

18 Quiz 18 MAT 1275 Professor Chiu

Name: _____

- This quiz consists of **2** questions, each worth 5 points for a total of **10** points.
- You have **15** minutes to complete the quiz.
- Show all work and justify your answers.
- Scientific calculators are allowed.
- Wishing you success.

1. Find the center and radius of the circle $x^2 + 4x + y^2 - 4y = 1$.

$$\begin{aligned}(x-a)^2 &= x^2 - 2ax + a^2 \\ -2a &= 4 \Rightarrow a = -2 \\ C &= a^2 = (-2)^2 = 4\end{aligned}$$

$$\begin{aligned}(y-b)^2 &= y^2 - 2by + b^2 \\ -2b &= -4 \Rightarrow b = 2 \\ C &= b^2 = (2)^2 = 4\end{aligned}$$

$$(x-a)^2 + (y-b)^2 = r^2$$

center (a, b) r : radius

$$\begin{aligned}x^2 + 4x + 4 + y^2 - 4y + 4 &= 1 + 4 + 4 \\ (x - (-2))^2 + (y - 2)^2 &= 9\end{aligned}$$

Center $(-2, 2)$

$$\text{radius} = \sqrt{9} = 3$$

2. Find the vertex, label two additional points, and sketch the graph of $y + 2 = (x - 3)^2$.

Vertex $(X, y) = (3, -2)$

$y + 2 = (x - 3)^2$
 $y = -2$ $x = 3$

| X | y | |
|---------|---------|--|
| (0, 7) | (0, 7) | $y + 2 = (0 - 3)^2 \Rightarrow y + 2 = 9$ |
| (1, 2) | (1, 2) | $y + 2 = (1 - 3)^2 \Rightarrow y + 2 = 4$ |
| (2, -1) | (2, -1) | $y + 2 = (2 - 3)^2 \Rightarrow y + 2 = 1$ |
| (3, -2) | (3, -2) | $y + 2 = (3 - 3)^2 \Rightarrow y + 2 = 0 \Rightarrow y = -2$ |
| (4, -1) | (4, -1) | $y + 2 = (4 - 3)^2 \Rightarrow y + 2 = 1 \Rightarrow y = -1$ |
| (5, 2) | (5, 2) | $y + 2 = (5 - 3)^2 \Rightarrow y + 2 = 4 \Rightarrow y = 2$ |

