

MAT1375, Classwork19, Fall2025

Ch18. Graphing Trigonometric Functions

1. Review: Even function and Odd function.

If $f(x)$ is an even function, then $f(-a) = \underline{f(a)}$.

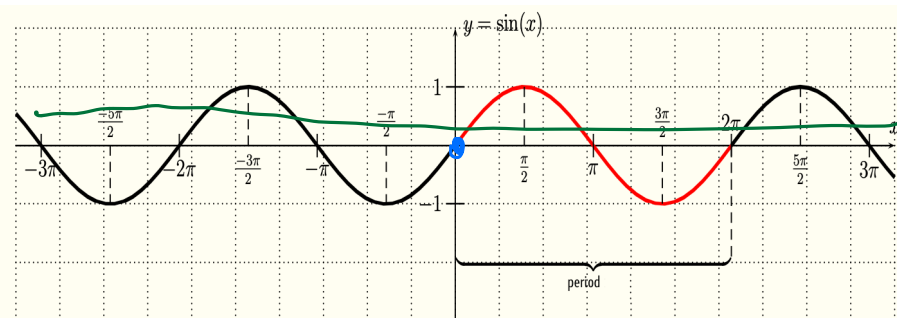
If $f(x)$ is an odd function, then $f(-a) = \underline{-f(a)}$.

2. Definition of a Periodic Function:

A function f is _____ if there is a positive number p called a _____ such that

$$f(x + p) = f(x) \quad \text{for all } x.$$

3. The graph of $y = \sin(x)$:



Characteristics:

Period: $\underline{2\pi}$

Domain: $\underline{(-\infty, \infty)}$

Range: $\underline{[-1, 1]}$

One-to-one function? $\underline{\text{NO}}$

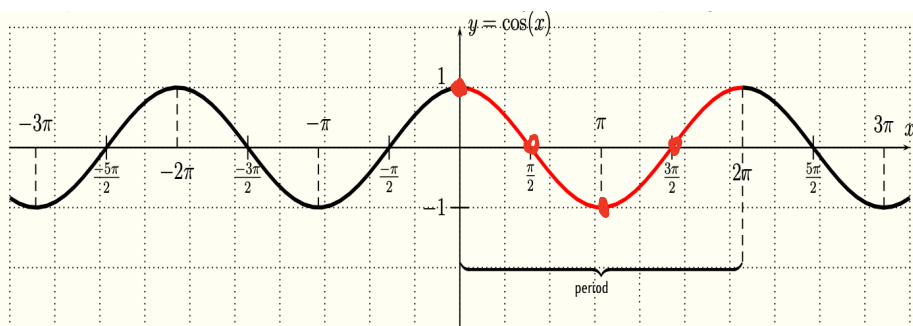
Inverse function? $\underline{\text{NO}}$

Property: odd function with origin symmetry where $\sin(-x) = \underline{-\sin(x)}$.

x	✓ 0	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	✓ $\frac{\pi}{2}$	$\frac{2\pi}{3}$	$\frac{3\pi}{4}$	$\frac{5\pi}{6}$	✓ π	$\frac{7\pi}{6}$	$\frac{5\pi}{4}$	$\frac{4\pi}{3}$	✓ $\frac{3\pi}{2}$	$\frac{5\pi}{3}$	$\frac{11\pi}{6}$	✓ 2π
$\sin(x)$	0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0	$-\frac{1}{2}$	$-\frac{\sqrt{2}}{2}$	$-\frac{\sqrt{3}}{2}$	-1	$-\frac{\sqrt{3}}{2}$	$-\frac{\sqrt{2}}{2}$	$-\frac{1}{2}$

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4. The graph of $y = \cos(x)$:



Characteristics:

Period: $\underline{2\pi}$

Domain: $\underline{(-\infty, \infty)}$

Range: $\underline{[-1, 1]}$

One-to-one function? $\underline{\text{NO}}$

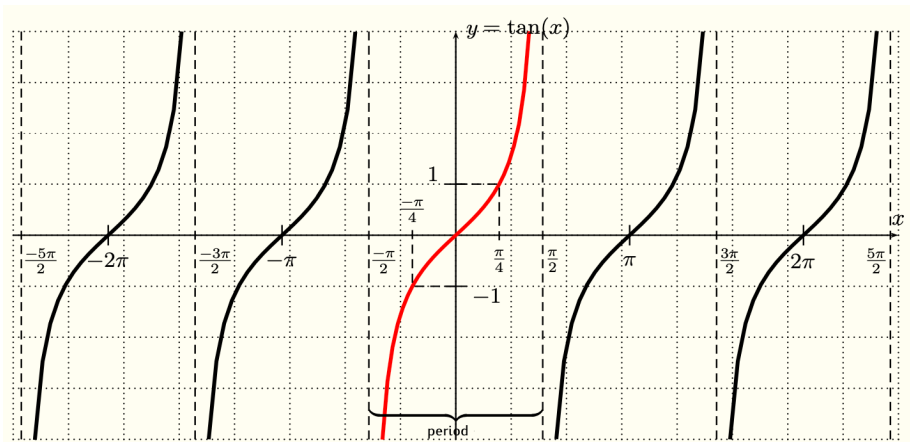
Inverse function? $\underline{\text{NO}}$

Property: even function with $x=0$ y-axis symmetry where $\cos(-x) = \underline{\cos(x)}$.

x	0	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	$\frac{\pi}{2}$	$\frac{2\pi}{3}$	$\frac{3\pi}{4}$	$\frac{5\pi}{6}$	π	$\frac{7\pi}{6}$	$\frac{5\pi}{4}$	$\frac{4\pi}{3}$	$\frac{3\pi}{2}$	$\frac{5\pi}{3}$	$\frac{11\pi}{6}$	2π
$\cos(x)$	1	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0	$-\frac{1}{2}$	$-\frac{\sqrt{2}}{2}$	$-\frac{\sqrt{3}}{2}$	-1	$-\frac{\sqrt{3}}{2}$	$-\frac{\sqrt{2}}{2}$	$-\frac{1}{2}$	0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$

I II III IV

5. The graph of $y = \tan(x)$: $= \frac{\sin(x)}{\cos(x)} = 0$



Characteristics:

Period: $\frac{3\pi}{2} - \frac{\pi}{2} = (\frac{3}{2} - \frac{1}{2})\pi = \pi$

Domain: All real numbers except odd multiples of $\frac{\pi}{2}$

Range: $(-\infty, \infty)$

Vertical Asymptotes: $x = -\frac{\pi}{2}, x = -\frac{3\pi}{2}, x = -\frac{5\pi}{2}$
 $x = \frac{\pi}{2}, x = \frac{3\pi}{2}, x = \frac{5\pi}{2}, x = \frac{7\pi}{2} \dots$

One-to-one function? NO

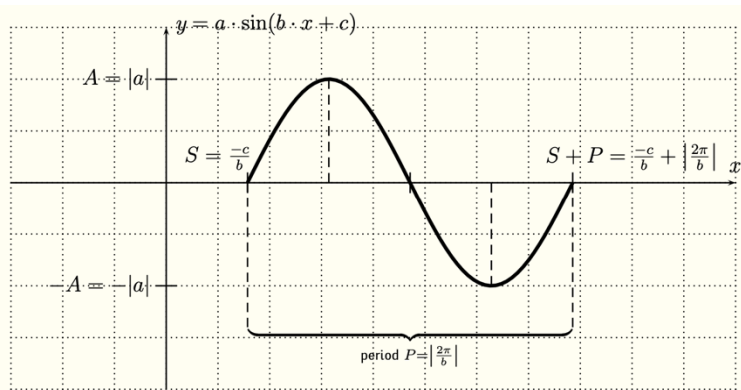
Inverse function? NO

Property: odd function with origin symmetry where $\tan(-x) = \frac{\sin(-x)}{\cos(-x)} = \frac{-\sin(x)}{\cos(x)} = -\tan(x)$

x	$-\frac{\pi}{2}$	$-\frac{\pi}{3}$	$-\frac{\pi}{4}$	$-\frac{\pi}{6}$	0	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	$\frac{\pi}{2}$
$\tan(x)$									

6. Amplitude, period, and phase shift:

Let $f(x) = a \cdot \sin(b \cdot x + c) = a \cdot \sin\left(b \cdot \left(x + \frac{c}{b}\right)\right)$ or $f(x) = a \cdot \cos(b \cdot x + c) = a \cdot \cos\left(b \cdot \left(x + \frac{c}{b}\right)\right)$.

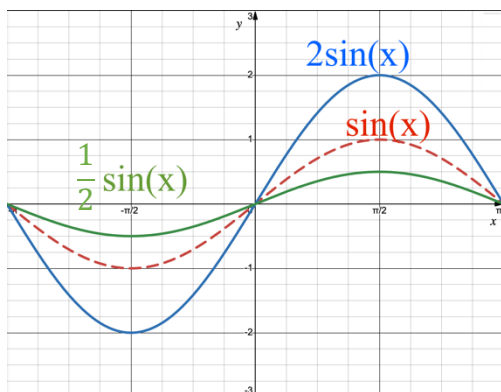


We define

1) the amplitude $A = |a|$;

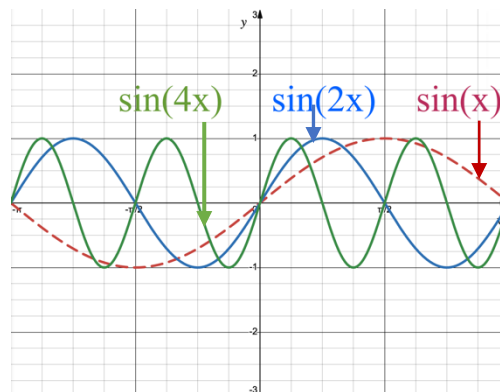
2) the period $P = \left|\frac{2\pi}{b}\right|$;

3) the phase shift $S = -\frac{c}{b}$.



For $f(x) = 2 \sin(x)$, its A is _____

For $f(x) = \frac{1}{2} \sin(x)$, its A is _____



For $f(x) = \sin(2x)$, its P is _____

For $f(x) = \sin(4x)$, its P is _____