

II Construct RLG  
and FA corresponding to the reg.  $0^* (10+01)^*$

RLG

$0^*$ :  $S \rightarrow 0S/\epsilon$



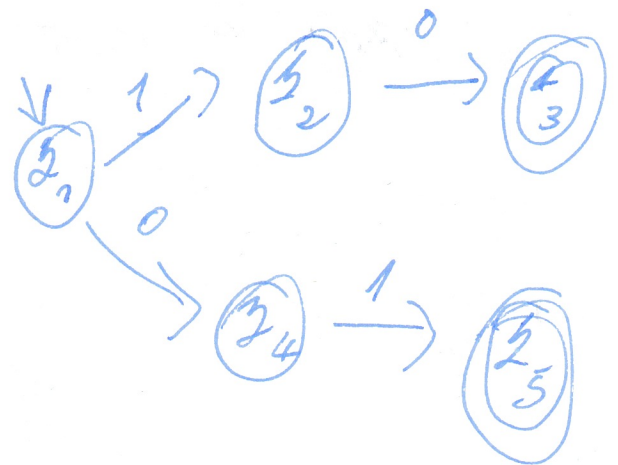
$10$ :  $S \rightarrow 1S_1$   
 $S_1 \rightarrow 0$



$01$ :  $S \rightarrow 0S_1$   
 $S_1 \rightarrow 1$



$(10+01)$ :  $S \rightarrow 1S_1/0S_2$   
 $S_1 \rightarrow 0$   
 $S_2 \rightarrow 1$



$(10+01)^*$ :  $S \rightarrow 1S_1/0S_2/\epsilon$   
 $S_1 \rightarrow 0S$   
 $S_2 \rightarrow 1S$



$0^* (10+01)^*$ :

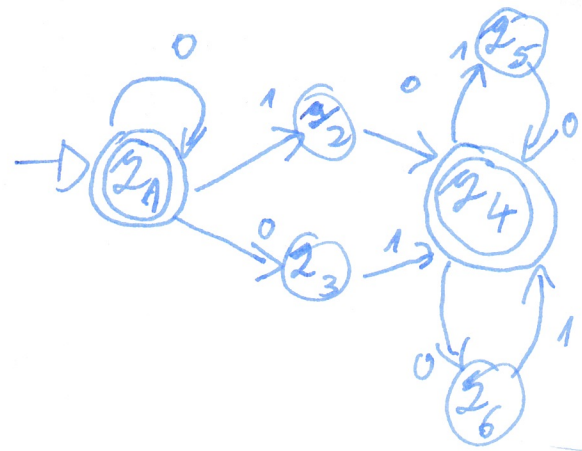
$S \rightarrow 0S_1 | \epsilon$

$S_1 \rightarrow 0S_1 | 010S_2 | 1S_3$

$S_2 \rightarrow 1 | 1S_4$

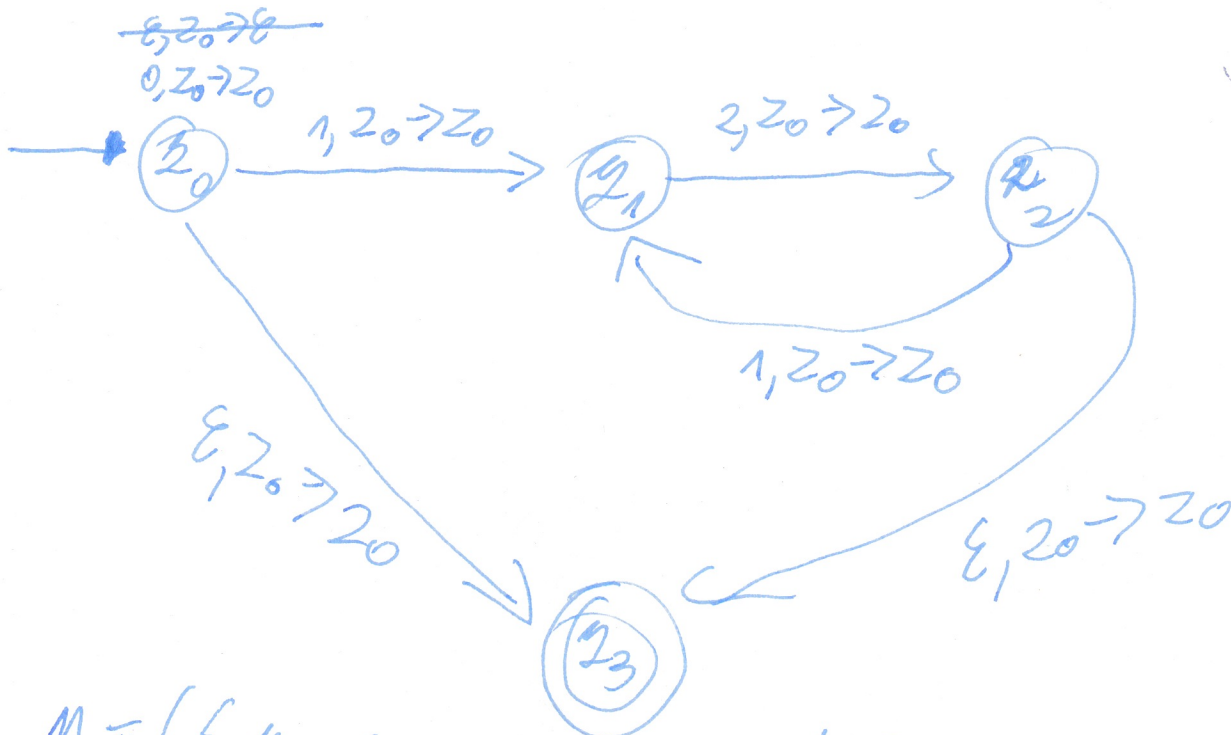
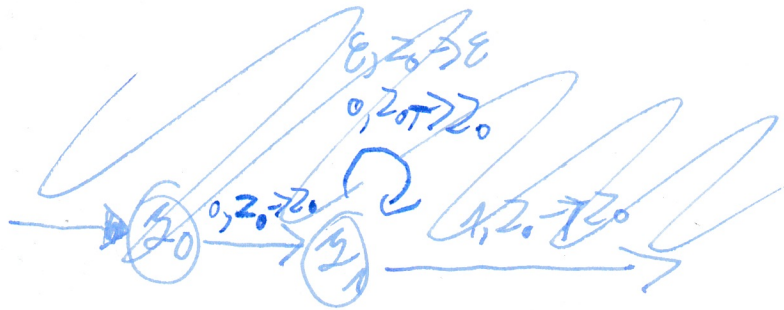
$S_3 \rightarrow 0 | 0S_4$

$S_4 \rightarrow 0S_2 | 1S_3$



III Construct a push-down automaton corresp. to the lang.:

$$L = \{ 0^m (12)^n \mid m > 0, n > 0 \}$$



$$M = (\underbrace{\{q_0, q_1, q_2, q_3\}}_Q, \underbrace{\{0, 1, 2\}}_\Sigma, \underbrace{\{\epsilon, 0\}}_\Gamma, \delta, q_0, Z_0, \{q_3\})$$

$$\delta: Q \times (\Sigma \cup \{\epsilon\}) \times \Gamma \rightarrow P(Q \times \Gamma^*)$$

V

label	operator	arg 1	arg 2	result
(1)	:=	0	—	1
(2)	:=	1	—	n
(3)	:=	1	—	i
(4)	>	i	n	t <sub>1</sub>
(5)	goto	t <sub>1</sub>	—	(17)
(6)	mod	a	2	t <sub>2</sub>
(7)	=	t <sub>2</sub>	0	t <sub>3</sub>
(8)	goto	t <sub>3</sub>	—	(12)
(9)	*	n	i	t <sub>4</sub>
(10)	:=	t <sub>4</sub>	—	n
(11)	goto	—	—	(14)
(12)	+	1	i	t <sub>5</sub>
(13)	:=	t <sub>5</sub>	—	1
(14)	+	i	1	t <sub>6</sub>
(15)	:=	t <sub>6</sub>	—	i
(16)	goto	—	—	(4)
(17)				



I

1)  $L_1 = \{\epsilon, 0, 1\}$ ,  $L_2 = \{0, 11\}$   
which elems. belong to  $L_1 \cup L_2$ ?

a)  $\epsilon$  b) 10 c) 0 d) 11

$R = a, c, d$

2) Which of the following strings belong to  $a(cd)^*$ ?

a) aaba b) a  
c) aabab d) ba

$R = b, c$

3) Consider the grammar with productions

$S \rightarrow RT$ ;  $R \rightarrow Ra$ ;  $T \rightarrow b$ . unproductive:

a)  $R$  b)  $R, S$  c)  $R, S, T$  d)  $S$

$R: a$  (?)

both  $R$  and  $S$  are unproductive

4) Consider the FA



which seq. belongs to  $L(M)$ ?

a) 00 b) 01 c) 011 d) 010

$R = a, b, d$

IV Consider the grammar  $G = (\{S, A, B, C, D\}, \{0, 1, a, b, c, d, e\}, P, S)$  where:

$P: S \rightarrow CD; 0$

$D \rightarrow dB$

$B \rightarrow D/e$

$C \rightarrow cA$

$A \rightarrow e/bA$

Construct FIRST and FOLLOW for the nonterminals of the grammar.