

# Assignment 3

Fei Li<sup>1</sup>

---

<sup>1</sup>Department of Computer Science, George Mason University, Fairfax, VA  
22030. Email: fli4@gmu.edu

## Problem

*Consider that you have two databases named A and B. Each database contains  $n$  values. Without loss of generality, you can assume that all these  $2n$  values are distinct. The median value is defined as the  $n$ -th smallest value among these  $2n$  values.*

*You need to find the median by sending queries to these two databases. In each query, you specify a value  $k$  so that the database returns you the  $k$ -th smallest value in that database. For example, if A has the values  $1, 2, \dots, n$ , and if you send a query with value 10, then A sends the value 10 to you.*

*Since each query is expensive, you want to minimize the number of queries sent to these two databases. Give an algorithm that finds the median value using at most  $O(\log n)$  queries. Show this algorithm and show its running time analysis.*