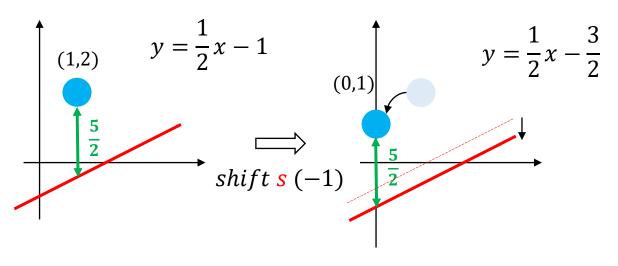


CNN itself is not shift invariant before applying pooling layer



original space

shifted space

$$x = \begin{bmatrix} 1 \\ 2 \end{bmatrix} \qquad W = \begin{bmatrix} -\frac{1}{2} \\ 1 \end{bmatrix} \qquad x' = \begin{bmatrix} 0 \\ 1 \end{bmatrix} \qquad s = \begin{bmatrix} -1 \\ -1 \end{bmatrix} \qquad W = \begin{bmatrix} -\frac{1}{2} \\ 1 \end{bmatrix}$$

$$b = 1 \qquad b' = -sW + b = \frac{3}{2}$$

$$bias \ correction \\ for \ shifting$$

$$xW + b = \frac{5}{2} \qquad x'W + b' = \frac{5}{2}$$

(a) CNN on image data

(b) Flipped GNN