

Cricket Mania

DiPS CodeJam 22

Prompt

A cricket championship of n teams is taking place, where each team plays all other teams once in a *round-robin* fashion. A team gets 5 points for winning a match, and 0 for loosing. It is assumed that no match will end in a draw or a tie. What is the **maximum possible difference** of points between the winning team and the second-placed team?

Solution

Simplifying the Problem

We can simplify the problem like so:

Find the maximum number of points by which a team can win a n -team competition, if each team plays every other team in round robin fashion. Teams get 5 points for a win and 0 points for a loss. Assume that there are no draws.

Input Format

- The first line of input contains a single integer t , denoting the number of test cases.
- The next t lines of input contain a single integer n .

Output Format

For each test case, output in a single line the maximum difference of points between first and second place.

Constraints

- $2 \geq n \geq 50$
- $1 \geq t \geq 50$

Sample Input/Output

Input	Output
5	120
49	105
43	90
36	70
28	30
13	

Solving the Problem

To get the maximum possible points, a team has to win every match they play. Let's assume that the team in 1st place won all the matches they played. In a *round-robin* fashion, each team will have played $n - 1$ matches. As the first team won all the matches they played, all the other teams have $n - 2$ matches, which they may win or lose. To maximize the difference in points between the first-placed team and second-placed team, points of the second-placed team must be the minimum possible, without changing its standing. This will happen only when the team wins and loses an equal number of matches. Applying this, we get the formula:

$$r(\text{number of rounds to play}) = n - 2$$
$$\text{minimum possible wins} = \lceil \frac{r}{2} \rceil = \lceil \frac{n - 2}{2} \rceil$$

Therefore (points/win = 5):

$$\begin{aligned} \text{points won by the first-placed team} &= 5 \cdot (n - 1) \\ \text{points won by the second-placed team} &= 5 \cdot \left(\lceil \frac{n - 2}{2} \rceil \right) \\ \therefore \text{difference in points} &= 5 \cdot (n - 1) - 5 \cdot \left(\lceil \frac{n - 2}{2} \rceil \right) \\ &= (5 * (n - 1)) - (5 * \text{ceil}((n - 2) / 2)) \end{aligned}$$

We will use this formula in the sample solution given below.

Sample Program

```
import math # import the math package for math.ceil()

numberOfCases = int(input()) # first line of input, number of testcases
while numberOfCases:
    n = int(input())          # while the number of remaining cases is not 0,
    team1 = 5*(n-1)           # take the next line of input,
    team2 = 5*math.ceil(((n-2)/2)) # calculate the score for the first-placed team,
    maxDiff = team1-team2      # calculate the score for the second-placed team,
    print(int(maxDiff))        # find the difference,
    numberOfCases-=1           # print the answer,
                              # and finally, decrement the number of cases.
```