


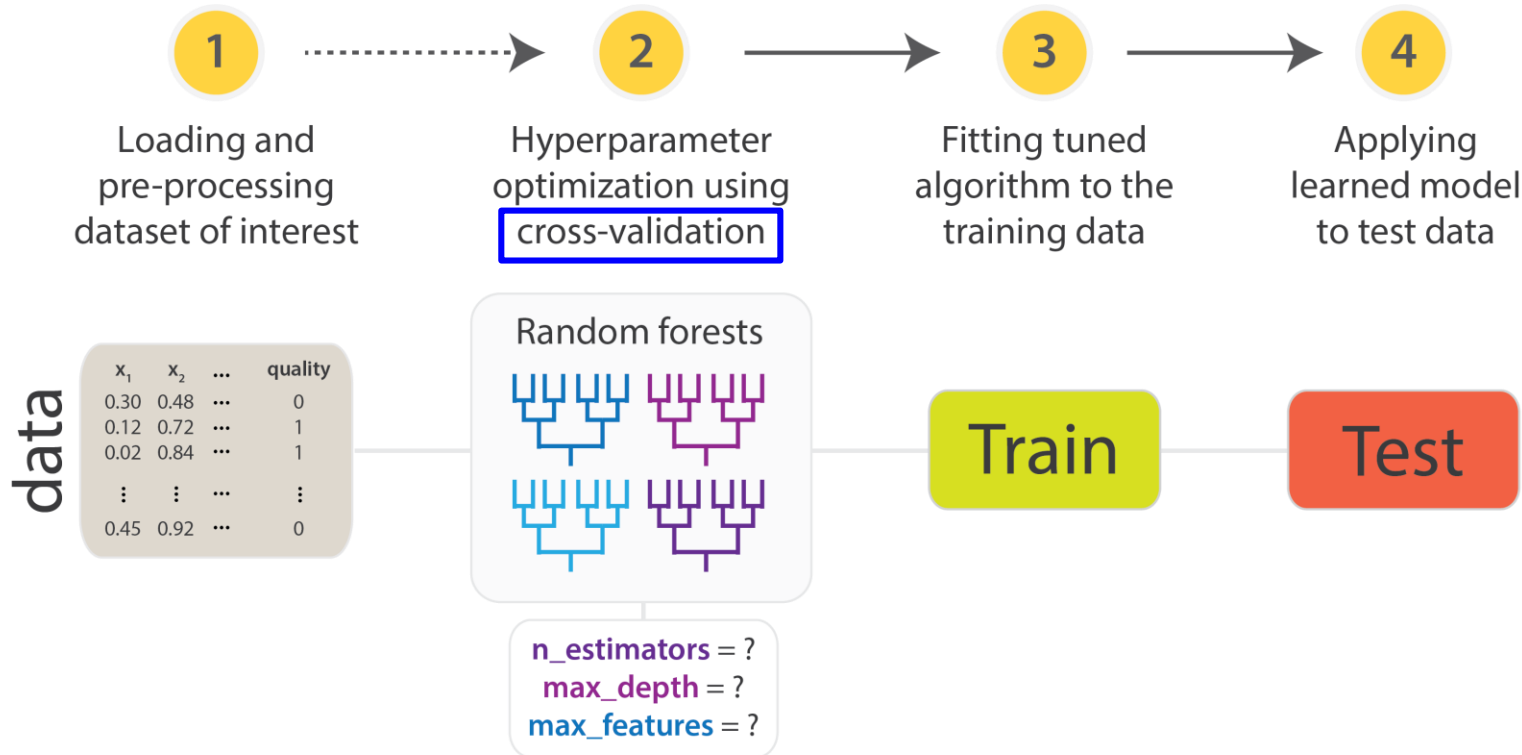


4. Cross Validation

KUBIG 학술부



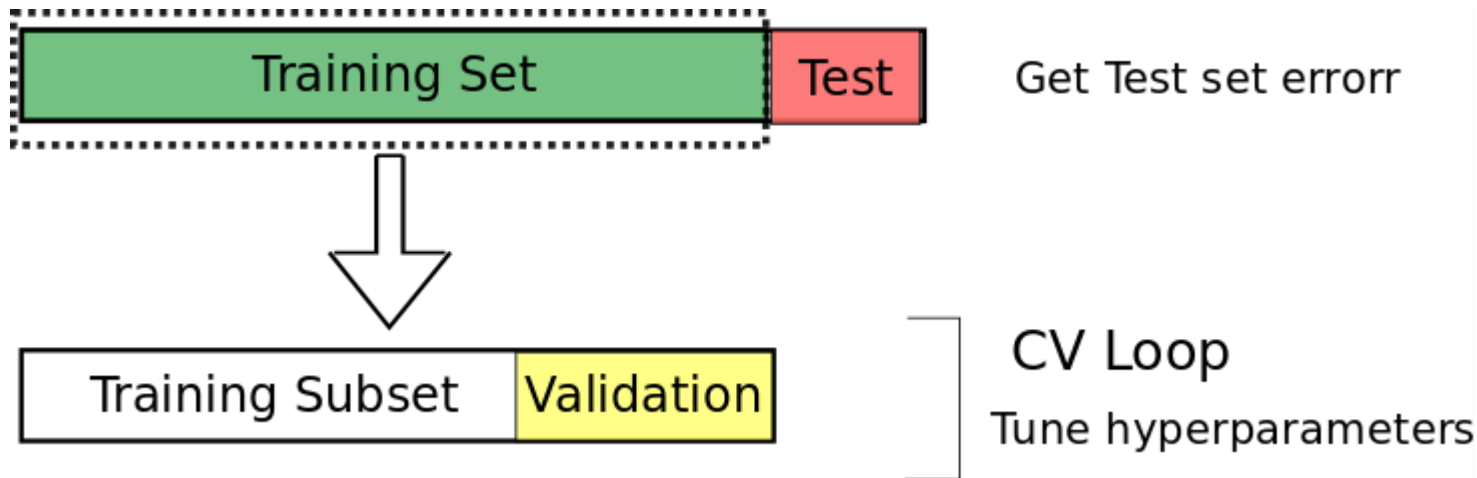
Hyperparameter tuning



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2. LOOCV (leave-one-out-cross-validation)
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1. Hold-out Cross Validation



0. 데이터를 Training set과 Test set으로 나눈다.
1. Training set을 다시 Training Subset과 Validation set으로 한번 나눈다.
2. Training Subset으로 학습한 모델이 Validation set에서 가장 좋은 성능을 내는 hyperparameter를 선택

```
In [1]: import pandas as pd
import numpy as np
from sklearn.datasets import load_iris
from sklearn.model_selection import train_test_split, ShuffleSplit, GridSearchCV
from sklearn.tree import DecisionTreeClassifier
from sklearn.metrics import accuracy_score
```

```
In [13]: rsf=rs.split(train_set_X,train_set_y)

for iteration, data in enumerate(rsf, start=1):
    print('\n{} {:^61}'.format('Iteration', 'Training subset observations'))
    print('\n{:^9} {}'.format(iteration, data[0]))
    print('\n{}{:^61}'.format('Validation set observations'))
    print('\n{:^9}'.format(str(data[1])))
```

```
Iteration           Training subset observations

1      [ 35 34 84 43 46 102 49 39 96 33 87 12 19 106 115 17 7 95
107 0 1 18 69 92 61 111 22 116 79 66 23 13 86 58 53 45
113 77 112 31 109 16 60 29 90 38 91 72 51 55 24 81 41 40
59 9 103 83 99 11 30 26 47 94 57 56 65 2 15 21 37 108
62 118 80 78 10 8 50 5 4 28 104 14 98 117 42 74 67 54
48 52 110 82 75 89]
```

```
Validation set observations

[ 25 68 101 44 105 64 100 119 93 85 6 73 27 97 32 20 71 88
63 3 114 36 70 76]
```

Iris data에는 150개의 관측치가 있다.

→ $150 \times 0.8 \times 0.8 = 96$ 개

→ $150 \times 0.8 \times 0.2 = 24$ 개

$150 - (96 + 24) = 150 \times 0.2 = 30$, Test data

```
In [2]: iris=load_iris()
train_set_X, test_set_X, train_set_y, test_set_y=train_test_split(iris.data,
                                                                    iris.target,
                                                                    test_size=0.2,
                                                                    random_state=1)
```

전체 data를 Training set과 Test set으로 분리

```
model=DecisionTreeClassifier()
param={
    'max_depth':[1,2,3],
    'min_samples_leaf':[2,3]
}
```

Tuning할 hyperparameter

Training set을 training subset과 validation set으로 분리해줄 CV splitter

```
rs=ShuffleSplit(n_splits=1, test_size=0.2)
Dtr=GridSearchCV(cv=rs, estimator=model, param_grid=param, scoring='accuracy')
Dtr.fit(train_set_X, train_set_y)
print('Model performance : ',
      accuracy_score(test_set_y, Dtr.predict(test_set_X)))
```

Model performance : 0.8666666666666667

```

In [17]: iris=load_iris()

model=DecisionTreeClassifier()
param={
    'max_depth':[1,2,3],
    'min_samples_leaf':[2,3]
}

for i in range(10):
    train_set_X, test_set_X,train_set_y, test_set_y=train_test_split(iris.data
                                                                    iris.target,
                                                                    test_size=0.2)

    rs=ShuffleSplit(n_splits=1,test_size=0.2)
    Dtr=GridSearchCV(cv=rs,estimator=model,param_grid=param,scoring='accuracy'
    Dtr.fit(train_set_X,train_set_y)
    print('Model performance : ',
          accuracy_score(test_set_y, Dtr.predict(test_set_X)),
          'Best parameter : ',
          Dtr.best_params_)

```

```

Model performance : 0.8666666666666667 Best parameter : {'max_depth': 2, 'min_samples_leaf': 2}
Model performance : 0.9333333333333333 Best parameter : {'max_depth': 3, 'min_samples_leaf': 2}
Model performance : 0.9 Best parameter : {'max_depth': 2, 'min_samples_leaf': 2}
Model performance : 0.9333333333333333 Best parameter : {'max_depth': 2, 'min_samples_leaf': 2}
Model performance : 0.9333333333333333 Best parameter : {'max_depth': 2, 'min_samples_leaf': 2}
Model performance : 0.9666666666666667 Best parameter : {'max_depth': 2, 'min_samples_leaf': 2}
Model performance : 0.9666666666666667 Best parameter : {'max_depth': 3, 'min_samples_leaf': 3}
Model performance : 1.0 Best parameter : {'max_depth': 3, 'min_samples_leaf': 3}
Model performance : 0.9333333333333333 Best parameter : {'max_depth': 2, 'min_samples_leaf': 2}
Model performance : 0.9333333333333333 Best parameter : {'max_depth': 2, 'min_samples_leaf': 2}

```

```
In [17]: iris=load_iris()

model=DecisionTreeClassifier()
param={
    'max_depth':[1,2,3],
    'min_samples_leaf':[2,3]
}

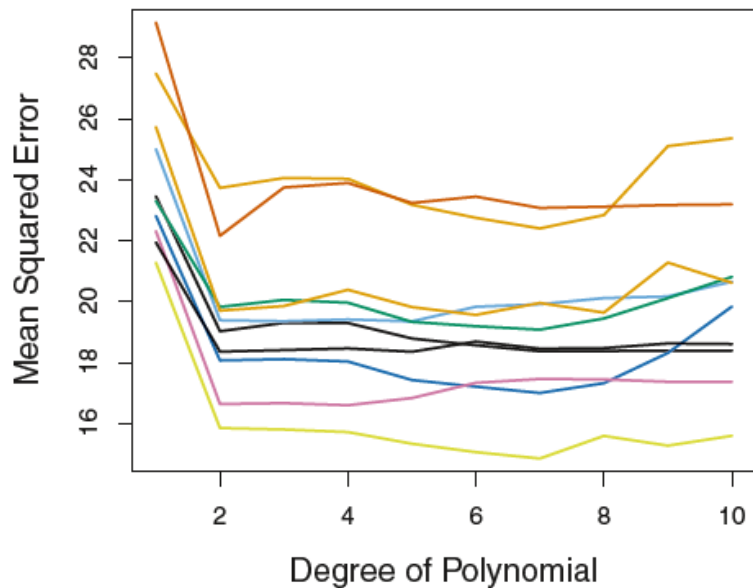
for i in range(10):
    train_set_X, test_set_X,train_set_y, test_set_y=train_test_split(iris.data
                                                                    iris.target,
                                                                    test_size=0.2)

    rs=ShuffleSplit(n_splits=1,test_size=0.2)
    Dtr=GridSearchCV(cv=rs,estimator=model,param_grid=param,scoring='accuracy')
    Dtr.fit(train_set_X,train_set_y)
    print('Model performance : ',
          accuracy_score(test_set_y, Dtr.predict(test_set_X)),
          'Best parameter : ',
          Dtr.best_params_)
```

Random한 split이 어떻게 이뤄지느냐에 따라 추정값이 크게 달라짐.

Model performance : 0.8666666666666667	Best parameter : {'max_depth': 2, 'min_samples_leaf': 2}
Model performance : 0.9333333333333333	Best parameter : {'max_depth': 3, 'min_samples_leaf': 2}
Model performance : 0.9	Best parameter : {'max_depth': 2, 'min_samples_leaf': 2}
Model performance : 0.9333333333333333	Best parameter : {'max_depth': 2, 'min_samples_leaf': 2}
Model performance : 0.9333333333333333	Best parameter : {'max_depth': 2, 'min_samples_leaf': 2}
Model performance : 0.9666666666666667	Best parameter : {'max_depth': 2, 'min_samples_leaf': 2}
Model performance : 0.9666666666666667	Best parameter : {'max_depth': 3, 'min_samples_leaf': 3}
Model performance : 1.0	Best parameter : {'max_depth': 3, 'min_samples_leaf': 3}
Model performance : 0.9333333333333333	Best parameter : {'max_depth': 2, 'min_samples_leaf': 2}
Model performance : 0.9333333333333333	Best parameter : {'max_depth': 2, 'min_samples_leaf': 2}

Hold-out Cross Validation의 단점



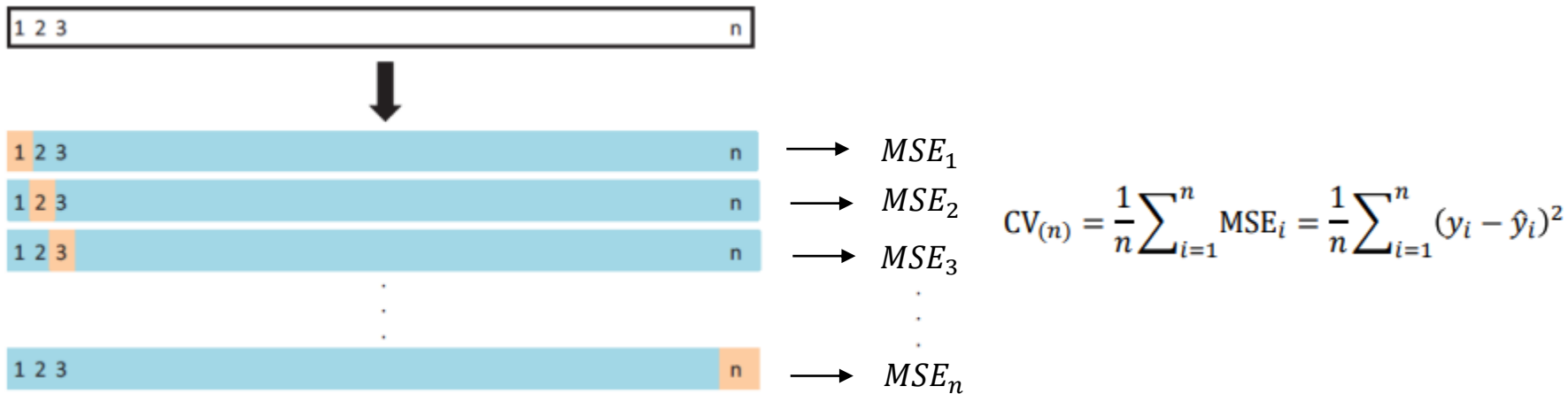
‘Auto’ dataset으로 Hold-out Cross Validation을 반복적으로 적용해 봄

동일한 데이터로 10번 해본 결과 매번 결과가 다를 수 있음.

Split에 randomness가 있고 random한 split을 한번만 하기 때문

출처 : *An introduction to statistical learning with Applications in R*

2. LOOCV(leave-one-out-cross validation)



1. 관측치가 n개인 training set을 관측치가 1개인 validation set과 관측치가 (n-1)개인 training subset으로 나눈다.
2. 각각의 관측치들이 한번씩 validation set이 되도록 1번 과정을 n번 반복하며 metric을 구한다.
3. 이 n개 metric의 평균을 기준으로 가장 좋은 성능을 보여주는 hyper parameter를 선택한다.

```
In [1]: import pandas as pd
import numpy as np
from sklearn.datasets import load_iris
from sklearn.model_selection import train_test_split, LeaveOneOut, GridSearchCV
from sklearn.tree import DecisionTreeClassifier
from sklearn.metrics import accuracy_score
```

```
In [13]: loof=loo.split(train_set_X,train_set_y)

for iteration, data in enumerate(loof, start=1):
    print('\n{} {}: ^61}'.format('Iteration', 'Training subset observations'))
    print('\n{}: ^9} {}'.format(iteration, data[0]))
    print('\n{}: ^70}'.format('Validation set observations'))
    print('\n{}: ^70}'.format(str(data[1])))
```

```
Iteration           Training subset observations
1      [ 1  2  3  4  5  6  7  8  9 10 11 12 13 14 15 16 17 18
19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36
37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54
55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72
73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90
91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 106 107 108
109 110 111 112 113 114 115 116 117 118 119]
```

Validation set observations

[0]

Iris data에는 150개의 관측치가 있다.

$(150 \times 0.8) - 1 = 119$ 개

1개

$150 - 119 - 1 = 150 \times 0.2 = 30$, Test data

Iteration Training subset observations

2	[0	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36		
37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54		
55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72		
73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90		
91	92	93	94	95	96	97	98	99	100	101	102	103	104	105	106	107	108		
109	110	111	112	113	114	115	116	117	118	119									

Validation set observations

[1]

Iteration Training subset observations

3	[0	1	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	
37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	
55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	
73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	
91	92	93	94	95	96	97	98	99	100	101	102	103	104	105	106	107	108	
109	110	111	112	113	114	115	116	117	118	119								

Validation set observations

[2]

Iteration Training subset observations

120	[0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35		
36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53		
54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71		
72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89		
90	91	92	93	94	95	96	97	98	99	100	101	102	103	104	105	106	107		
108	109	110	111	112	113	114	115	116	117	118									

Validation set observations

[119]

In [3]:

```
iris=load_iris()
train_set_X, test_set_X, train_set_y, test_set_y=train_test_split(iris.data,
                                                                    iris.target,
                                                                    test_size=0.2,
                                                                    random_state=4)
```

전체 data를 Training set과 Test set으로 분리

```
model=DecisionTreeClassifier()
param={
    'max_depth':[1,2,3],
    'min_samples_leaf':[2,3]
}
```

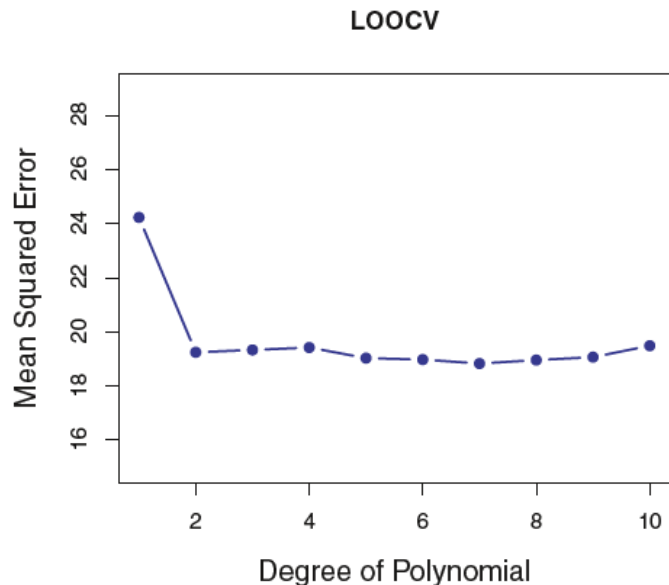
) Tuning할 hyperparameter

Training set을 training subset과 validation set으로 분리해줄 CV splitter

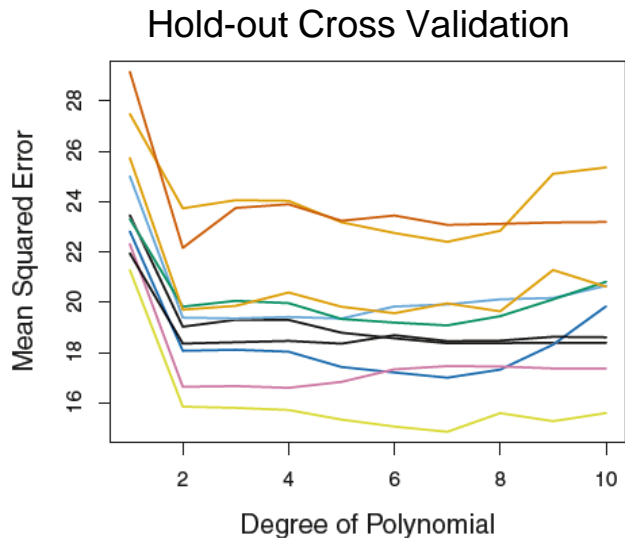
```
loo=LeaveOneOut()
Dtr=GridSearchCV(cv=loo, estimator=model, param_grid=param, scoring='accuracy')
Dtr.fit(train_set_X, train_set_y)
print('Model performance : ',
      accuracy_score(test_set_y, Dtr.predict(test_set_X)))
```

Model performance : 0.9666666666666667

LOOCV의 장점

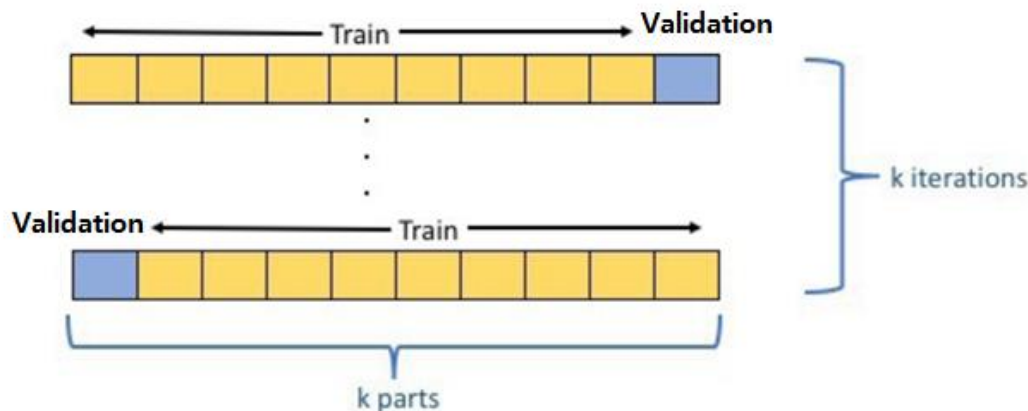


VS



LOOCV는 Training set이 어떻게 Training subset과 validation set으로 나뉘는지에 randomness가 없음.
따라서, Training set이 동일하다면 항상 같은 결과를 반환함.

3. k-fold cross validation



$$CV_{(k)} = \frac{1}{k} \sum_{i=1}^k MSE_i.$$

1. Training set을 동일한 크기의 k개의 그룹으로 나눈다.
2. K개의 그룹 중 (k-1)개의 그룹에 해당하는 data들을 training subset으로 하고 나머지 1개의 그룹에 해당하는 data들을 validation set으로 한다.
3. 모든 그룹이 한번씩 validation set이 되도록 2번 과정을 k번 반복하며 K개의 metric을 구한 후 평균을 내서 가장 좋은 성능을 보여주는 hyperparameter를 선택한다.

```
In [1]: from sklearn.datasets import load_iris
from sklearn.tree import DecisionTreeClassifier
from sklearn.model_selection import train_test_split, KFold, GridSearchCV
from sklearn.metrics import accuracy_score
```

```
In [65]: kf = KFold(n_splits=5, shuffle=False).split(train_set_X,train_set_y)

for iteration, data in enumerate(kf, start=1):
    print('\n{} {:^61}'.format('Iteration', 'Training subset observations'))
    print('\n{:^9} {}'.format(iteration, data[0]))
    print('\n{:^61}'.format('Validation set observations'))
    print('\n{:^9}'.format(str(data[1])))
    print('\n{:^61}'.format("Test set observations"))
    print('\n',np.arange(iris.data.shape[0]-test_set_X.shape[0],
                        iris.data.shape[0],1))
```


Iteration Training subset observations

1 [24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41
 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59
 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77
 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95
 96 97 98 99 100 101 102 103 104 105 106 107 108 109 110 111 112 113
 114 115 116 117 118 119]

Validation set observations

[0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23]

Test set observations

[120 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137
 138 139 140 141 142 143 144 145 146 147 148 149]

Iteration Training subset observations

⑤ [0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23
 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47
 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71
 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95]

Validation set observations

[96 97 98 99 100 101 102 103 104 105 106 107 108 109 110 111 112 113
 114 115 116 117 118 119]

Test set observations

[120 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137
 138 139 140 141 142 143 144 145 146 147 148 149]

Iteration Training subset observations

2 [0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17
 18 19 20 21 22 23 48 49 50 51 52 53 54 55 56 57 58 59
 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77
 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95
 96 97 98 99 100 101 102 103 104 105 106 107 108 109 110 111 112 113
 114 115 116 117 118 119]

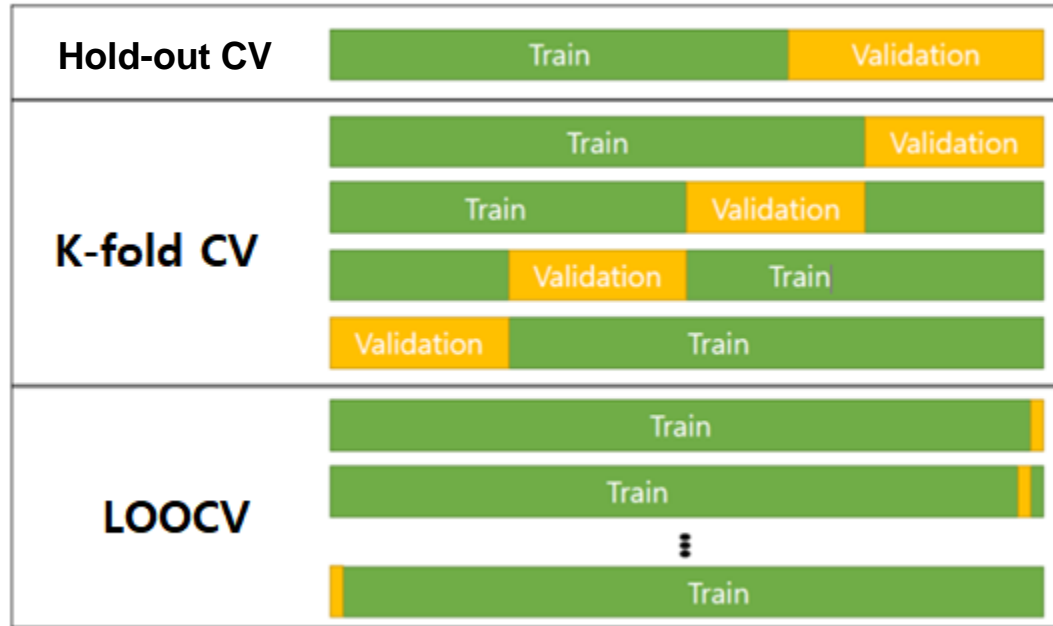
Validation set observations

[24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47]

Test set observations

[120 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137
 138 139 140 141 142 143 144 145 146 147 148 149]

Hold-out CV, K-fold CV, LOOCV



Time series data를 위한 Cross Validation

1. Temporal dependence

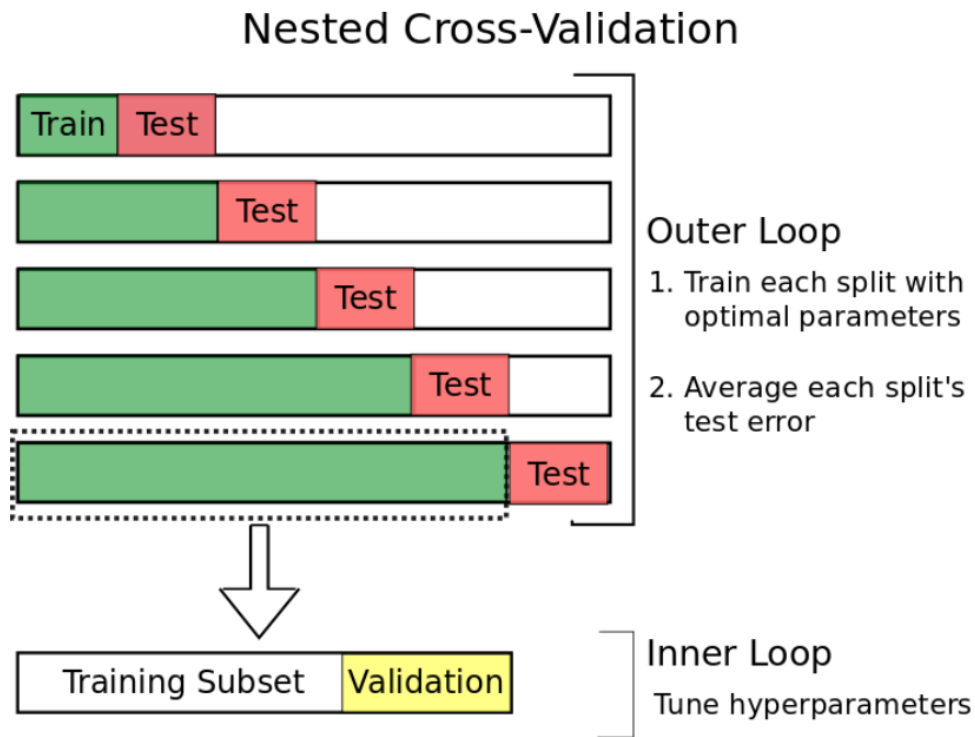
- 시간 순서가 있는 time series data를 random하게 training subset, validation set으로 나눌 수 없다.
- 어느 시점부터를 test data로 나눌지가 자의적임. Biased estimator가 될 가능성이 높음

2. 과거의 데이터를 이용해 미래를 예측해야 함.

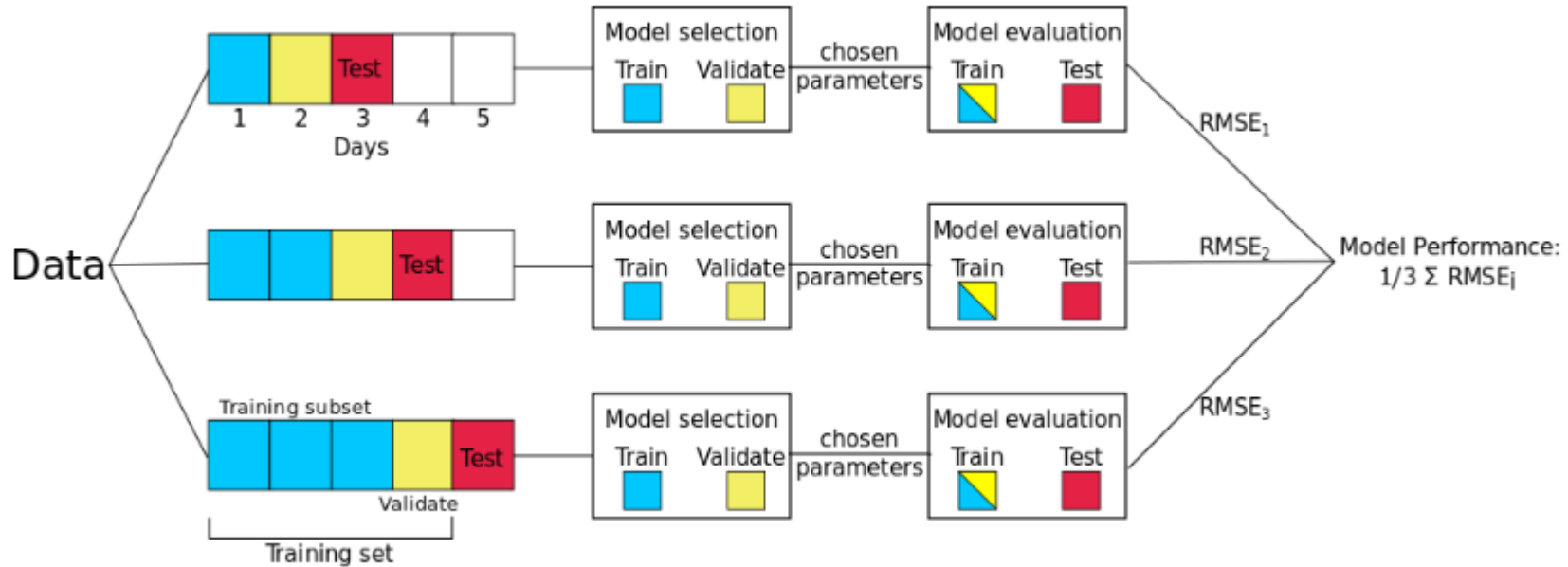
- 미래의 데이터로 과거의 데이터를 예측하는 상황을 원하지 않음.

따라서, k-fold cross validation 사용이 곤란

4. Nested Cross Validation



Day forward chaining



```
In [1]: import pandas as pd
import numpy as np
from sklearn.model_selection import TimeSeriesSplit, GridSearchCV
from sklearn.linear_model import ElasticNet
from sklearn.metrics import mean_absolute_error

df=pd.read_csv("C:/Users/jjw11/Desktop/고려대학교/학회/data/Gemini_ETHUSD_d.csv")
df.head()
```

```
Out[1]:
```

	Date	Symbol	Open	High	Low	Close	Volume ETH	Volume USD
0	2019-09-14	ETHUSD	181.55	181.55	181.43	181.43	0.00	0.00
1	2019-09-13	ETHUSD	180.88	181.80	177.70	181.55	4447.19	798113.88
2	2019-09-12	ETHUSD	178.47	182.60	176.45	180.88	2749.15	491636.33
3	2019-09-11	ETHUSD	179.61	182.70	173.70	178.47	12741.56	2270428.10
4	2019-09-10	ETHUSD	181.04	184.35	176.68	179.61	8576.85	1544625.31

```
In [2]: df=df.drop(['Symbol'],axis=1)
df=df.sort_values(by='Date').set_index('Date')
df2=df.iloc[:100,: ]
df2.head()
```

```
Out[2]:
```

	Open	High	Low	Close	Volume ETH	Volume USD
Date						
2016-05-09	12.00	12.00	9.36	9.98	1317.90	12885.06
2016-05-10	9.98	9.98	9.36	9.68	672.06	6578.20
2016-05-11	9.68	10.47	9.68	10.43	3052.51	30978.11
2016-05-12	10.43	12.00	9.92	10.20	2072.56	22183.39
2016-05-13	10.20	11.59	10.20	10.69	1769.71	18923.55

```
In [32]: model=ElasticNet()
param={'alpha':np.arange(0.1,10,0.1)}
tscv=TimeSeriesSplit(n_splits=95)
```

```
In [33]: mae=[]

X=df2[['Open','High','Low','Volume ETH','Volume USD','Close']]
X=X.iloc[:-1,]
y=df2['Close'].shift(periods=-1)
y=y.iloc[:-1,]

Els=GridSearchCV(cv=tscv, estimator=model, param_grid=param,
                  scoring='neg_mean_absolute_error')
Els.fit(X,y)

for train_index, Validation_index in tscv.split(df2):
    if Validation_index==df2.shape[0]-2:
        break

    print("TRAIN subset:", train_index, "\nValidation set:",
          Validation_index, "\ntest set:", Validation_index+1)

    X_test=X.iloc[Validation_index+1,:]
    y_test=y.iloc[Validation_index+1]

    mae.append(mean_absolute_error(y_test,Els.predict(X_test)))

print(' Model performance : ',np.mean(mae))
```

```
TRAIN subset: [0 1 2 3 4]
Validation set: [5]
test set: [6]
TRAIN subset: [0 1 2 3 4 5]
Validation set: [6]
test set: [7]
TRAIN subset: [0 1 2 3 4 5 6]
Validation set: [7]
test set: [8]
TRAIN subset: [0 1 2 3 4 5 6 7]
Validation set: [8]
test set: [9]
```

```
TRAIN subset: [ 0  1  2  3  4  5  6  7  8  9 10 11 12 13 14 15 16 17 18 19 20 21 22 23
 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47
 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71
 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95]
Validation set: [96]
test set: [97]
TRAIN subset: [ 0  1  2  3  4  5  6  7  8  9 10 11 12 13 14 15 16 17 18 19 20 21 22 23
 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47
 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71
 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95
 96]
Validation set: [97]
test set: [98]
Model performance : 0.6953183352916578
```

```
In [32]: model=ElasticNet()
param={'alpha':np.arange(0.1,10,0.1)}
tscv=TimeSeriesSplit(n_splits=95)
```

```
In [33]: mae=[]

X=df2[['Open','High','Low','Volume ETH','Volume USD','Close']]
X=X.iloc[:-1,]
y=df2['Close'].shift(periods=-1)
y=y.iloc[:-1,]

Els=GridSearchCV(cv=tscv, estimator=model, param_grid=param,
                  scoring='neg_mean_absolute_error')
Els.fit(X,y)
```

Inner Loop??

```
for train_index, Validation_index in tscv.split(df2):
    if Validation_index==df2.shape[0]-2:
        break

    print("TRAIN subset:", train_index, "\nValidation set:",
          Validation_index, "\ntest set:", Validation_index+1)

    X_test=X.iloc[Validation_index+1,:]
    y_test=y.iloc[Validation_index+1]

    mae.append(mean_absolute_error(y_test,Els.predict(X_test)))

print(' Model performance : ',np.mean(mae))
```

```
TRAIN subset: [0 1 2 3 4]
Validation set: [5]
test set: [6]
TRAIN subset: [0 1 2 3 4 5]
Validation set: [6]
test set: [7]
TRAIN subset: [0 1 2 3 4 5 6]
Validation set: [7]
test set: [8]
TRAIN subset: [0 1 2 3 4 5 6 7]
Validation set: [8]
test set: [9]
```

```
TRAIN subset: [ 0  1  2  3  4  5  6  7  8  9 10 11 12 13 14 15 16 17 18 19 20 21 22 23
24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47
48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71
72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95]
Validation set: [96]
test set: [97]
TRAIN subset: [ 0  1  2  3  4  5  6  7  8  9 10 11 12 13 14 15 16 17 18 19 20 21 22 23
24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47
48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71
72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95
96]
Validation set: [97]
test set: [98]
Model performance : 0.6953183352916578
```


In [60]:

```
model=ElasticNet()  
tscv=TimeSeriesSplit(n_splits=95)
```

In [9]:

```
model_performance_mae=[]  
for train_index, Validation_index in tscv.split(df2):  
    if Validation_index==df2.shape[0]-2:  
        break  
    mae=[]  
    model_set={}  
    print("TRAIN subset:", train_index, "\nValidation set:", Validation_index,  
          df2_train, df2_validation, df2_test = df2.iloc[train_index,:], df2.iloc[Vali  
X_train=df2_train[['Open', 'High', 'Low', 'Volume ETH', 'Volume USD', 'Close']]  
X_train=X_train.iloc[:-1,]  
y_train=df2_train['Close'].shift(periods=-1)  
y_train=y_train.iloc[:-1,]  
  
X_validation=df2_validation[['Open', 'High', 'Low', 'Volume ETH', 'Volume USD'  
y_validation=df2.iloc[Validation_index+1,3]  
X_test=df2_test[['Open', 'High', 'Low', 'Volume ETH', 'Volume USD', 'Close']]  
y_test=df2.iloc[Validation_index+2,3]  
  
for i in np.arange(0.1,10,0.1):  
    model_set[round((i/0.1)-1)]=ElasticNet(alpha=i)  
    mae.append(mean_absolute_error(y_validation, model_set[round((i/0.1)-1)  
idx_least_mae=np.argmin(np.array(mae))  
model_to_fit=model_set[idx_least_mae]  
  
df2_final_train=df2.iloc[:int(Validation_index+1),:]  
X_final_train=df2_final_train[['Open', 'High', 'Low', 'Volume ETH', 'Volume US  
  
X_final_train=X_train.append(X_validation)  
  
y_final_train=y_train.append(y_validation)  
model_to_fit.fit(X_final_train, y_final_train)  
model_performance_mae.append(mean_absolute_error(y_test,  
                                                    model_to_fit.predict(X_te  
  
print(' Model performance : ', np.mean(model_performance_mae))
```

Inner loop,
hyperparameter tuning

```
TRAIN subset: [ 0  1  2  3  4  5  6  7  8  9 10 11 12 13 14 15 16 17 18 19 20 21 22 23  
24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47  
48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71  
72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95]  
Validation set: [96]  
test set: [97]  
TRAIN subset: [ 0  1  2  3  4  5  6  7  8  9 10 11 12 13 14 15 16 17 18 19 20 21 22 23  
24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47  
48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71  
72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95]  
96]  
Validation set: [97]  
test set: [98]  
Model performance : 1.064419068751438
```

Thank you!

- Q&A Time!