

SUPPLEMENTARY MATERIAL

The supplementary material is organized as follows:

- Section A shows more detailed testing results on both training and unseen tasks in simulation. It also contains ablation studies which compare more TVF variants trained with different demo numbers.
- Section B discusses more details on the equivariance property of the dynamics of tabletop rearrangement.
- Section C shows more experiment details.

A. Simulation Results

In Tab. VI&VII, we show full testing results on 6 training and 8 unseen tasks. We show both the success rate and rate of progress for each task. For the rate of progress, partial credit is also given to trials which are partially completed. The rate of progress is defined as $\frac{\# \text{of blocks in target poses}}{\# \text{of blocks}}$. Besides TVF-Small and -Large, we also report results for another TVF variant, TVF-Extra. The tree depth of TVF-Extra is 5: the first 4 layers are expanded by the multi-modal action proposal module and the last layer is expanded by vanilla GCTN for runtime and computation consideration.

TVF variants outperform vanilla GCTN in most tasks, even with only one-step foresight (TVF-Small). With the increase of demo number per task, the success rates of all methods grow in general. A substantial performance improvement is observed when the demo number per task increases from 1 to 10. When the demo number increases further, the performance improves in general except in 100 and/or 1000 demos for some tasks. Similar results are also reported in [9]. On unseen tasks, TVF variants outperform GCTN in general. With the increase of the tree depth, the performance improves considerably from TVF-Small to TVF-Large. However, further increase of tree depth does not improve the performance substantially and sometimes even deteriorates performance. For example, in Plane Square (demo 1000), Plane T (demo 10), Stair 2 (demo 10), Twin Tower (demo 10), Stair 3 (demo 10, 1000), Pallet (demo 10, 100, 1000), and Rectangle (demo 1000), the performance of TVF-Extra becomes worse than the other two variants. This counter-intuitive result will be explained in the next paragraph. The only task in which the success rate improves dramatically with the increase of the tree depth is Building. TVF-Extra achieves a success rate of 40.0% in demo 1000, outperforming other methods by a large margin.

Similar conclusions can also be drawn from Tab. VIII&X where we show more results on more TVF variants. In these tables, we name each method with three letters “K”, “M” and “G”, which represent the number of clusters in K-Means Clustering, the number of steps expanded by the multi-modal action proposal module, and the number of steps expanded by vanilla GCTN. For TVF-Extra, the number of clusters is 3; the first 4 steps are expanded by the multi-modal action proposal module; the last step is expanded by vanilla GCTN. Thus, it is referred to as TVF-K3-M4-G1. TVF-Small and -Large correspond to TVF-K2-M1-G0 and TVF-K3-M3-G0, respectively. One additional result from Tab. VIII&X is that

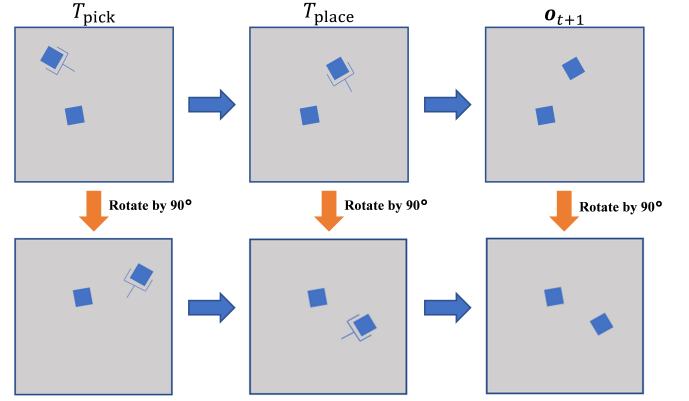


Fig. 7: **Tabletop Rearrangement.** When the current observation and the pick-and-place action are transformed by $g \in SE(2)$, the next-step observation will also be transformed by the same g .

using more clusters for the action proposal always improves performance.

The reason why in some cases the performance does not improve substantially for TVF-Extra is threefold:

- 1) If all the proposed actions are wrong at a given depth, the performance will not improve with the increase of tree depth.
- 2) If the task can be finished within very few steps, larger tree depth will not improve results.
- 3) If the prediction of the dynamics model becomes unreliable as the tree grows, larger tree depth may deteriorate the performance.

Therefore, to achieve better results with larger tree depth, the action proposal module and the dynamics model should improve simultaneously. Indeed, on training tasks, methods with larger tree depth and larger demo number achieve better results (Tab. VI). However, this pattern is not as obvious for unseen tasks (Tab. VII&X). We believe it is due to the well-known out-of-distribution problem: using more training data on training tasks will not improve the performance on unseen tasks. To further improve the performance on unseen tasks, one future direction is to improve the generalization capability.

B. $SE(2)$ Equivariance of Dynamics

We assume a pre-defined 2D frame is attached to the infinite tabletop plane. All the coordinates and poses defined below are relative to this frame. Our observation is the orthographic top-down view $\mathbf{o}_t : \mathbb{R}^2 \rightarrow \mathbb{R}^4$ of the whole tabletop workspace where $\mathbf{o}_t(u, v)$ gives the observed RGB and height value at position $\mathbf{p} = [u, v]^T \in \mathbb{R}^2$. $g \in SE(2)$ can be parameterized with $g = (R(\theta), \mathbf{q})$ in which $\mathbf{q} = [\Delta u, \Delta v]^T \in \mathbb{R}^2$ represents the translation; $R(\theta)$ represents the rotation:

$$R(\theta) = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix} \quad (4)$$

The group action of $SE(2)$ on $\mathbf{p} \in \mathbb{R}^2$ and its inverse are defined respectively as:

$$g \diamond \mathbf{p} = R(\theta)\mathbf{p} + \mathbf{q} \quad (5)$$

$$g^{-1} \diamond \mathbf{p} = R(\theta)^{-1}\mathbf{p} - R(\theta)^{-1}\mathbf{q} \quad (6)$$

TABLE V: **Hyperparameters**

Hyperparameter	Value
Learning Rate (VF)	1×10^{-4}
Minibatch Size (VF)	1
Training Steps (VF)	6×10^4
Learning Rate (Latent Dynamics)	1×10^{-4}
Minibatch Size (Latent Dynamics)	1
Training Steps (Latent Dynamics)	6×10^4
Tree Value Coefficient C (TVF)	1
Discount Factor γ (TVF)	0.99
K-Means Clustering Threshold Coefficient α (TVF)	0.01
Top N number in K-Means Clustering N (TVF)	100
Number of Rotation Bin for GCTN R (GCTN)	36

We define the group action of $SE(2)$ on \mathbf{o}_t as $g \cdot \mathbf{o}_t(\mathbf{p}) = \mathbf{o}_t(g^{-1} \diamond \mathbf{p})$. We denote $\mathbf{x}_t = (\mathbf{o}_t, \mathbf{a}_t)$ where $\mathbf{a}_t = (T_{\text{pick}}, T_{\text{place}}) \in SE(2) \times SE(2)$. The group action of $SE(2)$ on \mathbf{a}_t is defined as $g \odot \mathbf{a}_t = (g \circ T_{\text{pick}}, g \circ T_{\text{place}})$. \circ is the group operation of $SE(2)$ defined as $g_1 \circ g_2 = (R_1 R_2, R_1 \mathbf{q}_2 + \mathbf{q}_1)$. We then define the group action on \mathbf{x}_t as $g \bullet \mathbf{x}_t = (g \cdot \mathbf{o}_t, g \odot \mathbf{a}_t)$. The $SE(2)$ equivariance property of the dynamics function $f : \mathbf{x}_t \rightarrow \mathbf{o}_{t+1}$ can be written as:

$$f(g \bullet \mathbf{x}_t) = g \cdot f(\mathbf{x}_t) \quad (7)$$

Intuitively, Eq. 7 describes the following property of the dynamics of tabletop rearrangement: when the current observation and the picking and placing poses are transformed by $g \in SE(2)$, the next-step observation should also be transformed by g (Fig. 7). Our visual foresight (VF) model achieves translational equivariance by using a fully convolutional network (FCN) as the network architecture. We leave the extension to $SE(2)$ equivariance as future work. A promising direction is to format the input (*i.e.*, the observation and action) in a way such that it is compatible with an $SE(2)$ equivariant network architecture.

C. More Experiment Details

In real robot experiments, we pre-process the top-down observation reconstructed from the captured RGB-D image. We filter the tabletop background from the observation by setting thresholds for the height and the color channels. For each filtered pixel, we set the RGB and height value as zero. We observe in the experiment that GCTN is not able to learn well without pre-processing. Tab. V shows the hyperparameters we used for training our VF model, GCTN, and Latent Dynamics in the paper. More details can be found in our project website: <https://chirikjianlab.github.io/tvf/>

TABLE VI: **Simulation Experiment Results on Training Tasks.** We show the average success rate (%) / rate of progress (%) on the test data of each training task v.s. # of demonstrations (1, 10, 100, or 1000) per task in the training data. Higher is better.

Method	Row				Square			
	1	10	100	1000	1	10	100	1000
GCTN	6.7/34.4	98.3/99.4	95.0/98.3	100.0/100.0	0.0/32.9	93.3/96.7	65.0/84.2	93.3/96.7
TVF-Small	13.3/ 43.9	100.0/100.0	95.0/98.3	100.0/100.0	1.7/37.1	93.3/96.7	80.0/90.8	98.3/99.2
TVF-Large	15.0/43.3	100.0/100.0	95.0/98.3	100.0/100.0	1.7/37.9	100.0/100.0	90.0/96.7	100.0/100.0
TVF-Extra	15.0/42.2	100.0/100.0	95.0/98.3	100.0/100.0	3.3/40.4	98.3/99.6	91.7/97.1	100.0/100.0
Method	T-shape				Tower			
	1	10	100	1000	1	10	100	1000
GCTN	1.7/33.7	78.3/92.9	95.0/98.8	96.7/99.2	3.3/32.8	100.0/100.0	98.3/98.3	100.0/100.0
TVF-Small	3.3/35.8	93.3/96.7	96.7/99.2	96.7/98.4	5.0/43.9	98.3/99.4	100.0/100.0	100.0/100.0
TVF-Large	3.3/35.8	98.3/99.2	96.7/99.2	98.3/99.6	6.7/41.7	100.0/100.0	100.0/100.0	100.0/100.0
TVF-Extra	1.7/ 40.0	95.0/97.9	96.7/99.2	98.3/99.6	8.3/44.4	100.0/100.0	100.0/100.0	100.0/100.0
Method	Pyramid				Palace			
	1	10	100	1000	1	10	100	1000
GCTN	0.0/31.7	76.7/94.5	83.3/96.7	81.7/96.7	0.0/31.2	58.3/88.3	75.0/94.1	85.0/96.2
TVF-Small	1.7/33.9	70.0/92.0	85.0/95.9	63.3/90.3	0.0/ 38.1	71.7/92.4	78.3/94.8	85.0/96.7
TVF-Large	0.0/33.1	83.3/95.0	83.3/96.1	75.0/91.1	0.0/34.0	75.0/93.3	90.0/96.4	85.0/95.5
TVF-Extra	0.0/ 34.2	80.0/94.7	83.3/ 97.2	91.7/97.8	0.0/35.0	86.7/96.4	83.3/95.0	86.7/96.9

TABLE VII: **Simulation Experiment Results on Unseen Tasks.** We show the average success rate (%) / rate of progress (%) on the test data of each unseen task v.s. # of demonstrations (1, 10, 100, or 1000) per task in the training data. Higher is better.

Method	Plane Square				Plane T			
	1	10	100	1000	1	10	100	1000
GCTN	1.7/42.5	86.7/96.3	95.0/98.8	96.7/98.8	5.0/38.9	78.3/92.8	93.3/97.8	90.0/96.1
TVF-Small	5.0/44.6	98.3/99.6	96.7/99.2	100.0/100.0	3.3/43.9	90.0/96.7	100.0/100.0	96.7/98.9
TVF-Large	5.0/44.2	100.0/100.0	96.7/99.2	100.0/100.0	13.3/45.0	86.7/95.6	100.0/100.0	95.0/98.3
TVF-Extra	8.3/47.5	100.0/100.0	96.7/99.2	95.0/96.7	13.3/ 45.6	86.7/95.6	100.0/100.0	96.7/97.8
Method	Stair 2				Twin Tower			
	1	10	100	1000	1	10	100	1000
GCTN	3.3/37.8	83.3/94.4	46.6/82.2	68.3/89.4	0.0/26.7	90.0/95.8	55.0/72.8	85.0/96.1
TVF-Small	6.7/44.4	98.3/99.4	70.0/90.0	90.0/96.7	0.0/ 36.4	98.3/98.9	83.3/88.9	93.3/98.3
TVF-Large	5.0/41.7	98.3/99.4	93.3/97.2	100.0/100.0	0.0/30.3	95.0/98.1	86.7/91.7	90.0/95.0
TVF-Extra	5.0/41.7	96.7/97.8	93.3/97.2	100.0/100.0	0.0/29.7	95.0/98.1	88.3/93.6	98.3/99.2
Method	Stair 3				Building			
	1	10	100	1000	1	10	100	1000
GCTN	0.0/31.9	44.7/86.1	23.3/67.0	18.3/76.7	0.0/26.7	3.3/54.3	0.0/57.0	3.3/55.0
TVF-Small	0.0/ 38.1	71.7/92.8	33.3/74.4	48.3/85.3	0.0/ 29.7	6.7/ 60.0	8.3/65.6	15.0/65.0
TVF-Large	0.0/35.3	83.3/95.3	56.7/85.6	93.3/98.1	0.0/26.0	11.7/58.0	6.7/58.7	23.3/67.0
TVF-Extra	0.0/36.7	80.0/ 95.8	56.7/86.4	86.7/97.2	0.0/27.7	13.3/60.0	15.0/61.3	40.0/74.3
Method	Pallet				Rectangle			
	1	10	100	1000	1	10	100	1000
GCTN	0.0/31.9	26.7/83.3	48.3/78.1	31.7/85.0	0.0/30.3	26.7/83.9	25.0/68.3	41.7/79.5
TVF-Small	0.0/32.1	58.3/91.1	58.3/83.3	60.0/93.1	0.0/ 36.4	50.0/85.6	38.3/76.4	75.0/89.7
TVF-Large	0.0/32.5	71.7/95.2	70.0/91.0	93.3/98.7	0.0/32.2	76.7/93.3	66.7/88.1	95.0/98.6
TVF-Extra	0.0/ 34.6	68.3/94.4	68.3/90.4	80.0/96.9	1.7/32.8	80.0/93.9	70.0/89.7	90.0/96.4

TABLE VIII: **Ablation Study (10 Demos)**. We show the average success rate (%) on the test data of unseen tasks. The number of demonstrations per task in the training data is 10. Higher is better.

Method	Plane Square	Plane T	Stair 2	Twin Tower	Stair 3	Building	Pallet	Rectangle
TVF-K2-M1-G0	98.3	90.0	98.3	98.3	71.7	6.7	58.3	50.0
TVF-K2-M2-G0	100.0	86.7	93.3	98.3	70.0	3.3	58.3	58.3
TVF-K2-M3-G0	100.0	85.0	93.3	98.3	73.3	6.7	58.3	58.3
TVF-K2-M4-G0	100.0	83.3	93.3	95.0	68.3	8.3	65.0	55.0
TVF-K2-M4-G1	100.0	83.3	93.3	98.3	66.7	13.3	63.3	56.7
TVF-K3-M1-G0	100.0	90.0	100.0	96.7	66.7	5.0	76.7	71.7
TVF-K3-M2-G0	100.0	88.3	98.3	93.3	75.0	5.0	60.0	71.7
TVF-K3-M3-G0	100.0	86.7	98.3	95.0	83.3	11.7	71.7	76.7
TVF-K3-M4-G0	100.0	86.7	96.7	96.7	71.7	6.7	68.3	83.3
TVF-K3-M4-G1	100.0	86.7	96.7	95.0	80.0	13.3	68.3	80.0

TABLE IX: **Ablation Study (100 Demos)**. We show the average success rate (%) on the test data of unseen tasks. The number of demonstrations per task in the training data is 100. Higher is better.

Method	Plane Square	Plane T	Stair 2	Twin Tower	Stair 3	Building	Pallet	Rectangle
TVF-K2-M1-G0	96.7	100.0	70.0	83.3	33.3	8.3	58.3	38.3
TVF-K2-M2-G0	96.7	100.0	75.0	78.3	35.0	0.0	61.7	40.0
TVF-K2-M3-G0	96.7	100.0	85.0	80.0	41.7	1.7	60.0	50.0
TVF-K2-M4-G0	96.7	100.0	85.0	83.3	45.0	6.7	58.3	51.7
TVF-K2-M4-G1	96.7	100.0	85.0	86.7	40.0	3.3	60.0	50.0
TVF-K3-M1-G0	95.0	100.0	83.3	90.0	53.3	10.0	60.0	55.0
TVF-K3-M2-G0	96.7	100.0	91.7	95.0	58.3	1.7	70.0	58.3
TVF-K3-M3-G0	96.7	100.0	93.3	86.7	56.7	6.7	70.0	66.7
TVF-K3-M4-G0	96.7	100.0	93.3	88.3	56.7	11.7	66.7	73.3
TVF-K3-M4-G1	96.7	100.0	93.3	88.3	56.7	15.0	68.3	70.0

TABLE X: **Ablation Study (1000 Demos)**. We show the average success rate (%) on the test data of unseen tasks. The number of demonstrations per task in the training data is 1000. Higher is better.

Method	Plane Square	Plane T	Stair 2	Twin Tower	Stair 3	Building	Pallet	Rectangle
TVF-K2-M1-G0	100.0	96.7	90.0	93.3	48.3	15.0	60.0	75.0
TVF-K2-M2-G0	98.3	98.3	90.0	96.7	60.0	5.0	75.0	78.3
TVF-K2-M3-G0	100.0	98.3	91.7	98.3	55.0	10.0	76.7	90.0
TVF-K2-M4-G0	100.0	98.3	91.7	98.3	58.3	23.3	73.3	91.7
TVF-K2-M4-G1	100.0	98.3	91.7	98.3	60.0	35.0	75.0	93.3
TVF-K3-M1-G0	100.0	95.0	98.3	96.7	81.7	15.0	88.3	83.3
TVF-K3-M2-G0	98.3	95.0	100.0	98.3	85.0	15.0	93.3	96.7
TVF-K3-M3-G0	100.0	95.0	100.0	90.0	93.3	23.3	93.3	95.0
TVF-K3-M4-G0	100.0	95.0	100.0	96.0	88.3	41.7	86.7	88.3
TVF-K3-M4-G1	95.0	96.7	100.0	98.3	86.7	40.0	80.0	90.0