

# MAT1375, Classwork19, Fall2025

## Ch18. Graphing Trigonometric Functions

1. Review: Even function and Odd function.

If  $f(x)$  is an even function, then  $f(-a) = \underline{f(a)}$ .

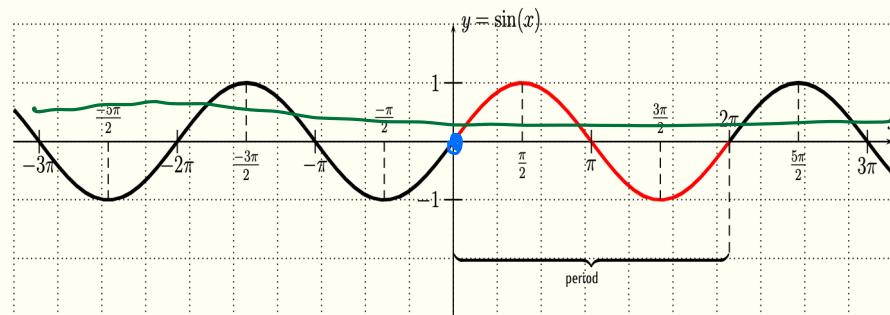
If  $f(x)$  is an odd function, then  $f(-a) = \underline{-f(a)}$

2. Definition of a Periodic Function:

A function  $f$  is \_\_\_\_\_ if there is a positive number  $p$  called a \_\_\_\_\_ such that

$$f(x + p) = f(x) \quad \text{for all } x.$$

3. The graph of  $y = \sin(x)$ :



**Characteristics:**

Period:  $2\pi$

Domain:  $(-\infty, \infty)$

Range:  $[-1, 1]$

One-to-one function? NO

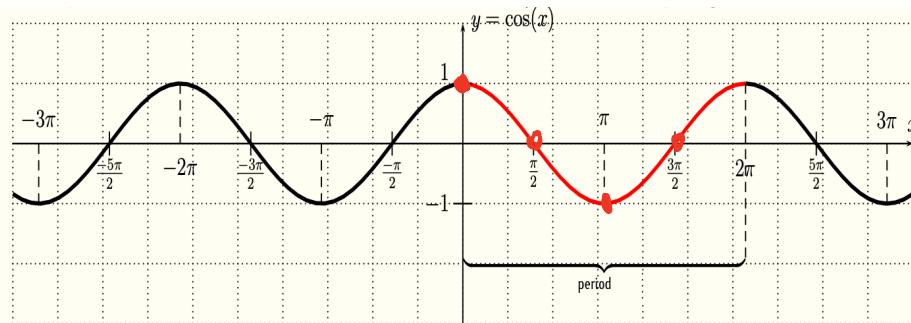
Inverse function? NO

**Property:** odd function with origin symmetry where  $\sin(-x) = \underline{-\sin(x)}$ .

$x$	✓ 0	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	✓ $\frac{\pi}{2}$	$\frac{2\pi}{3}$	$\frac{3\pi}{4}$	$\frac{5\pi}{6}$	✓ $\pi$	$\frac{7\pi}{6}$	$\frac{4\pi}{3}$	✓ $\frac{3\pi}{2}$	$\frac{5\pi}{3}$	$\frac{11\pi}{6}$	✓ $2\pi$	
$\sin(x)$	0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0	$-\frac{1}{2}$	$-\frac{\sqrt{2}}{2}$	$-\frac{\sqrt{3}}{2}$	-1	$-\frac{\sqrt{3}}{2}$	$-\frac{\sqrt{2}}{2}$	$-\frac{1}{2}$

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4. The graph of  $y = \cos(x)$ :



**Characteristics:**

Period:  $2\pi$

Domain:  $(-\infty, \infty)$

Range:  $[-1, 1]$

One-to-one function? NO

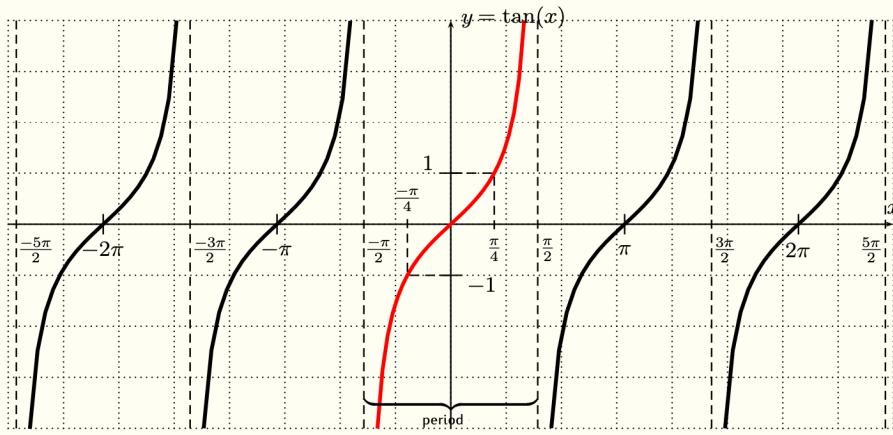
Inverse function? NO

**Property:** even function with  $y$ -axis symmetry where  $\cos(-x) = \underline{\cos(x)}$ .

$x$	0	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	$\frac{\pi}{2}$	$\frac{2\pi}{3}$	$\frac{3\pi}{4}$	$\frac{5\pi}{6}$	0	$\frac{7\pi}{6}$	$\frac{4\pi}{3}$	$\frac{3\pi}{2}$	$\frac{5\pi}{3}$	$\frac{11\pi}{6}$	$2\pi$	
$\cos(x)$	1	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0	$-\frac{1}{2}$	$-\frac{\sqrt{2}}{2}$	$-\frac{\sqrt{3}}{2}$	0	$-\frac{\sqrt{3}}{2}$	$-\frac{\sqrt{2}}{2}$	$-\frac{1}{2}$	0	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	1

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5. The graph of  $y = \tan(x)$ :  $\frac{\sin(x)}{\cos(x)} = 0$



Characteristics:

$$\text{Period: } \frac{\frac{3\pi}{2} - \frac{\pi}{2}}{2} = (\frac{3}{2} - \frac{1}{2})\pi = \pi$$

Domain: All real numbers except odd multiples of  $\frac{\pi}{2}$

Range:  $(-\infty, \infty)$

Vertical Asymptotes:  $x = -\frac{\pi}{2}, x = -\frac{3\pi}{2}, x = -\frac{5\pi}{2}, x = \frac{\pi}{2}, x = \frac{3\pi}{2}, x = \frac{5\pi}{2}, \dots$

One-to-one function? NO

Inverse function? NO

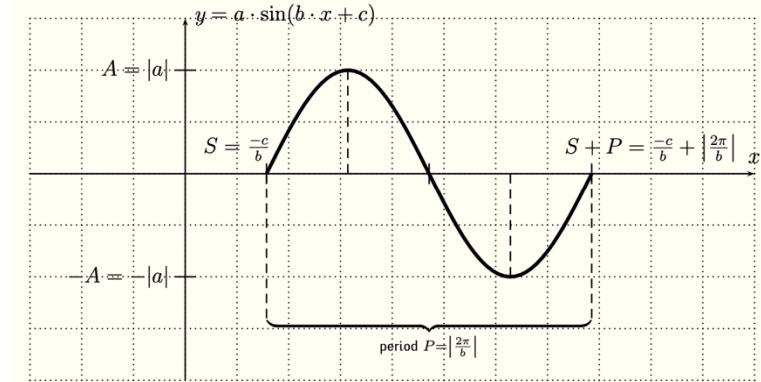
$$\frac{\sin(-x)}{\cos(-x)} = -\frac{\sin(x)}{\cos(x)} = -\tan(x)$$

Property: odd function with origin symmetry where  $\tan(-x) =$

$x$	$-\frac{\pi}{2}$	$-\frac{\pi}{3}$	$-\frac{\pi}{4}$	$-\frac{\pi}{6}$	0	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	$\frac{\pi}{2}$
$\tan(x)$									

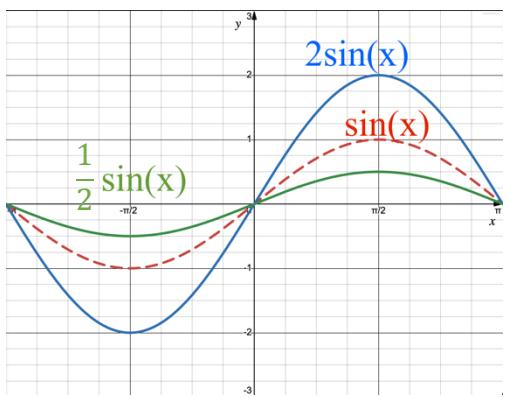
6. Amplitude, period, and phase shift:

Let  $f(x) = a \cdot \sin(b \cdot x + c) = a \cdot \sin(b \cdot (x + S))$  or  $f(x) = a \cdot \cos(b \cdot x + c) = a \cdot \cos(b \cdot (x + S))$ .



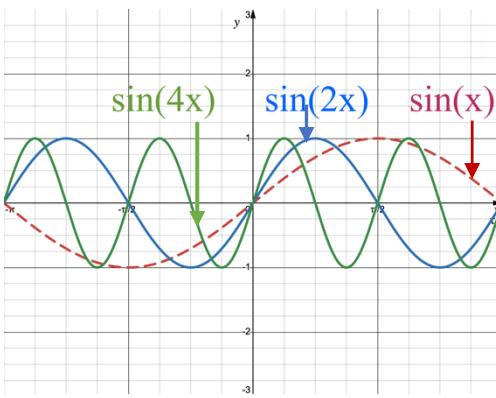
We define

- 1) the amplitude  $A = |a|$ ;
- 2) the period  $P = \left| \frac{2\pi}{b} \right|$ ;
- 3) the phase shift  $S = -\frac{c}{b}$ .



For  $f(x) = 2 \sin(x)$ , its A is \_\_\_\_\_

For  $f(x) = \frac{1}{2} \sin(x)$ , its A is \_\_\_\_\_



For  $f(x) = \sin(2x)$ , its P is \_\_\_\_\_.

For  $f(x) = \sin(4x)$ , its P is \_\_\_\_\_.