Test 3 Review MAT 1275 Professor Chiu

Name: _____

- \bullet This review consists of 10 questions for a total of 100 points.
- You have 100 minutes to complete the review.
- Show all work and justify your answers.
- Scientific calculators are allowed.
- Wishing you success.

Problem 1 Evaluate the expression.

$$-2^{-3} + 7^0 - 27^{\frac{2}{3}}.$$

Problem 2 Solve

$$x^2 = 6x - 10$$

Problem 3 Simplify the fraction:

$$\frac{\frac{2}{x} + \frac{1}{y}}{\frac{3}{y} - \frac{4}{x}}$$

Problem 4 Divide and simplify:

$$\frac{3+4i}{7+2i}$$

Problem 5 Solve

$$4\sqrt{2x+1} - 3 = 17$$

Problem 6 Solve for x:

$$\frac{5}{x-3} + \frac{x}{x+4} = \frac{28}{x^2+x-12}$$

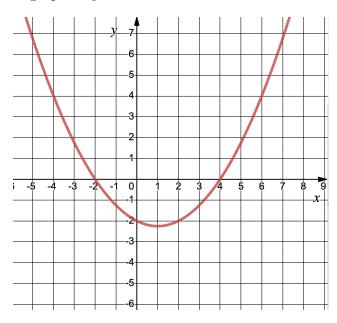
Problem 7 Find the equation of a line that passes through the points (1,1) and (-4,6).

Problem 8 Given an equation of circle $x^2 + 2x + y^2 - 4y = 1$ and answer the following questions:

- (a) Write this equation in standard form.
- (b) Find the center and radius of this circle.
- (c) Sketch the circle.

Problem 9 Find an equation representing the relationship between Celsius and Fahrenheit temperature scales noting the freezing point of water is $0^{\circ}C$ and $32^{\circ}F$ and boiling point of water is $100^{\circ}C$ and $212^{\circ}F$. If it is $74^{\circ}F$ outside, what is the temperature in Celsius (use your equation)?

Problem 10 Given the graph of $y = ax^2 + bx + c$ and answer the following questions:



- (a) Find all solutions to $0 = ax^2 + bx + c$.
- (b) What is the value of the constant coefficient c? Justify your answer.
- (c) Is the coefficient a, positive, negative or zero? Justify your answer.
- (d) How many solutions does the system $\begin{cases} y = ax^2 + bx + c, \\ y = 3. \end{cases}$ have? Justify your answer.
- (e) Find the equation for the line of symmetry of the given parabola.