MAT1375, Classwork6, Fall2025

Ch6. The Inverse of a Function

1. (Review) Let f and g be the functions defined by the table below. Complete the table by performing the indicated operations.

x	1	2	3	4	5	6	7
f(x)	4	5	7	0	-2	6	4
g(x)	6	-8	5	2	9	11	2
g(x) + 3	6+3=9	-8 +3=-5	573=8	2+3=5	9+3=12	11+3=14	2+3-5
f(x) - 2g(x)	f(1)-2\$(1) =4-2·6=-8	f=5-2·(+6)=2	P	-4	-20	-(6	0
g(x+3)	g(1+3) = $g(\varphi)$ =2	g(2+ 3) = 9	g(3+3) =g(6)=11	9(4 +3) =9(9)= 2	9 (573) =3(8) undi	Tived underval	f(r+3) = f
$(f \circ g)(x) = f(g)$	+(6) = 6	f(2)) =f(-8) undefin	f(g(z)) =((5)=-2	f(g(4)) =f(2)=5	f(g(s)) := +(g) (udit)	f(gG) $=f(II)$ undate	+(g(1)) =f(2)=5
$(g \circ f)(x) = g(fo)$	2	9	2	undet:	undof.	il	2
$(g \circ g)(x) = g[$	(x)) 9(g()))	9	-8	undeln	undefind	-8

2. Complete the definition of the one-to-one function (or injective):

Given a function f(x). If any two different inputs X = X always have different outputs X = X then we call this function f a **one-to-one function**.

3. The tables below describe assignments between inputs x and outputs y. Determine which of the given tables describe a one-to one function.

Since	input	(G =	F 3	but	Huy	how	e su	٤
	у	1	3	5	7	1	9	
(a)	x	19	7	6	-2	(3)	-11	

same output which is 1,

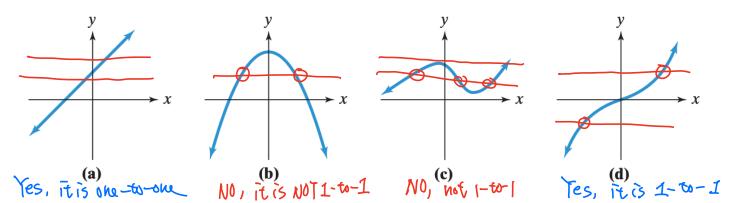
so, no, this is NOT me—to—one
function

(b)	x	19	7	6	-2	3	-1	
	у	1	2	3	4	5	6	
19 2					Yes, it is			

because different impost get different outputs

4. **Horizontal Line test**: A function is one-to-one when every horizontal line intersects the graph of the function most one-to-one when every horizontal line intersects the graph of the function

5. Use **Horizontal Line Test** to determine which of the following are the graphs of one-to-one functions.



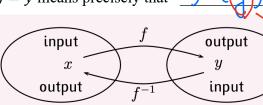
6. Complete the definition of the Inverse of a Function:

Let f be a function with domain D_f and the range R_f , and assume that f is one-to-one. The **inverse** of f is

the function f^{-1} , determined by:



f(x) = y means precisely that



old output -> new input

>old input

7. How to check if two given functions are **inverse** with each other:

Let f and g be two functions such that

$$\frac{f(g(x)) = \chi}{g(+\infty) = \chi}$$
 for every x in the domain of g and for every x in the domain of f.

The function g is the **inverse of the function f** and is denoted by g = g

8. How to find the inverse function for a given **invertible** function f(x):

Step1: Replace for by 4

- 9. Given a function $f(x) = x^2 + 1$, $x \ge 0$.
 - (a) Find the inverse function of f(x).
 - (b) Graph f and f^{-1} in the same coordinate system.

Step 1
$$y = x^{2}+1, x > 0(, y > 1)$$

Step 2 $x = y^{2}+1, y > 0$
Step 3 $y^{2}=x-1, y > 0$
 $y = t_{1}x-1, y > 0$
 $y = t_{1}x-1, y > 0$
 $y = \sqrt{x}-1, y > 0$

