

Data Structure and Algorithm, Spring 2025

Mini-Homework K

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Due: 13:00:00, Tuesday, June 10, 2025

Rules and Instructions

- Any form of cheating, lying, or plagiarism will not be tolerated. Students can get zero scores and/or fail the class and/or be kicked out of school and/or receive other punishments for those kinds of misconducts.
- Discussions on course materials and homework solutions are encouraged. But you should write the final solutions alone and understand them fully. Books, notes, and Internet resources (including chatGPT) can be consulted, but not copied from.
- Since everyone needs to write the final solutions alone, there is **absolutely no need to lend your homework solutions and/or source codes to your classmates at any time**. In order to maximize the level of fairness in this class, lending and borrowing homework solutions are both regarded as dishonest behaviors and will be punished according to the honesty policy.
- In each mini-homework, we will have one programming problem that is closely connected to what we have taught in the class. The purpose of the problem is for you to *practice* what you have learned, before conquering the more challenging problems in other homework sets.
- Like other programming problems, you should write your code in C programming language, and then submit the code via the *DSA Judge*:

<https://dsa-2025.csie.org/>.

Each day, you can submit up to 5 times for each problem. The judge system will compile your code with

```
gcc [id].c -static -O2 -std=c11
```

- For debugging in the programming part, we strongly suggest you produce your own test-cases with programs and/or use tools like `gdb` or compile with flag `-fsanitize=address` to help you solve issues like illegal memory usage. For `gdb`, you are strongly encouraged to use compile flag `-g` to preserve symbols after compiling.

Note: For students who use IDE (VScode, DevC++...) you can modify the compile command in the settings/preference section. Below are some examples:

- `gcc [id].c -O2 -std=c11 -fsanitize=address # Works on Unix-like OS`
- `gcc [id].c -O2 -std=c11 -g # use it with gdb`

- The score of the part that is submitted after the deadline will get some penalties according to the following rule:

$$Late\ Score = \max \left(\left(\frac{5 \times 86400 - Delay\ Time(sec.)}{5 \times 86400} \right) \times Original\ Score, 0 \right)$$

Please note that the “gold medal” of the class cannot be used on mini-homework problems.

- If you have questions about this mini-homework, please go to the Discord channel and discuss the issues with your classmates. This is *strongly preferred* because it will provide everyone with a more interactive learning experience. If you really need email clarifications, you are encouraged to include the following tag in the subject of your email:
 - The subject should contain one tag, "[hwk]", specifying the problem where you have questions. For example, "[hwk] Will there be a repeated number?". Adding these tags potentially allows the TAs to track the status of each email and to provide faster responses to you.
 - If you want to provide your code segments to us as part of your question, please upload it to [Gist](#) or similar platforms and provide the link. Please remember to protect your uploaded materials with proper permission settings. Screenshots or code segments directly included in the email are discouraged and may not be reviewed.

Red-Black Tree (15 pts)

Problem Description

In this problem, we ask you to implement the `LEFT-ROTATE` and `RIGHT-ROTATE` operations on a red-black tree. The operations are illustrated in the figure below and are identical to the ones introduced in the lecture. The pseudo code of `LEFT-ROTATE` is given as follows, and you will need to implement your own `RIGHT-ROTATE` (which is a with-lecture quiz, remember?). Note that after the rotations, some red-black tree properties might not be satisfied anymore. In addition, the problem does not require your program to insert or delete a tree node, and thus there is no need for the implementations of these operations.

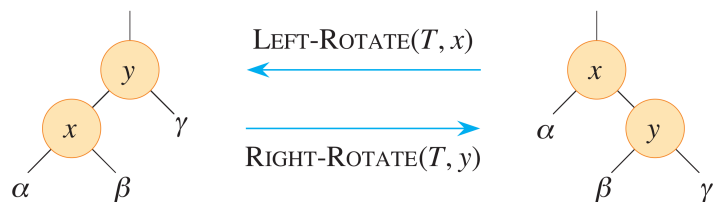
Here we define the *depth* of a tree node x as the number of nodes in the path from node x to the root of the tree, excluding x . For example, the root has a depth of 0 as the root itself is excluded. The child nodes of the root has a depth of 1, counting only the root node in the path. We can also define *black-depth* of a red-black tree node y as the number of *black* nodes in the path from node y to the root of the tree, excluding y . For example, the black-depth of the root of a red-black tree is always 0, and the black-depth of the child nodes of the root is always 1.

In this problem, we will ask you to output the depth and the black-depth of certain nodes in the tree.

`LEFT-ROTATE(T, x)`

```

1   $y = x.right$ 
2   $x.right = y.left$ 
3  if  $y.left \neq T.nil$ 
4       $y.left.p = x$ 
5   $y.p = x.p$ 
6  if  $x.p == T.nil$ 
7       $T.root = y$ 
8  elseif  $x == x.p.left$ 
9       $x.p.left = y$ 
10 else  $x.p.right = y$ 
11  $y.left = x$ 
12  $x.p = y$ 
```



Input

The first line has a single positive integer number N , which specifies the number of internal nodes (non-NIL nodes) in the given red-black tree.

Each of the following N lines includes the information of one node, and the nodes in these N lines are given in the order of the pre-order traversal of the given red-black tree. In each line, we have one character C and one integer number k . C represents the color of the node, and is either R, representing red, or B, representing black. k is the key of the node. Note that since a legal red-black tree is also a legal binary search tree, the list of nodes with the order of a pre-order traversal can uniquely determine a red-black tree.

The next line has a single integer number M , which specifies the number of operations to be performed on the given red-black tree. Each of the following M lines is in one of these three formats.

1. L k – You should execute $\text{LEFT-ROTATE}(T, x)$, where x is the node with key k .
2. R k – You should execute $\text{RIGHT-ROTATE}(T, y)$, where y is the node with key k .
3. P k – You should output information about the node with the given key k , in the output format specified below.

A single space character is used to separate different items in the same line.

You should execute all operations according to the given order. We ensure that all keys of the given red-black tree are *distinct*.

Output

For each given P operation with key k , output one line in this format – LK RK BD D, with a single space character separating consecutive numbers. Assume node x is the node with key k . LK is the key of the left child node of x , RK is the key of the right child node of x . If the left child of x is NIL, then LK is -1 . The same applies to RK . Finally, BD is the black-depth of x and D is the depth of x .

Constraints

- $2 \leq N \leq 3 \times 10^5$
- $1 \leq M \leq 3 \times 10^5$
- $0 \leq k \leq 10^9$
- We ensure that all rotation and output operations can be executed successfully.
- Although it is possible that a search in the given tree have a worst-case running time of $O(n)$, we ensure that the judge will not produce a Time Limit Exceeded (TLE) error in our test cases if you execute the operations in the given order.

Sample Testcases

Sample Input 1

5
B 2
B 1
B 4
R 3
R 5
5
P 4
L 2
P 4
R 4
P 4

Sample Output 1

3 5 1 1
2 5 0 0
3 5 1 1

Sample Input 2

2
B 2
R 1
3
P 2
R 2
P 2

Sample Output 2

1 -1 0 0
-1 -1 0 1