

# Diseño de un sistema hardware in the loop para un Robot manipulador serial RR

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# MATERIALES

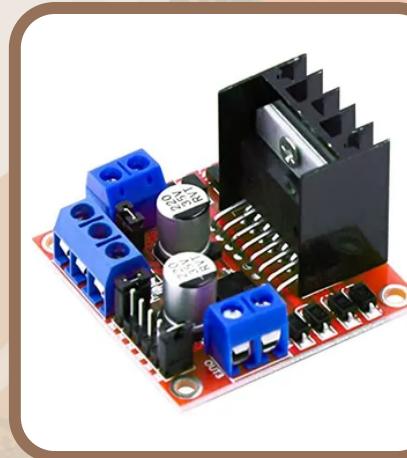
ESP32



Motores encoder



INTEGRADO L299N



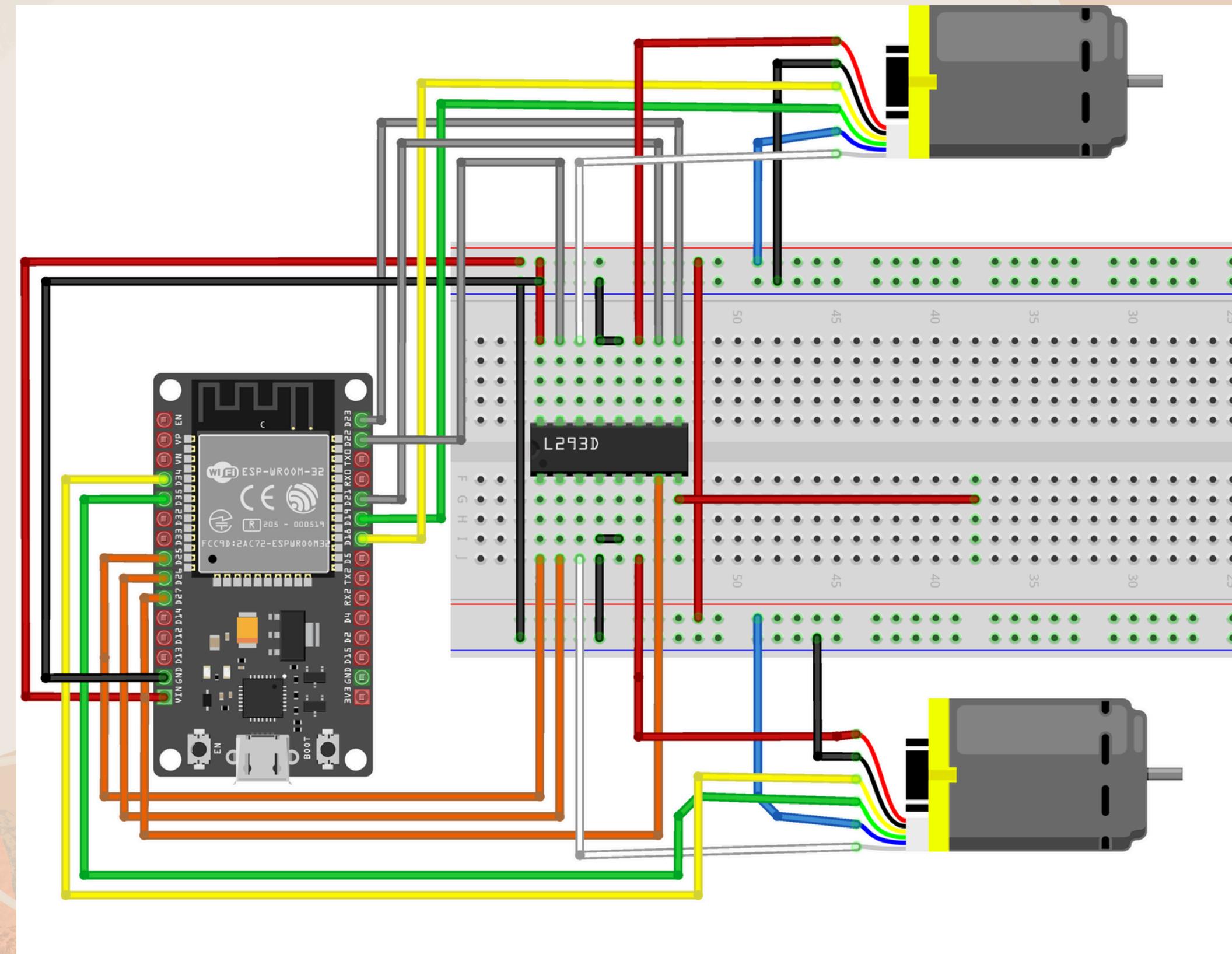
Fuente de Poder



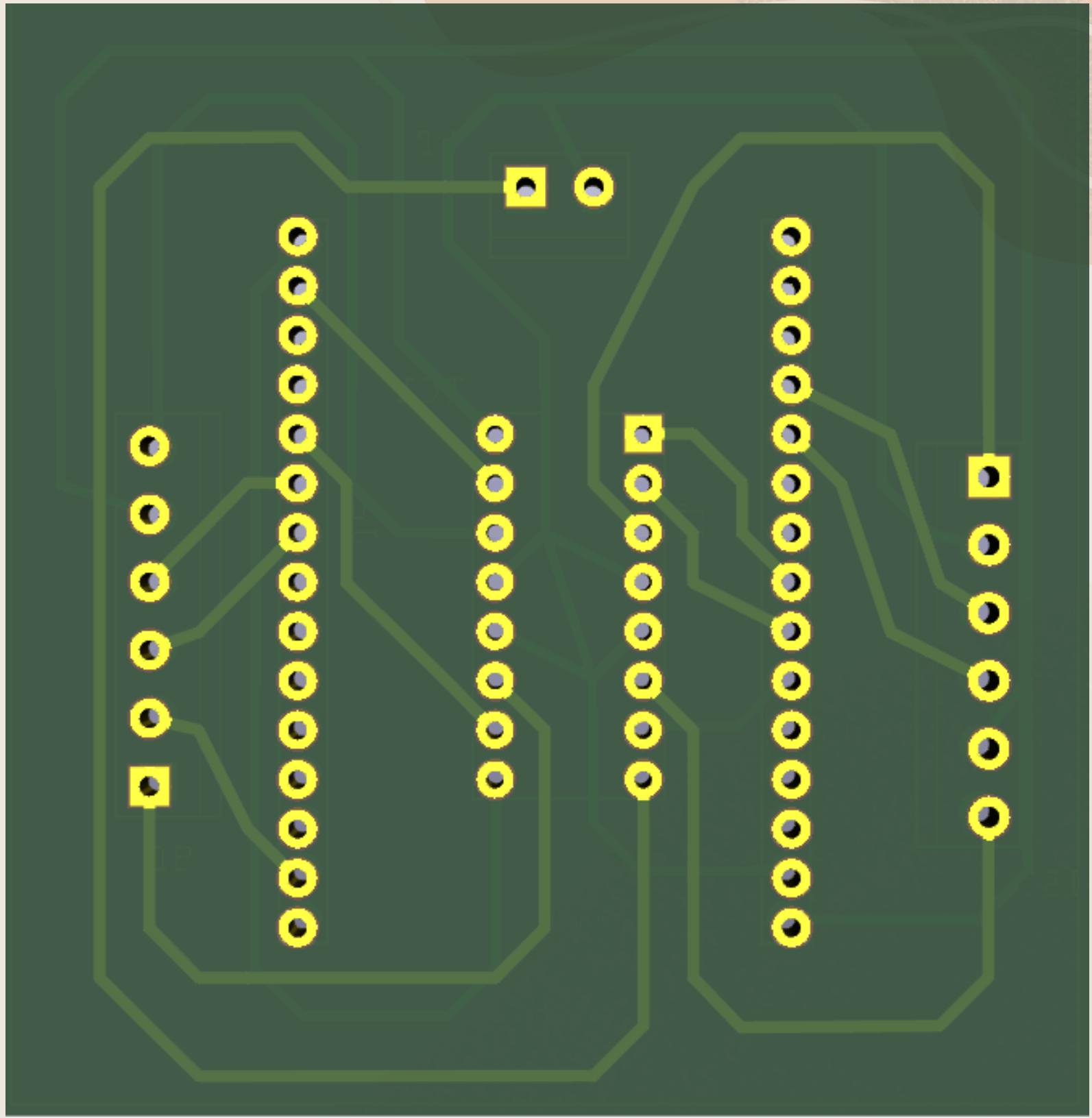
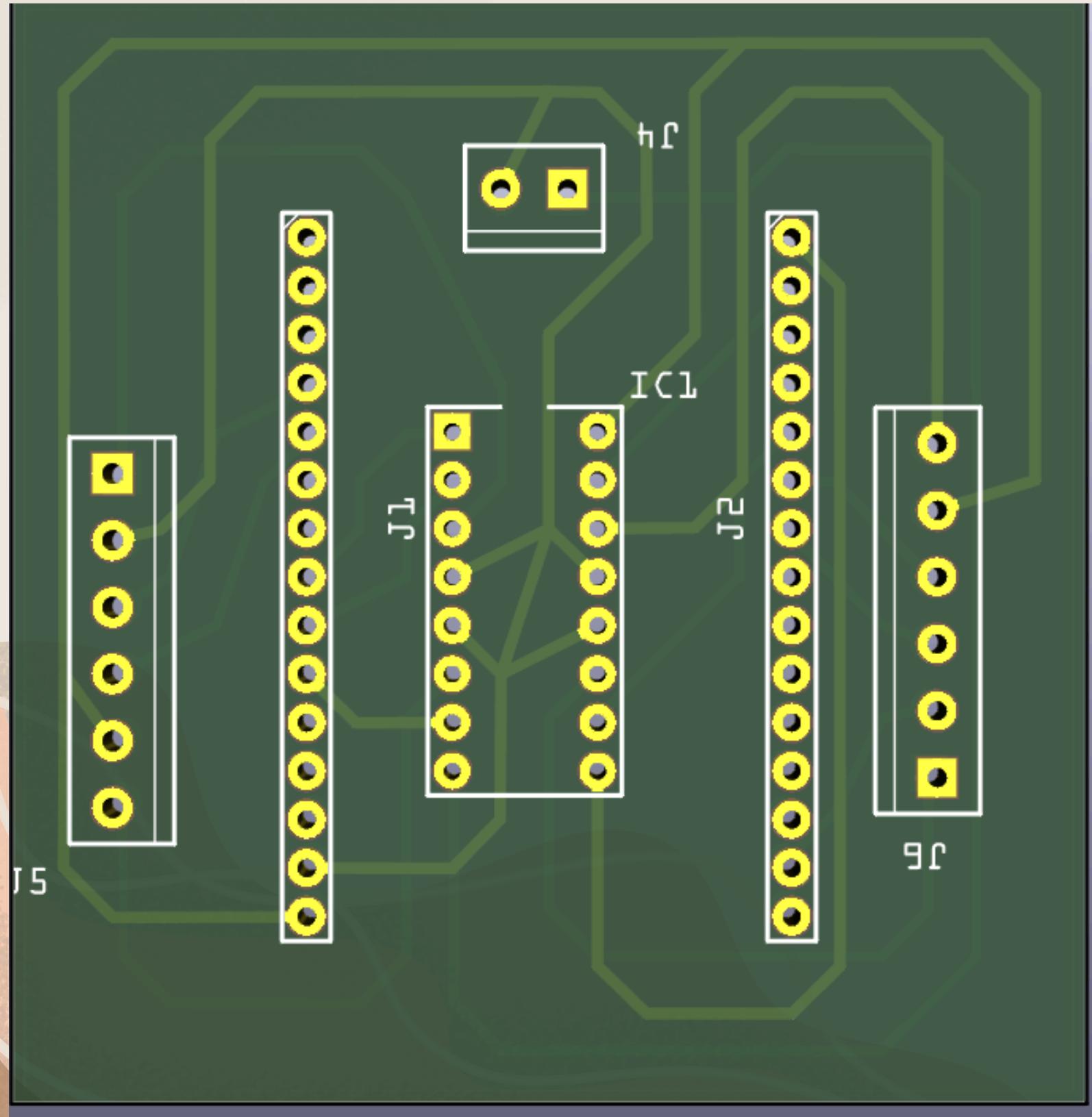
Cables de conexión



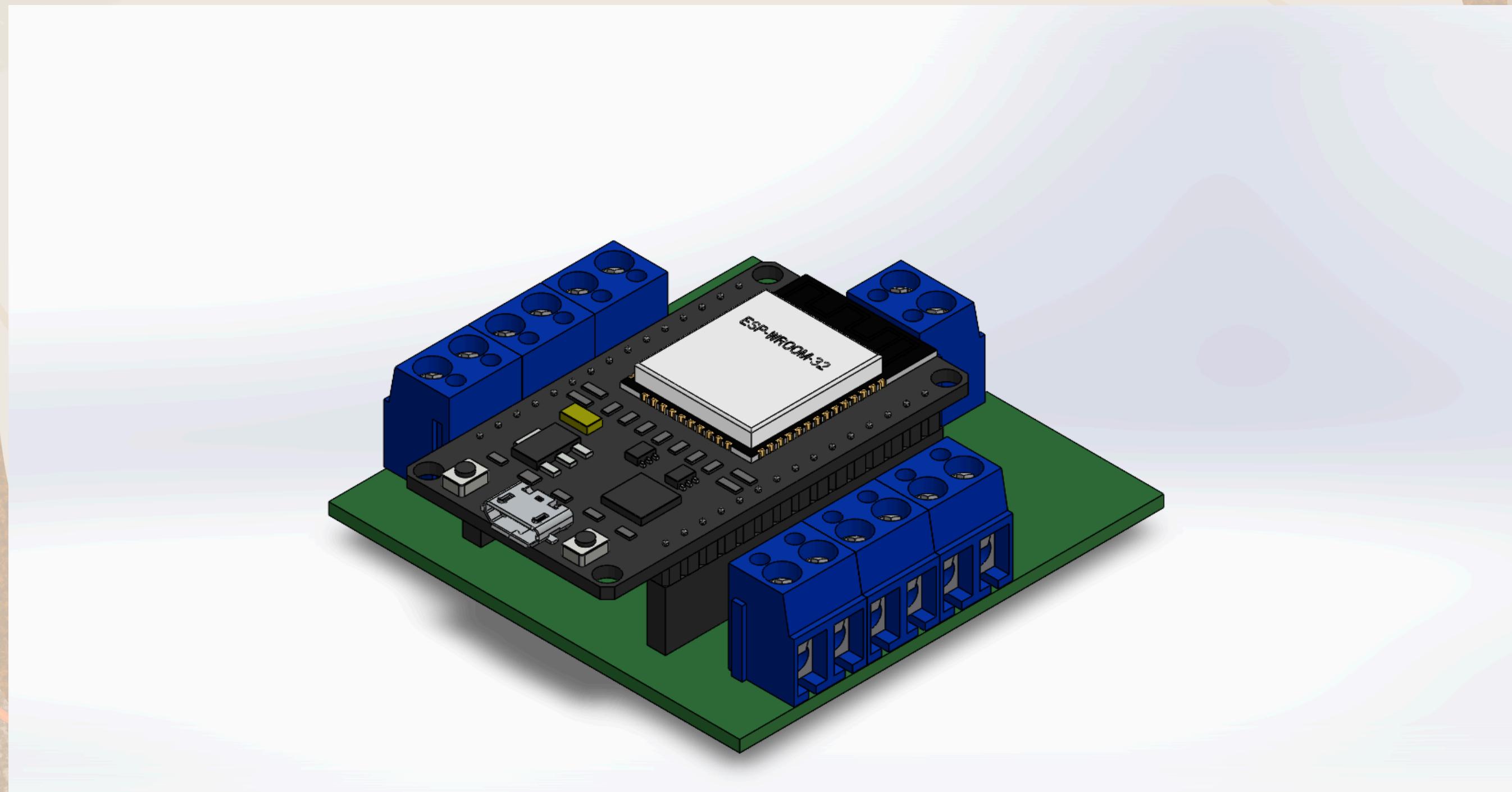
# CIRCUITO CONTROLADOR DE MOTORES



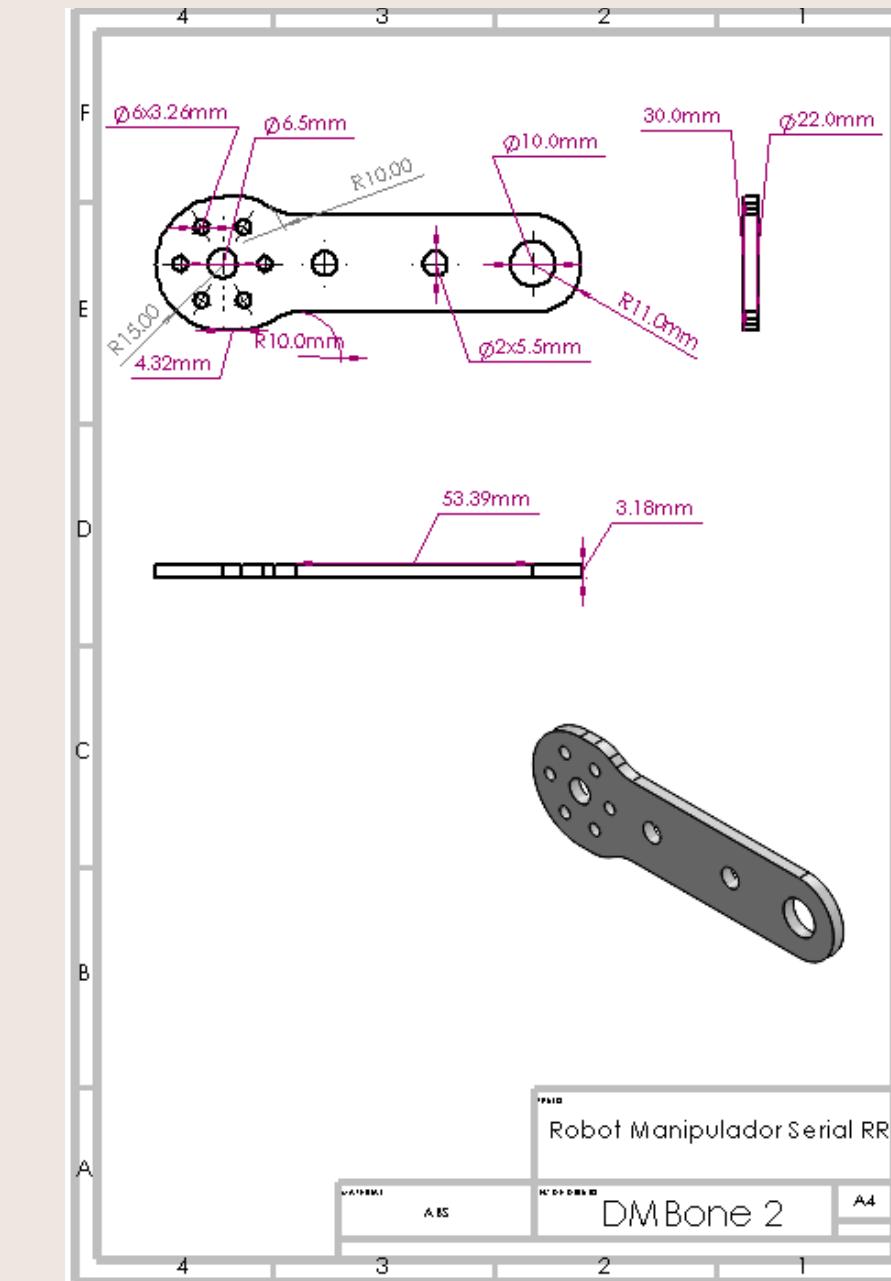
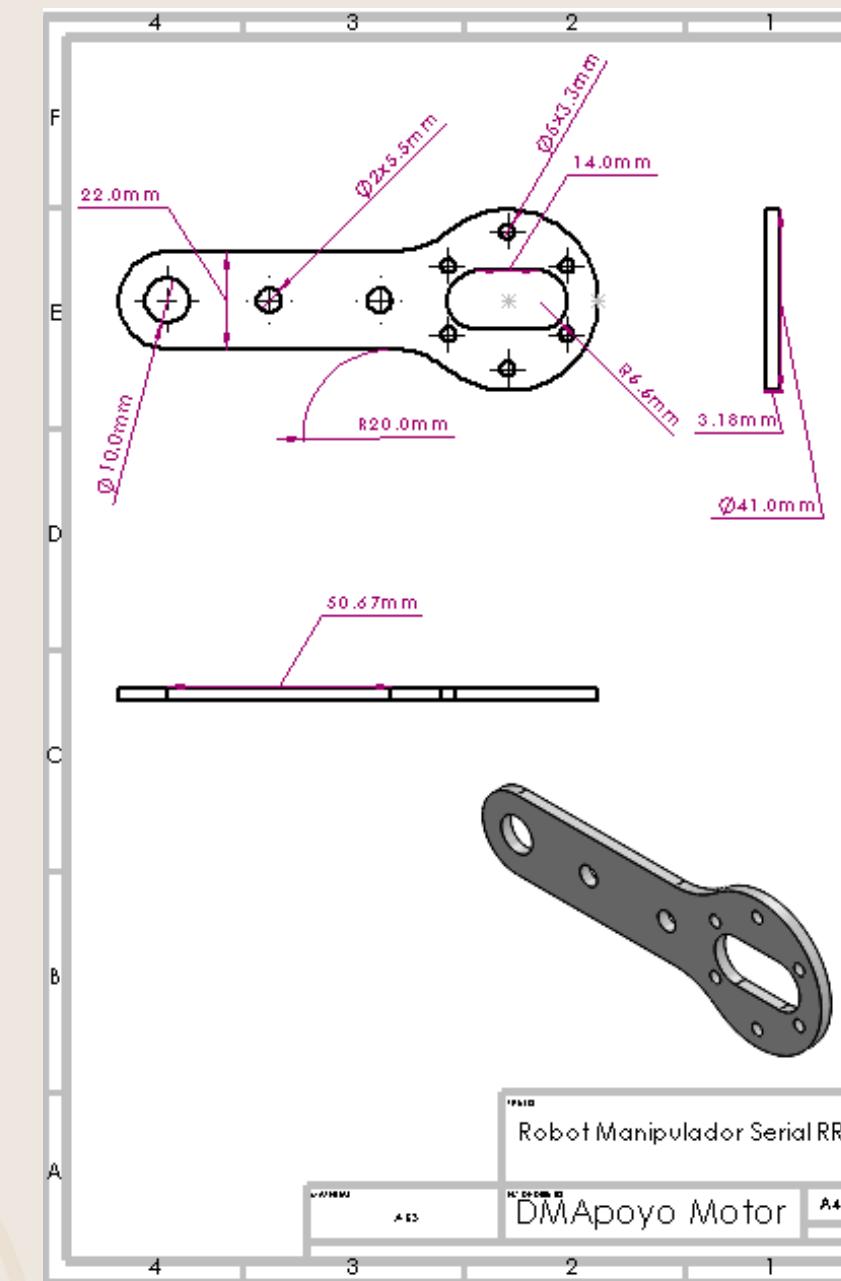
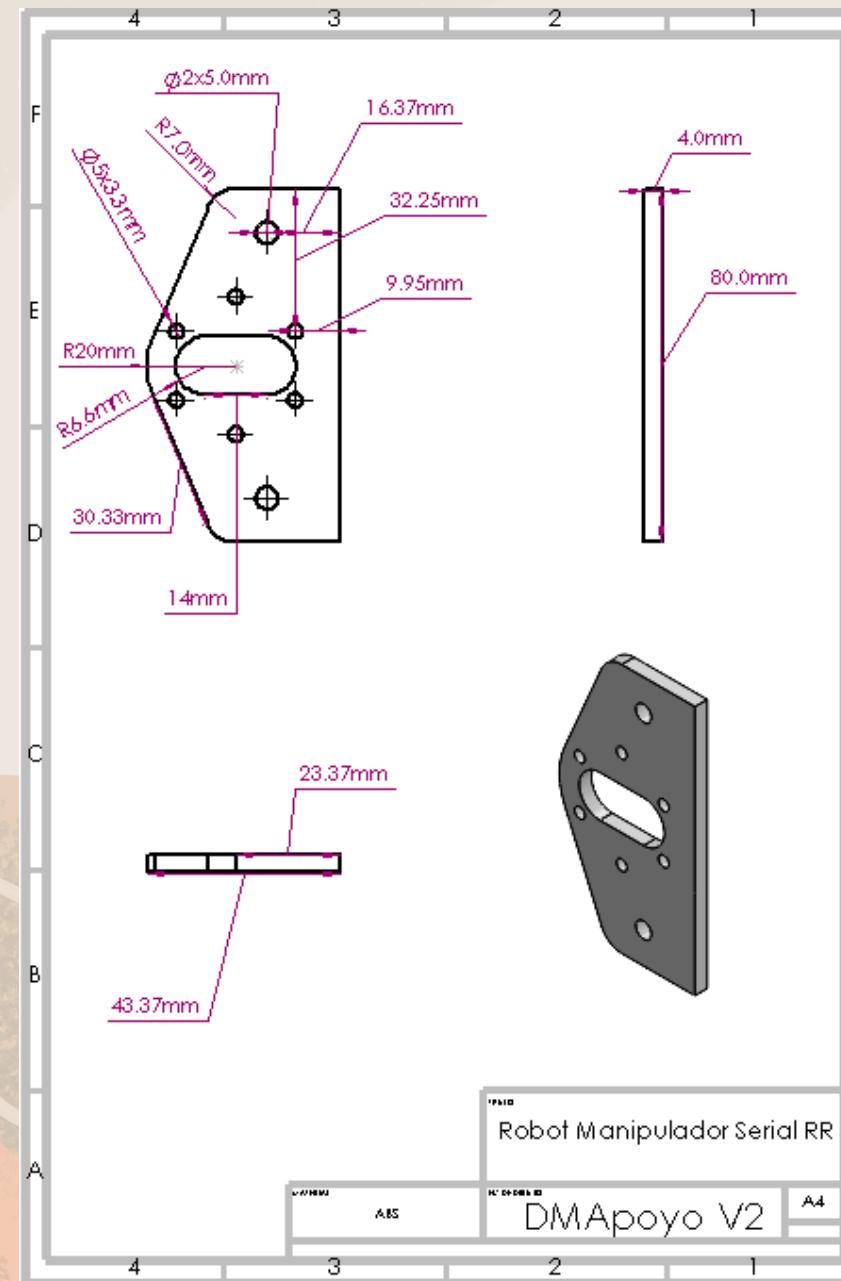
# PCB



# Representación grafica del PCB



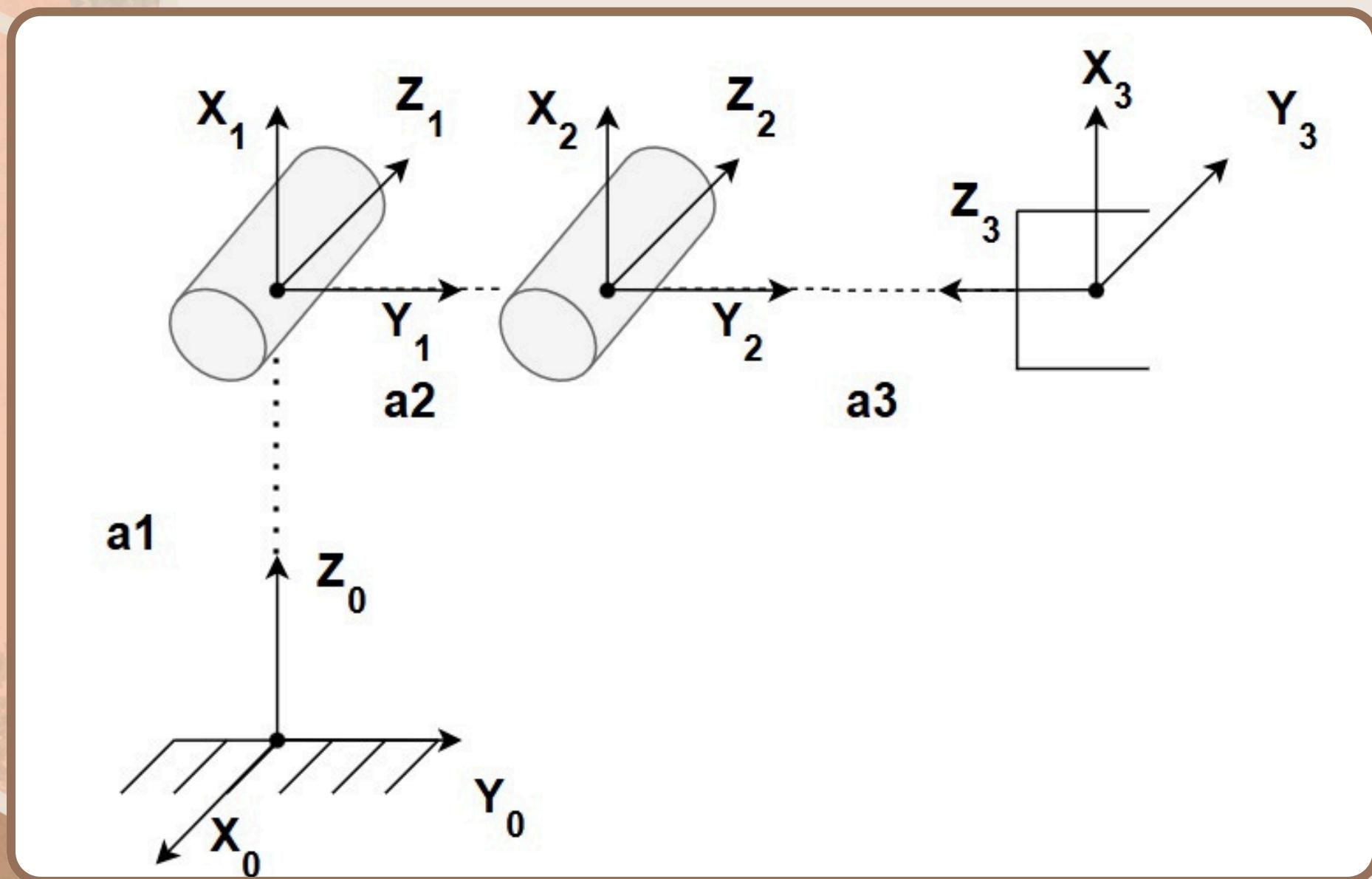
# MODELO MECANICO



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# CINEMÁTICA DIRECTA



Operación del marco 1 al marco 0:

$$A_0^1 = T_z(a_1) = \begin{bmatrix} 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & a_1 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Operación del marco 2 al marco 1:

$$A_1^2 = R_z(q_1) \cdot T_y(a_2) = \begin{bmatrix} \cos(q_1) & -\sin(q_1) & 0 & 0 \\ \sin(q_1) & \cos(q_1) & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & a_2 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \cos(q_1) & -\sin(q_1) & 0 & -a_2 \sin(q_1) \\ \sin(q_1) & \cos(q_1) & 0 & a_2 \cos(q_1) \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

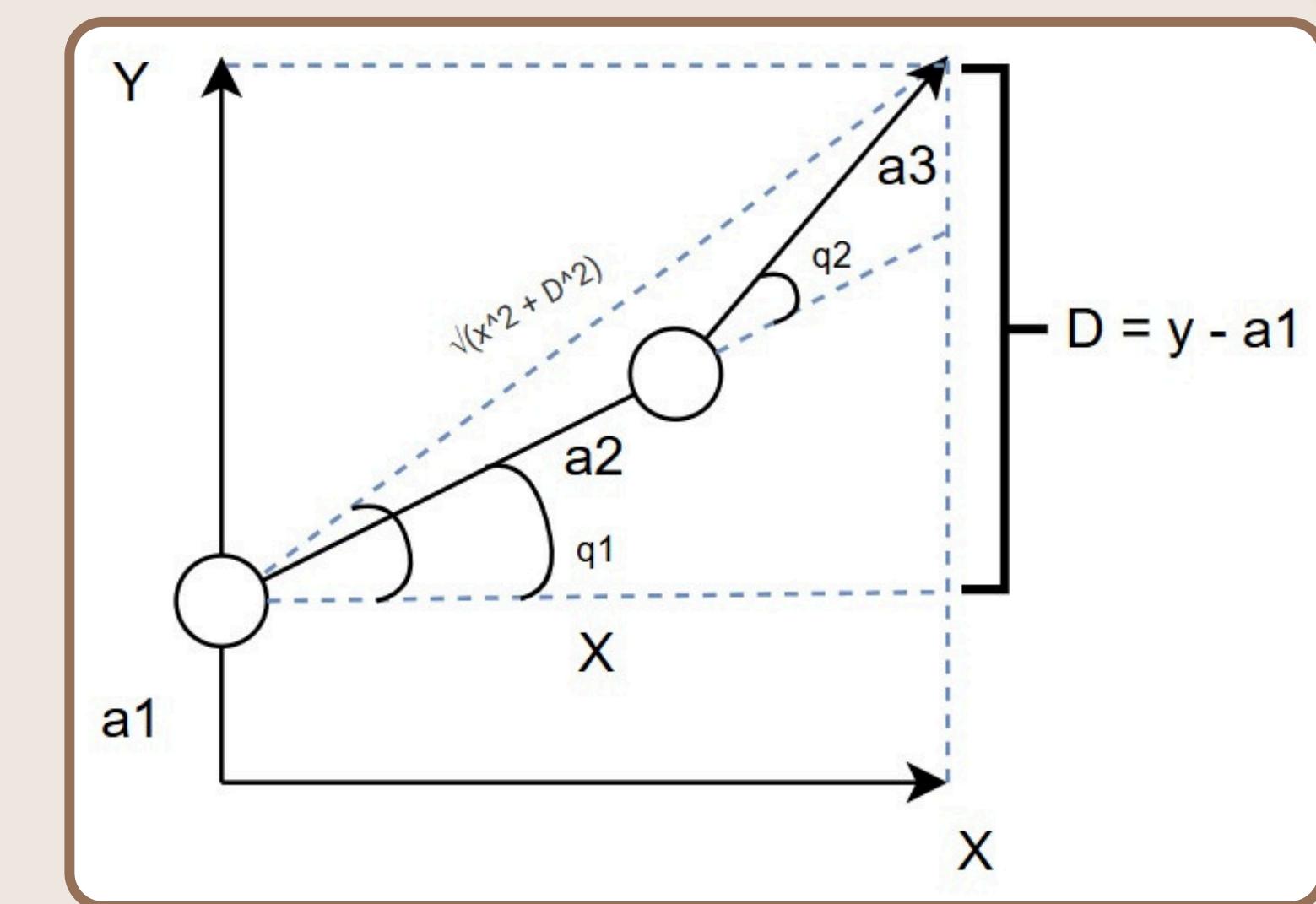
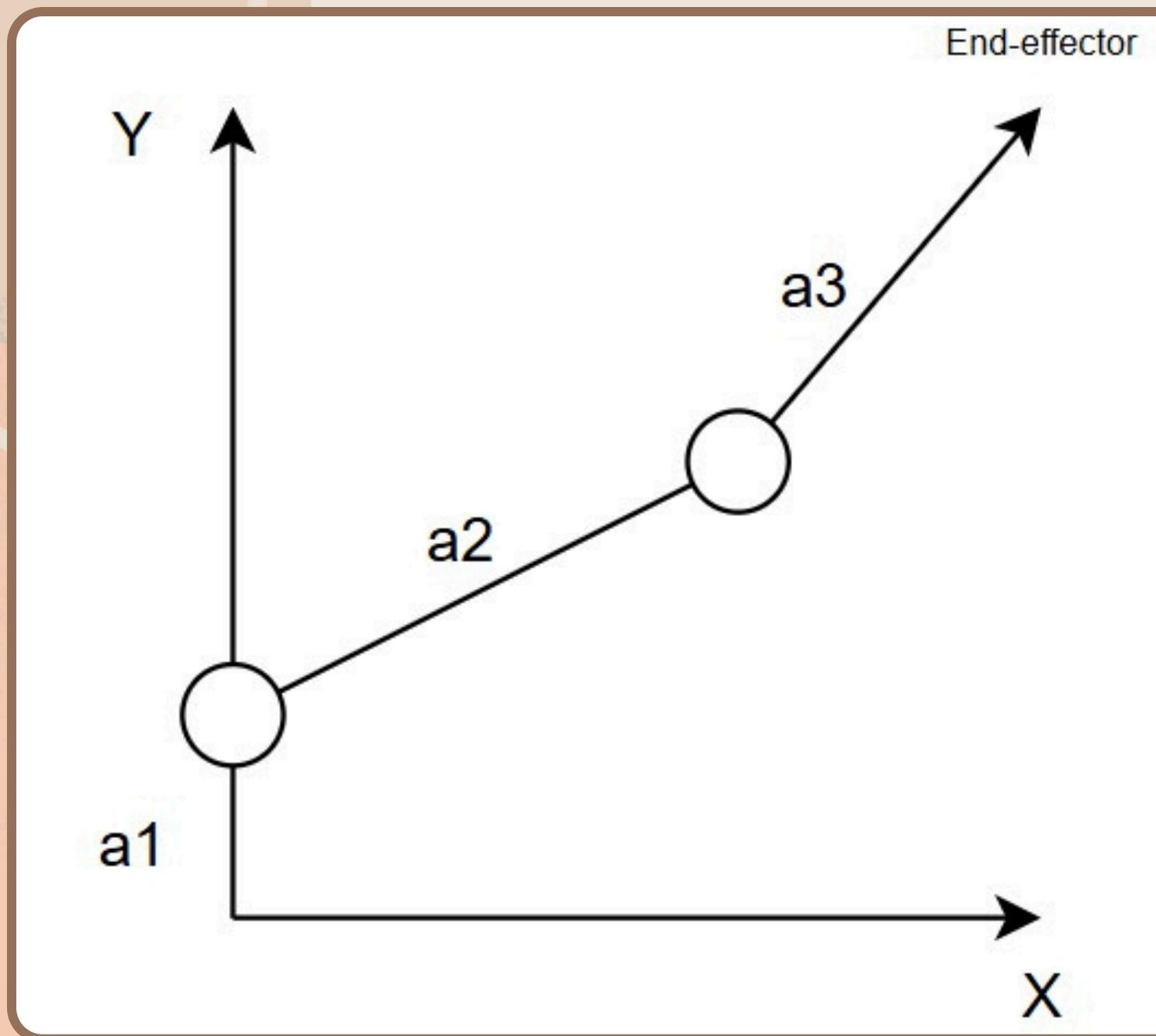
Operación del marco 3 al marco 1:

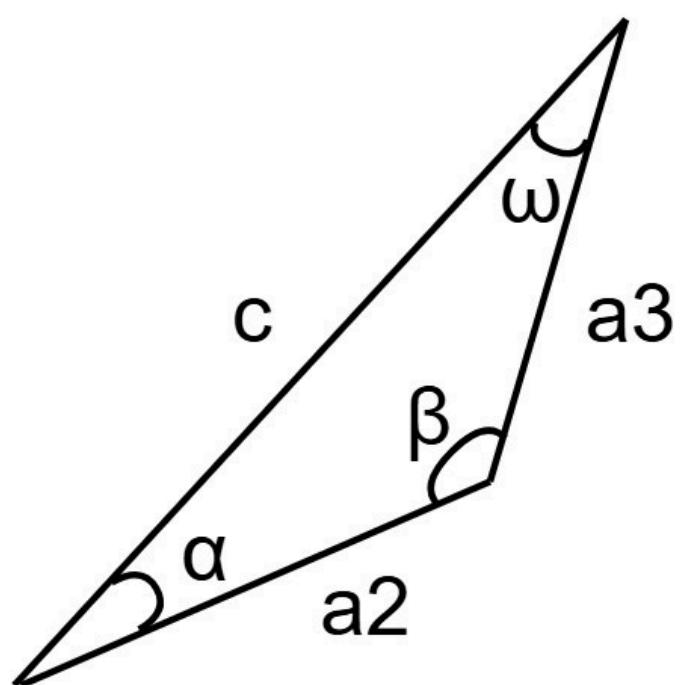
$$A_2^3 = R_z(q_2) \cdot T_y(a_3) = \begin{bmatrix} \cos(q_2) & -\sin(q_2) & 0 & 0 \\ \sin(q_2) & \cos(q_2) & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & a_3 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \cos(q_2) & -\sin(q_2) & 0 & -a_3 \sin(q_2) \\ \sin(q_2) & \cos(q_2) & 0 & a_3 \cos(q_2) \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

## Resultado:

$$T_f = A_0^1 A_1^2 A_2^3 = \begin{bmatrix} 0 & -1 & 0 & 0 \\ \sin(q_1 + q_2) & 0 & -\cos(q_1 + q_2) & a_3 \cos(q_1 + q_2) + a_2 \cos(q_1) \\ \cos(q_1 + q_2) & 0 & \sin(q_1 + q_2) & a_1 - a_3 \sin(q_1 + q_2) - a_2 \sin(q_1) \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

# CINEMÁTICA INVERSA





Por medio del triángulo obtusángulo se puede obtener  $q2$  por medio de la ley de cosenos.

$$c^2 = a_2^2 + a_3^2 - 2 * a_2 * a_3 * \cos(180 - q2)$$

$$- \cos(180 - q2) = \frac{x^2 + D^2 - a_2^2 - a_3^2}{2a_2a_3}$$

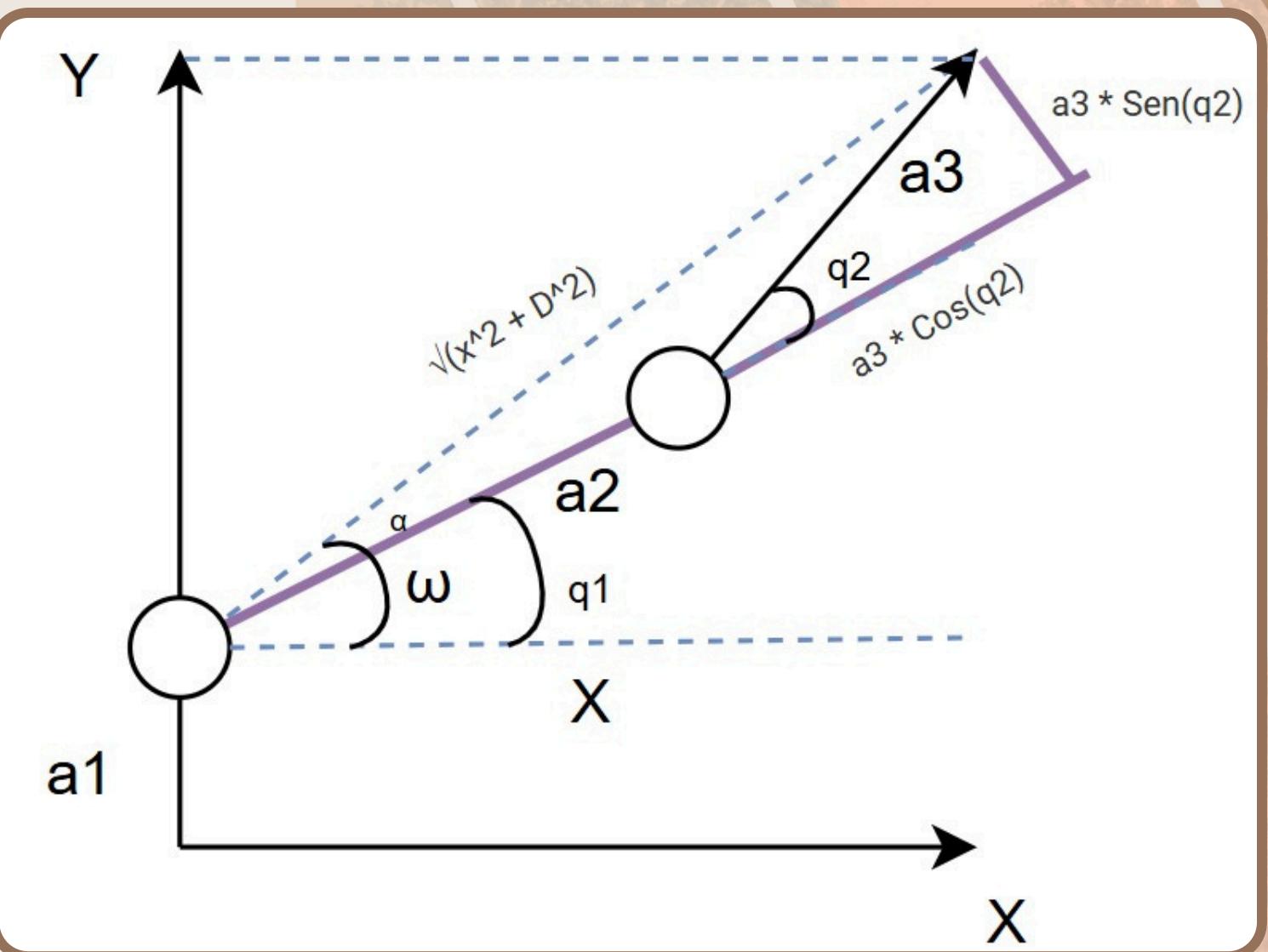
$$(q2) = \arccos * \left( \frac{x^2 + D^2 - a_2^2 - a_3^2}{2a_2a_3} \right)$$

Para q1:

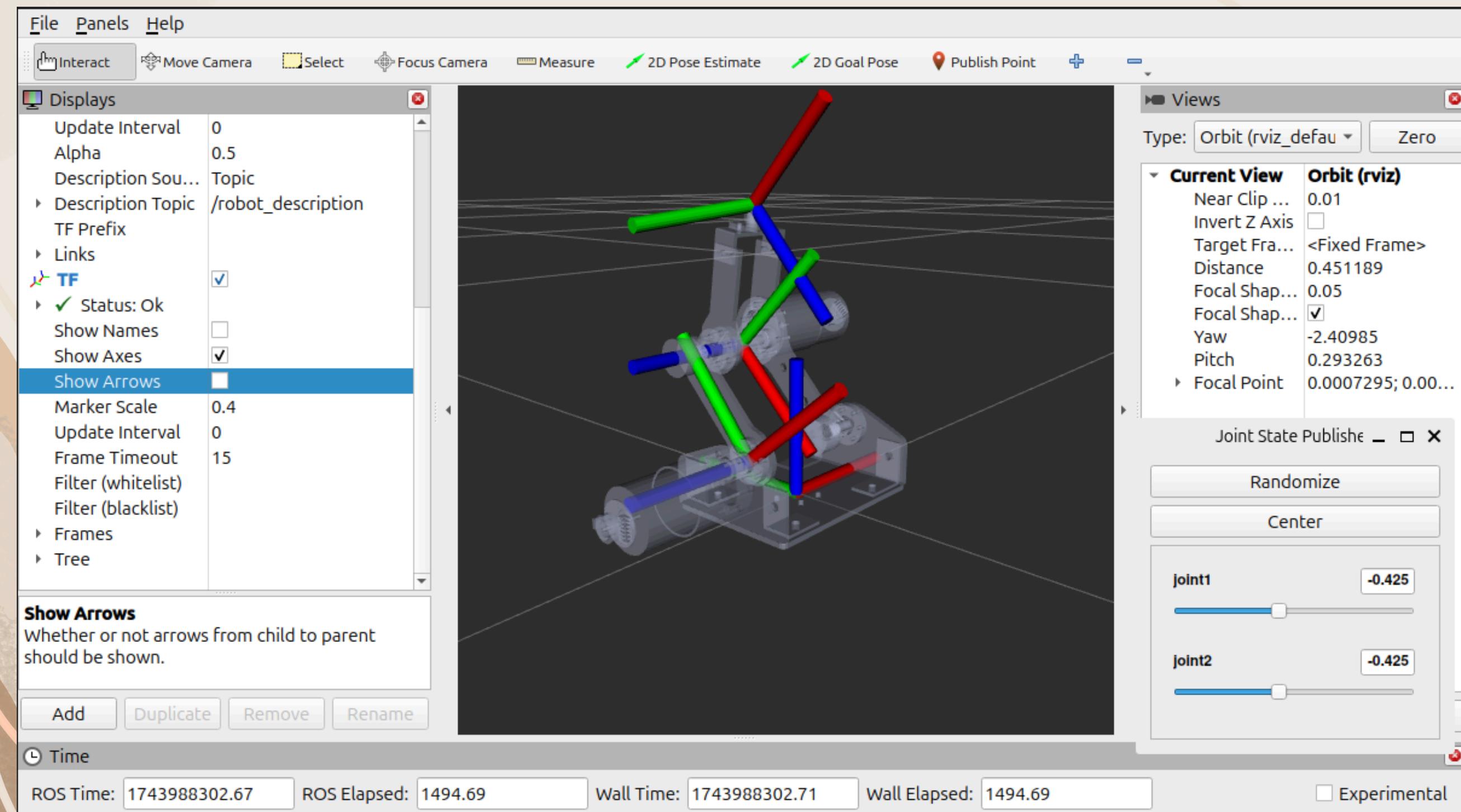
$$q1 = w - a$$

$$(q1) = \text{atan} * \left( \frac{D}{X} \right) - a$$

$$(q1) = \text{atan} * \left( \frac{D}{X} \right) - \text{atan} * \left( \frac{a_3 * \text{sen}(q2)}{a_2 + a_3 * \text{Cos}(q2)} \right)$$



# Visualización del modelo en Rviz





**GRACIAS**