

MAT2440, Classwork20, Spring2025

ID: _____ Name: _____

1. Use the membership table to prove one of the De Morgan's law: $\overline{A \cap B} = \bar{A} \cup \bar{B}$.

	A	B	$A \cap B$	$A \cup B$	\bar{A}	\bar{B}	$\bar{A} \cup \bar{B}$	$\overline{A \cap B}$
$a \in A \quad a \in B$	1	1	1	1	0	0	0	0
$a \in A \quad a \notin B$	1	0	0	1	0	1	1	1
$a \notin A \quad a \in B$	0	1	0	1	1	0	1	1
$a \notin A \quad a \notin B$	0	0	0	0	1	1	1	1

2. The Computer Representation of Sets:

Let S be a set and U be the universal set. If the universal set U is finite, then S can be represented bit strings.

3. Let the universal set $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$, and the ordering of element of U has the elements in increasing order.

(a) What bit strings can represent the subset of all odd integers in U ?

$\{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$
 $\{1, 3, 5, 7, 9\}$ odd integers in U
 string 1 0 1 0 1 0 1 0 1 0

(b) What bit strings can represent the set $B = \{1, 2, 5, 6\}$ in U ?

$U = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$
 $B = \{1, 2, 5, 6\}$
 1 1 0 0 1 1 0 0 0 0 ← string of B.

(c) What set in U can be represented by the bit string 00 1111 0010?

$1, 2, 3, 4, 5, 6, 7, 8, 9, 10$
 0 0 1 1 1 1 0 0 1 0
 $\Rightarrow \{3, 4, 5, 6, 9\}$

(d) Let $A_1 = \{1, 2, 3, 4, 5\}$ and $A_2 = \{1, 3, 5, 7, 9\}$ in U . Use bit string to find $A_1 \cup A_2$ and $A_1 \cap A_2$.

4. The Generalized Unions and Intersections with the **finite** family of sets:

The union of the sets A_1, A_2, \dots, A_n : _____ = _____.

The intersection of the sets A_1, A_2, \dots, A_n : _____ = _____.

5. The Generalized Unions and Intersections with the **infinite** family of sets:

The union of the sets $A_1, A_2, \dots, A_n, \dots$: _____ = _____.

The intersection of the sets $A_1, A_2, \dots, A_n, \dots$: _____ = _____.

6. Let $A = \{0, 2, 4, 6, 8\}$, $B = \{0, 1, 2, 3, 4\}$, and $C = \{0, 3, 6, 9\}$. Then find (a) $A \cup B \cup C$ and (b) $A \cap B \cap C$.

7. Suppose that $A_i = \{1, 2, 3, \dots, i\}$ for $i = 1, 2, 3, \dots$. Then find (a) $\bigcup_{i=1}^{\infty} A_i$ and (b) $\bigcap_{i=1}^{\infty} A_i$