1. (Ex 2.1)

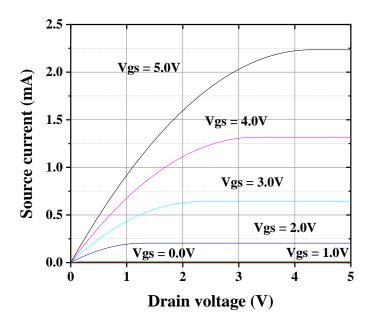
We can draw Id vs. Vds graph for Vgs with this equation.(from lecture material)

Subthreshold 
$$I_d=0$$
  
Linear  $I_d=\beta\left(V_{gs}-V_t-\frac{V_{ds}}{2}\right)V_{ds}$   
Saturation  $I_d=\frac{\beta}{2}\left(V_{gs}-V_t\right)^2$ 

With,

$$\beta = \mu_n C_{OX} \frac{W}{L}$$

Then, result is here.



At their linear region,

$$I_{\!d2} = \mu_n C_{\!O\!X} \frac{W}{L} \! \left( V_{\!D\!D} \! - V_t \! - \frac{V_{\!D\!S} \! - V_1}{2} \right) \! (V_{\!D\!S} \! - V_1) \label{eq:eq:ld2}$$

$$I_{\!d2} = \mu_n C_{\!O\!X} \frac{W}{L} \! \left( V_{\!D\!D} \! - V_1 \! - V_t \! - \! \frac{V_1}{2} \right) V_1 \label{eq:id2}$$

Then,

$$V_{1} = \, V_{D\!D} - \, V_{t} - \sqrt{(\,V_{D\!D} - \,V_{t})^{2} - \left(\,V_{D\!D} - \,V_{t} - \frac{\,V_{D\!S}}{2}\,\right) V_{D\!S}}$$

Therefore,

$$I_{d2} = \mu_n C_{OX} \frac{W}{2L} \left( V_{DD} - V_t - \frac{V_{DS}}{2} \right) V_{DS} = I_{d1}$$

3. (Ex 2.3)

(a)에서는 source와 body에 같은 전압이 인가되었지만, (b)의 윗쪽 nmos에서는 source에 비해 body에 낮은 전압이 인가되었다. 이는 p-type인 body 부분의 reverse bias를 걸어주는 것이므로, electrostatic potential은 감소하게 되고, 그에 따라 depletion region의 두께가 증가하게 된다. 그러므로 V th가 상승하는 것과 비슷한 결과를 얻게 되므로, 전체적인 전류의 량은 줄어들게 된다.

$$I_d1 > I_d2$$

4. (Ex 2.4)

$$C_{g/mow} = C_{ox}L \frac{1.0m}{10^{-6}\mu m} = \frac{\varepsilon_{OX}}{t_{OX}}L \frac{1.0m}{10^{-6}\mu m} = \frac{3.9\varepsilon_0}{16 \times 10^{-10}m} \times 90 \times 10^{-9}m \times \frac{1.0m}{10^{6}\mu m}$$

$$C_{g/mow} = 1.9424 \times 10^{-15} \, \text{F}/\mu \text{m} = 1.9424 \times \, \text{fF}/\mu \text{m}$$

5. (Ex 2.5)

$$\begin{split} C_{db}(0) &= (4\lambda \times 5\lambda)(0.42\,\mathrm{fF}/\mu\mathrm{m}^2) + 2\times (4\lambda + 5\lambda)(0.33\,\mathrm{fF}/\mu\mathrm{m}^2) = 2.538\,\mathrm{fF} \\ C_{db}(5) &= (4\lambda \times 5\lambda)(0.42\,\mathrm{fF}/\mu\mathrm{m}^2) \left(1 + \frac{5}{0.98}\right)^{-0.44} + 2\times (4\lambda + 5\lambda)(0.33\,\mathrm{fF}/\mu\mathrm{m}^2) \left(1 + \frac{5}{0.98}\right)^{-0.12} = 1.775\,\mathrm{fF} \end{split}$$

6.

$$\begin{split} I_{d}dx &= \mu_{n}C_{ox}W(\ V_{gs} - V(x) - V_{t})d\ V \\ I_{d}x &= \mu_{n}C_{ox}W(\ V_{gs} - \frac{V(x)}{2} - V_{t})\ V(x) \\ &\frac{V(x)^{2}}{2} - (\ V_{gs} - V_{t})\ V(x) + \frac{I_{d}x}{\mu_{n}C_{ox}W} = 0 \\ &\therefore \ V(x) = (\ V_{gs} - V_{t}) \pm \sqrt{(\ V_{gs} - V_{t})^{2} - \frac{2I_{d}x}{\mu_{n}C_{ox}W}} \end{split}$$

When x = 180nm,  $V(x) = V_ds$ .

$$\therefore V(x) = (V_{gs} - V_t) - \sqrt{(V_{gs} - V_t)^2 - \frac{2I_dx}{\mu_n C_{ox} W}}$$

