

Quiz18, MAT 1375 Professor Chiu

ID: _____

Name: _____

- This quiz consists of 4 sets of questions for a total of 20 points.
- You have 15 minutes to complete the quiz.
- Wishing you success.

1. Find the trigonometric function values by using the addition and subtraction formulas.

$$\begin{aligned} \text{a) } \sin(75^\circ) &= \sin(30^\circ + 45^\circ) = \sin(30^\circ) \cos(45^\circ) + \cos(30^\circ) \sin(45^\circ) \\ &= \frac{1}{2} \cdot \frac{\sqrt{2}}{2} + \frac{\sqrt{3}}{2} \cdot \frac{\sqrt{2}}{2} \\ &= \frac{\sqrt{2}}{4} + \frac{\sqrt{6}}{4} = \frac{\sqrt{2} + \sqrt{6}}{4} \end{aligned}$$

$$\begin{aligned} \text{b) } \cos(15^\circ) &= \cos(60^\circ - 45^\circ) = \cos(60^\circ) \cos(45^\circ) + \sin(60^\circ) \sin(45^\circ) \\ &= \frac{1}{2} \cdot \frac{\sqrt{2}}{2} + \frac{\sqrt{3}}{2} \cdot \frac{\sqrt{2}}{2} \\ &= \frac{\sqrt{2}}{4} + \frac{\sqrt{6}}{4} = \frac{\sqrt{2} + \sqrt{6}}{4} \end{aligned}$$

2. Find the amplitude, period, and phase shift of the function: $y = 3 \cos(2x + \pi)$.

$$\begin{aligned} &\text{Amplitude: } 3 \\ &\text{Period: } \frac{2\pi}{2} = \pi \\ &\text{Phase shift: } -\frac{\pi}{2} \end{aligned}$$

$$= 3 \cos\left(2 \cdot \left(x + \frac{\pi}{2}\right)\right)$$

3. Find the value of the given inverse sine functions: $\sin^{-1}\left(-\frac{\sqrt{3}}{2}\right)$.

$$\begin{aligned} \text{Let } \theta &= \sin^{-1}\left(-\frac{\sqrt{3}}{2}\right) \iff \sin(\theta) = -\frac{\sqrt{3}}{2} \\ &\left(-\frac{\pi}{2} \leq \theta \leq \frac{\pi}{2}\right) \end{aligned}$$

$$\theta = -\frac{\pi}{3} \text{ or } -60^\circ$$

4. Complete the chart of the unit circle: quadrants, radian, and the coordinates representing $(\cos(\theta), \sin(\theta))$.

