **Then:** Right triangle

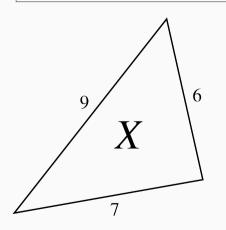


$$7^{2} + 6^{2} \stackrel{?}{=} 9^{2}$$

 $49 + 36 \stackrel{?}{=} 81$
 $85 \neq 81$

X is **not** a right triangle.

If:
$$a^2 + b^2 = c^2$$
; **Then:** Right triangle

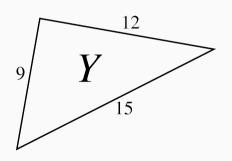


$$7^{2} + 6^{2} \stackrel{?}{=} 9^{2}$$

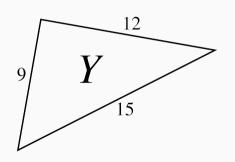
 $49 + 36 \stackrel{?}{=} 81$
 $85 \neq 81$

X is **not** a right triangle.

 $(85 > 81 \Rightarrow X \text{ is an } \textbf{acute} \text{ triangle.})$

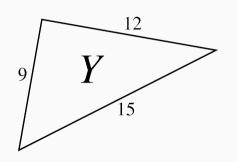


$$a^2 + b^2 \stackrel{?}{=} c^2$$

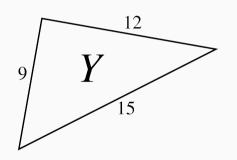


$$a^{2} + b^{2} \stackrel{?}{=} c^{2}$$

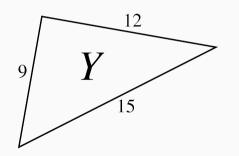
 $12^{2} + 9^{2} \stackrel{?}{=} 15^{2}$



$$a^{2} + b^{2} \stackrel{?}{=} c^{2}$$
 $12^{2} + 9^{2} \stackrel{?}{=} 15^{2}$
 $144 + 81 \stackrel{?}{=} 225$

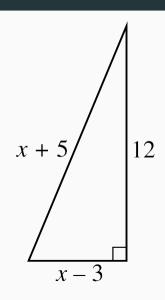


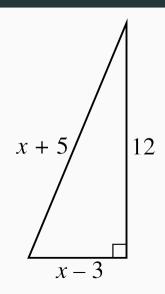
$$a^{2} + b^{2} \stackrel{?}{=} c^{2}$$
 $12^{2} + 9^{2} \stackrel{?}{=} 15^{2}$
 $144 + 81 \stackrel{?}{=} 225$
 $225 = 225$



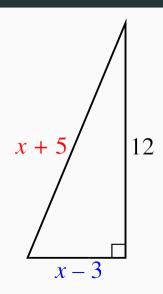
$$a^{2} + b^{2} \stackrel{?}{=} c^{2}$$
 $12^{2} + 9^{2} \stackrel{?}{=} 15^{2}$
 $144 + 81 \stackrel{?}{=} 225$
 $225 = 225$

Y **is** a right triangle.

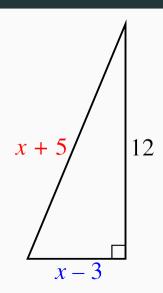




$$a^2 + b^2 = c^2$$

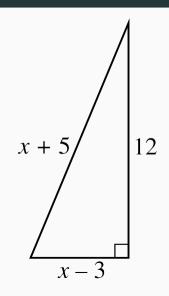


$$a^2 + b^2 = c^2$$



$$a^2 + b^2 = c^2$$

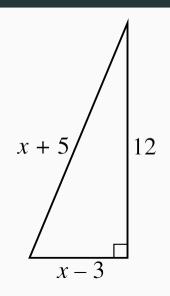
 $(x-3)^2 + 12^2 = (x+5)^2$



$$a^{2} + b^{2} = c^{2}$$

$$(x-3)^{2} + 12^{2} = (x+5)^{2}$$

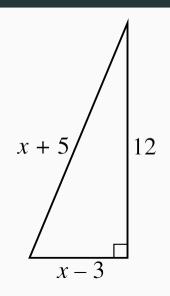
$$(x-3)(x-3) + 144 = (x+5)(x+5)$$



Solve for x.

$$(x-3)^2 + 12^2 = (x+5)^2$$
$$(x-3)(x-3) + 144 = (x+5)(x+5)$$
$$x^2 - 6x + 9 + 144 = x^2 + 10x + 25$$

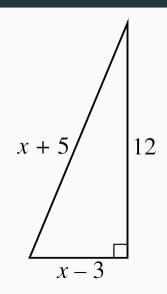
 $a^2 + b^2 = c^2$



Solve for *x*.

$$(x-3)^2 + 12^2 = (x+5)^2$$
$$(x-3)(x-3) + 144 = (x+5)(x+5)$$
$$x^2 - 6x + 9 + 144 = x^2 + 10x + 25$$

 $a^2 + b^2 = c^2$



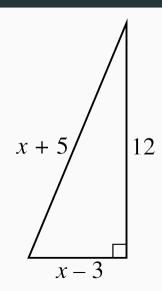
$$a^{2} + b^{2} = c^{2}$$

$$(x-3)^{2} + 12^{2} = (x+5)^{2}$$

$$(x-3)(x-3) + 144 = (x+5)(x+5)$$

$$x^{2} - 6x + 9 + 144 = x^{2} + 10x + 25$$

$$-6x + 153 = 10x + 25$$



$$a^{2} + b^{2} = c^{2}$$

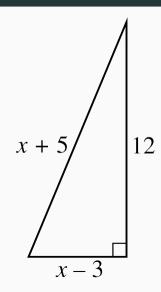
$$(x-3)^{2} + 12^{2} = (x+5)^{2}$$

$$(x-3)(x-3) + 144 = (x+5)(x+5)$$

$$x^{2} - 6x + 9 + 144 = x^{2} + 10x + 25$$

$$-6x + 153 = 10x + 25$$

$$128 = 16x$$



$$a^{2} + b^{2} = c^{2}$$

$$(x-3)^{2} + 12^{2} = (x+5)^{2}$$

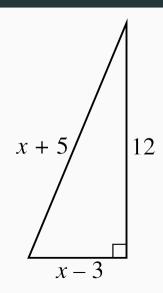
$$(x-3)(x-3) + 144 = (x+5)(x+5)$$

$$x^{2} - 6x + 9 + 144 = x^{2} + 10x + 25$$

$$-6x + 153 = 10x + 25$$

$$128 = 16x$$

$$8 = x$$



$$a^{2} + b^{2} = c^{2}$$

$$(x-3)^{2} + 12^{2} = (x+5)^{2}$$

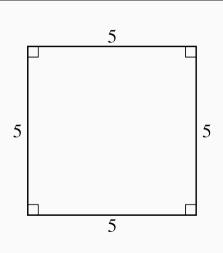
$$(x-3)(x-3) + 144 = (x+5)(x+5)$$

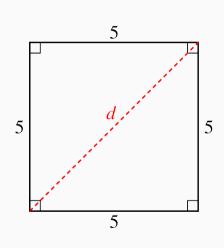
$$x^{2} - 6x + 9 + 144 = x^{2} + 10x + 25$$

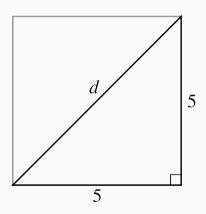
$$- 6x + 153 = 10x + 25$$

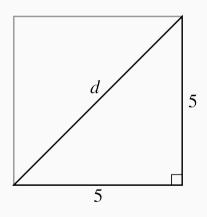
$$128 = 16x$$

$$8 = x$$

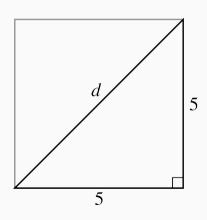




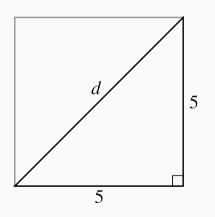




$$5^2 + 5^2 = d^2$$

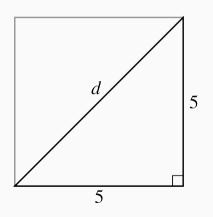


$$5^2 + 5^2 = d^2$$
$$25 + 25 = d^2$$

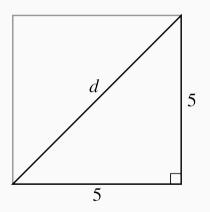


$$5^{2} + 5^{2} = d^{2}$$

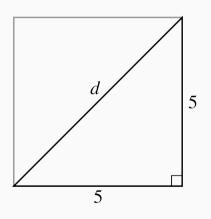
 $25 + 25 = d^{2}$
 $50 = d^{2}$



$$5^{2} + 5^{2} = d^{2}$$
$$25 + 25 = d^{2}$$
$$50 = d^{2}$$
$$\sqrt{50} = d$$



$$5^{2} + 5^{2} = d^{2}$$
$$25 + 25 = d^{2}$$
$$50 = d^{2}$$
$$\sqrt{50} = d$$
$$\sqrt{25 \cdot 2} = d$$



$$5^{2} + 5^{2} = d^{2}$$

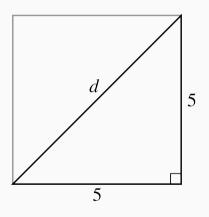
$$25 + 25 = d^{2}$$

$$50 = d^{2}$$

$$\sqrt{50} = d$$

$$\sqrt{25 \cdot 2} = d$$

$$5\sqrt{2} = d$$



$$5^{2} + 5^{2} = d^{2}$$

$$25 + 25 = d^{2}$$

$$50 = d^{2}$$

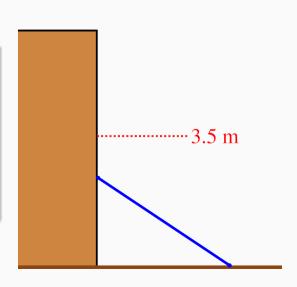
$$\sqrt{50} = d$$

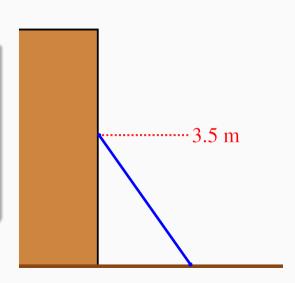
$$\sqrt{25 \cdot 2} = d$$

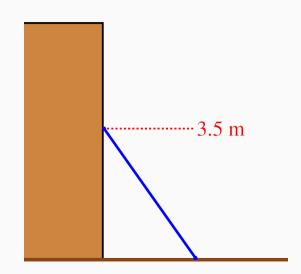
$$5\sqrt{2} = d$$

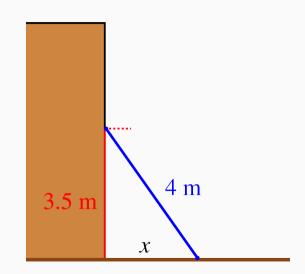
3.5 m

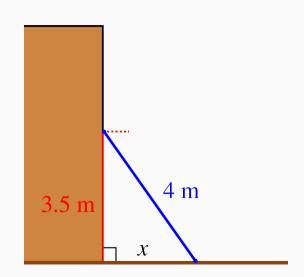
4 m -----3.5 m

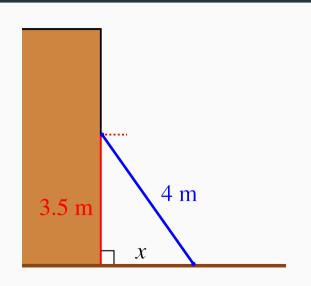




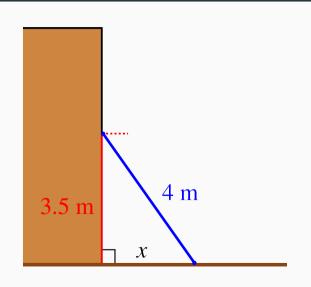




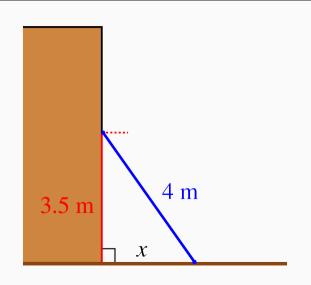




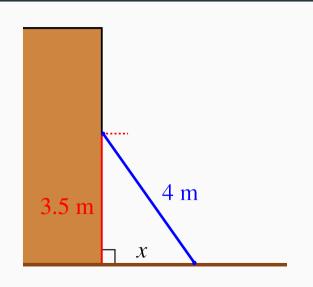
$$3.5^2 + x^2 = 4^2$$



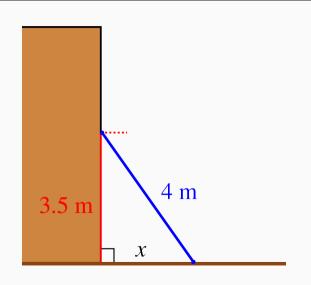
$$3.5^2 + x^2 = 4^2$$
$$12.25 + x^2 = 16$$



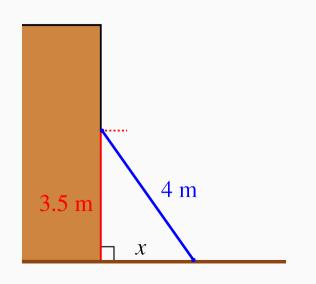
$$3.5^{2} + x^{2} = 4^{2}$$
 $12.25 + x^{2} = 16$
 $x^{2} = 3.75$



$$3.5^{2} + x^{2} = 4^{2}$$
 $12.25 + x^{2} = 16$
 $x^{2} = 3.75$
 $x = \sqrt{3.75}$



$$3.5^{2} + x^{2} = 4^{2}$$
 $12.25 + x^{2} = 16$
 $x^{2} = 3.75$
 $x = \sqrt{3.75} \approx 1.93649$



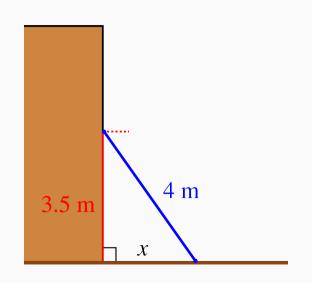
$$3.5^{2} + x^{2} = 4^{2}$$

$$12.25 + x^{2} = 16$$

$$x^{2} = 3.75$$

$$x = \sqrt{3.75} \approx 1.93649$$

$$x = 1.94$$

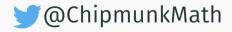


$$3.5^{2} + x^{2} = 4^{2}$$
 $12.25 + x^{2} = 16$
 $x^{2} = 3.75$
 $x = \sqrt{3.75} \approx 1.93649$
 $x = 1.94m$

THANKS FOR WATCHING!

Watch the rest of the videos on this topic!

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