

Ch22. Vectors in the Plane

1. Definition of a geometric vector:

A geometric vector  $\overrightarrow{PQ}$  is a directed line segment with a direction and a magnitude.

The magnitude of  $\overrightarrow{PQ}$  is its length, denoted by  $|\overrightarrow{PQ}|$  or  $|\overrightarrow{PQ}|$

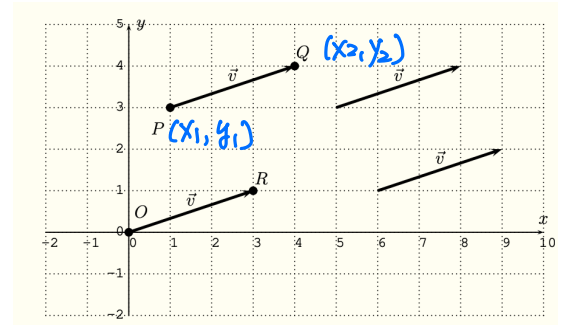
2. How to find and present a vector:

Given a vector  $\vec{v} = \overrightarrow{PQ}$ . We call  $P$  the initial point and  $Q$  the terminal point.

We find  $\vec{v} = \overrightarrow{PQ}$  by  $P(x_1, y_1)$  and  $Q(x_2, y_2)$ :

$$\vec{v} = (x_2 - x_1)\mathbf{i} + (y_2 - y_1)\mathbf{j} \text{ or } \langle x_2 - x_1, y_2 - y_1 \rangle,$$

where  $\mathbf{i} = \langle 1, 0 \rangle$  and  $\mathbf{j} = \langle 0, 1 \rangle$ .



The magnitude of  $\vec{v}$  is  $\|\vec{v}\| =$  \_\_\_\_\_.

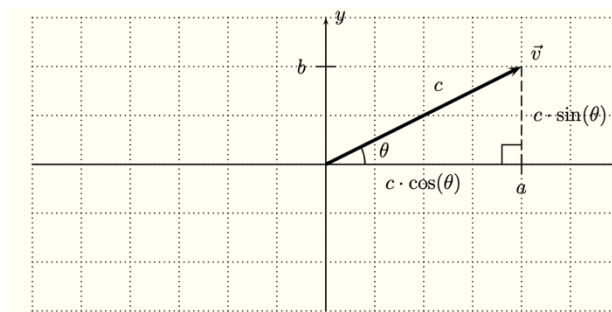
Any vectors with the same \_\_\_\_\_ and \_\_\_\_\_ are equivalent.

3. Direction angle:

Let  $\vec{v} = \langle a, b \rangle = \overrightarrow{OR}$  be a vector with original point \_\_\_\_\_ as the initial point of  $\vec{v}$  and  $R( \quad, \quad )$  as the terminal point of  $\vec{v}$ .

The \_\_\_\_\_ of  $\vec{v}$  is the angle  $\theta$  determined by  $\overrightarrow{OR}$ :

$c =$  \_\_\_\_\_ is the \_\_\_\_\_ of  $\vec{v}$  and we have  $\sin(\theta) =$  \_\_\_\_\_,  $\cos(\theta) =$  \_\_\_\_\_, and  $\tan(\theta) =$  \_\_\_\_\_.



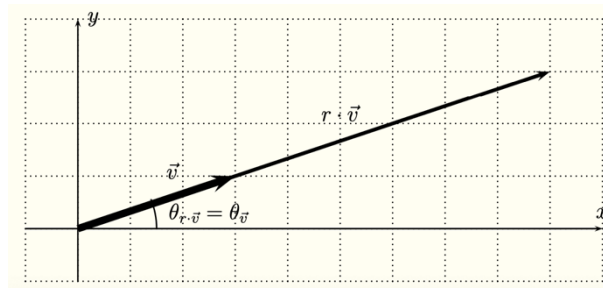
4. The vector  $\vec{v}$  can be presented by its length \_\_\_\_\_ and direction angle \_\_\_\_\_:

$$\vec{v} = \langle a, b \rangle = \langle \quad, \quad \rangle$$

5. Operations on vectors: Let  $\vec{v} = \langle a, b \rangle$  and  $\vec{w} = \langle c, d \rangle$

Scalar multiplication:  $r\vec{v} = r \cdot \langle a, b \rangle = \langle \quad, \quad \rangle$

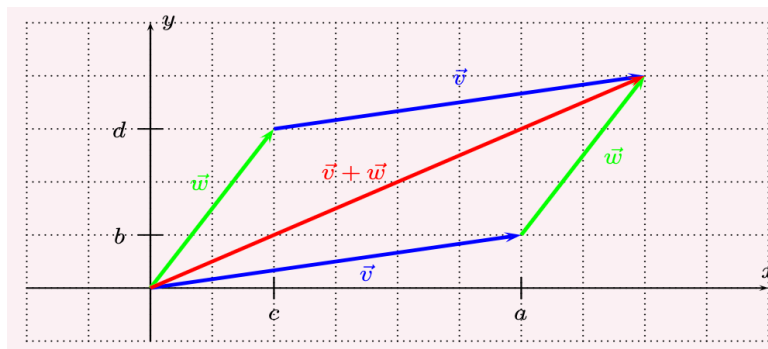
$r > 0$ :



$r < 0$ :

**Unit vector of  $\vec{v}$ :**  $r\vec{v}$  where  $r = \quad$  and we have  $r\vec{v} = \quad$ .

Vector addition:  $\vec{v} + \vec{w} = \langle a, b \rangle + \langle c, d \rangle = \langle \quad, \quad \rangle$



6. Let  $\vec{v} = \langle 3, 4 \rangle$  and  $\vec{w} = 4\mathbf{i} - 9\mathbf{j}$ . Find (a) the directional angle of  $\vec{v}$ , (b) the unit vector of  $\vec{v}$ , (c)  $\vec{v} + \vec{w}$ , and (d)  $2\vec{v} - 3\vec{w}$