

---

# DIC L10: MOSFET (4)

Sung-Min Hong ([smhong@gist.ac.kr](mailto:smhong@gist.ac.kr))

Semiconductor Device Simulation Lab.  
School of Electrical Engineering and Computer Science  
Gwangju Institute of Science and Technology

## 2.4. Nonideal IV (6)

---

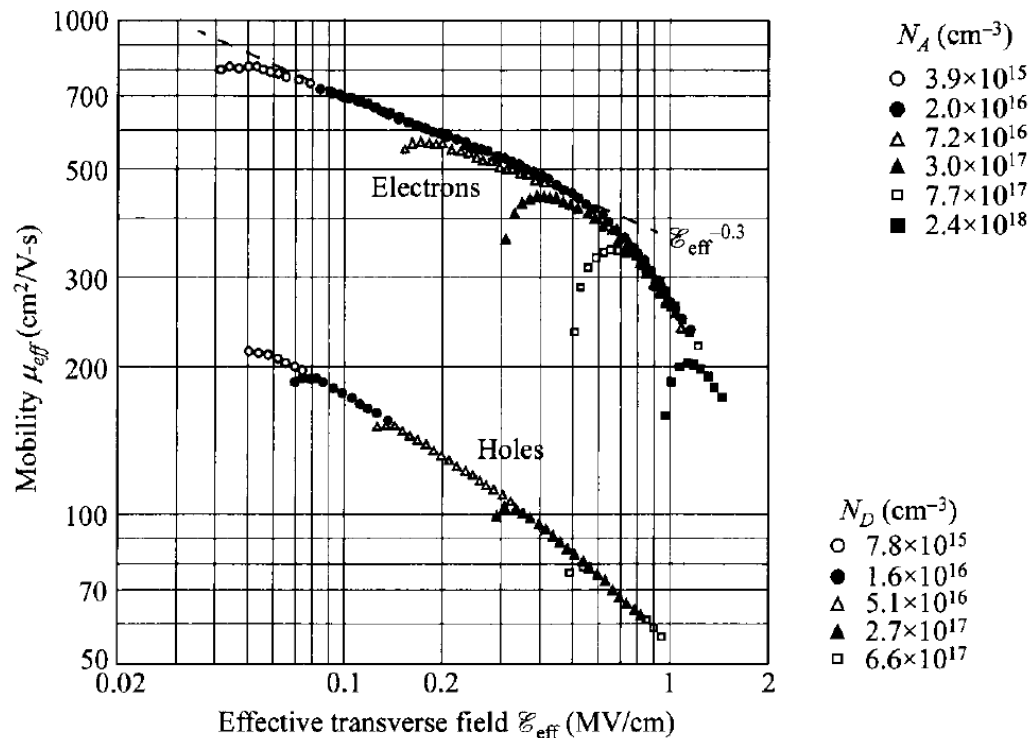
- Mobility degradation due to the vertical E-field
  - Collisions with oxide interface

$$\mu_{\text{eff}-n} = \frac{540 \frac{\text{cm}^2}{\text{V} \cdot \text{s}}}{1 + \left( \frac{V_{gs} + V_t}{0.54 \frac{\text{V}}{\text{nm}} t_{\text{ox}}} \right)^{1.85}} \quad \mu_{\text{eff}-p} = \frac{185 \frac{\text{cm}^2}{\text{V} \cdot \text{s}}}{1 + \frac{\left| V_{gs} + 1.5V_t \right|}{0.338 \frac{\text{V}}{\text{nm}} t_{\text{ox}}}} \quad \text{Eq. (2.23)}$$

- Why do we have different behaviors for electrons and holes?

## 2.4. Nonideal IV (7)

- Experimental data (So-called “universal” mobility)



Inversion-layer  
mobility (Sze's  
book)

## 2.4. Nonideal IV (8)

---

- Example 2.3
  - Calculation of the mobilities at  $|V_{gs}| = 1.0$  V. Assume that  $t_{ox} = 1.05$  nm and  $|V_t| = 0.3$  V.

```
>> 540 / (1 + ((1.0+0.3)/(0.54*1.05))^1.85)
```

```
ans =
```

```
95.7177
```

```
>> 185 / (1 + ((1.0+1.5*0.3)/(0.338*1.05))^1.0)
```

```
ans =
```

```
36.3768
```

## 2.4. Nonideal IV (9)

- Velocity saturation
  - Saturation velocity (Canali model)
    - Electrons:  $1.07 \times 10^7$  cm/sec
    - Holes:  $8.37 \times 10^6$  cm/sec
  - Simple model

$$v = \begin{cases} \frac{\mu_{\text{eff}} E}{1 + \frac{E}{E_c}} & E < E_c \\ v_{\text{sat}} & E \geq E_c \end{cases} \quad E_c = \frac{2v_{\text{sat}}}{\mu_{\text{eff}}}$$

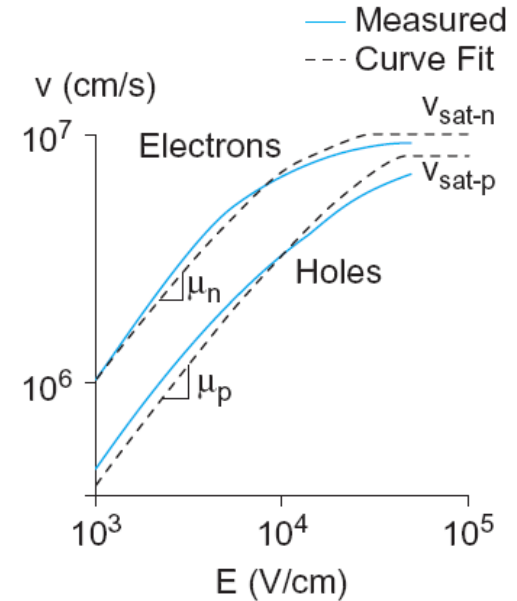


Fig. 2.15

## 2.4. Nonideal IV (10)

---

- Example 2.4

- Then, the critical fields are given by 208 kV/cm (electrons) and 444 kV/cm (holes), respectively.
- Assume that the channel length is 50 nm.
- Then, at 1.04 V (NMOS) and 2.22 V (PMOS), the carrier velocities are saturated.
- The NMOS transistor is velocity saturated in normal operation.

>> 2 \* 1e7 / 96

ans =

2.0833e+05

>> 2 \* 8e6 / 36

ans =

4.4444e+05

## 2.4. Nonideal IV (11)

---

- Saturation current
  - Simplified expression

$$I_{dsat} = W C_{ox} v_{sat} \frac{V_{GT}^2}{V_{GT} + V_c}$$

- One extreme ( $V_{GT} \ll V_c$ )

$$I_{dsat} = W C_{ox} v_{sat} \frac{V_{GT}^2}{V_c}$$

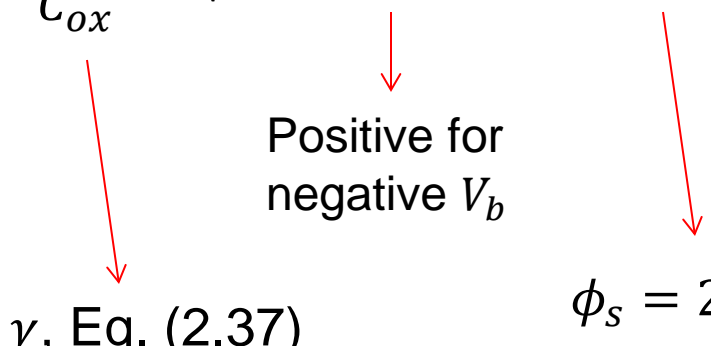
- Another one ( $V_{GT} \gg V_c$ )

$$I_{dsat} = W C_{ox} v_{sat} V_{GT}$$

## 2.4. Nonideal IV (12)

---

- Threshold voltage (Body effect)
  - It is given by

$$V_t = \frac{\sqrt{2\epsilon_{si}qN_A}}{C_{ox}} \sqrt{\phi_s + V_{sb}} + V_{FB} + \phi_s$$


Positive for  
negative  $V_b$

$\gamma$ , Eq. (2.37)

$$\phi_s = 2v_T \log \frac{N_A}{n_i}, \text{ Eq. (2.36)}$$

- Written as

$$V_t = V_{t0} + \gamma (\sqrt{\phi_s + V_{sb}} - \sqrt{\phi_s})$$



## 2.4. Nonideal IV (13)

- Leakage
  - Subthreshold slope
  - DIBL
  - GIDL

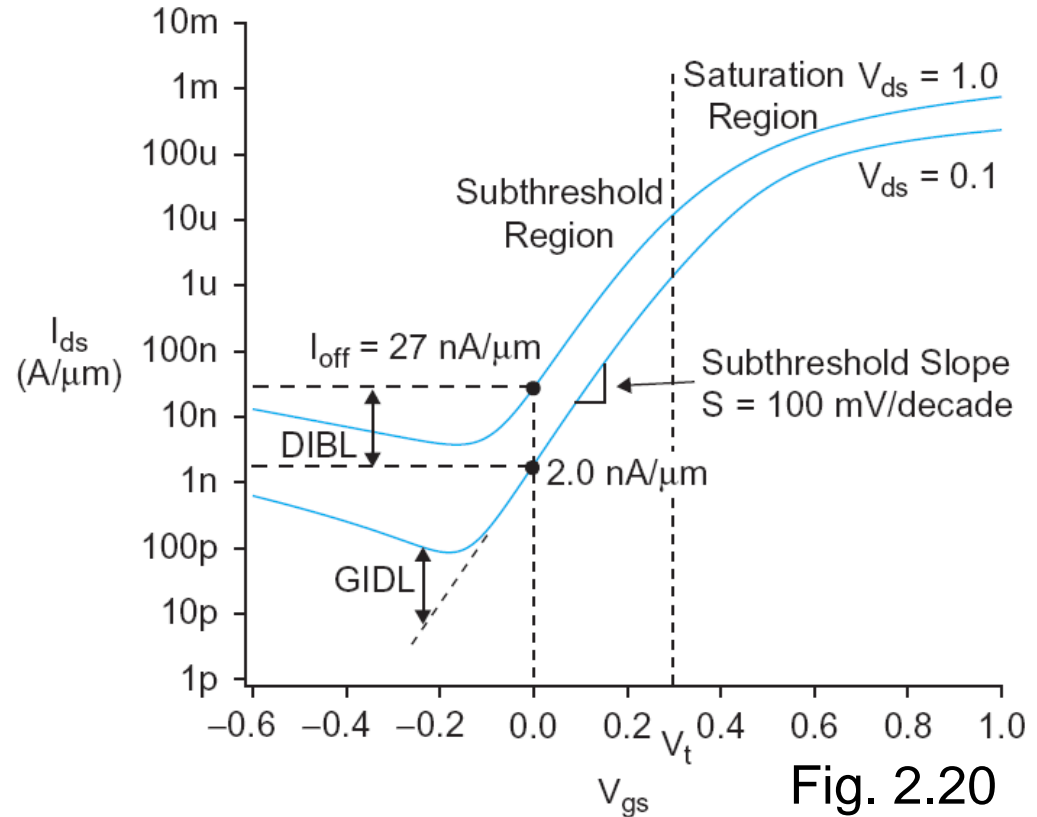


Fig. 2.20

# Homework#4

---

- Write a report.
  - Select a CMOS technology. (It's up to you.)
  - Describe its electrical characteristics. (Free style!)
  - Explicitly show your reference.
- Due: October 22, 2019 (Before the lecture starts)
  - Upload your Homework to our GitHub repository.