```
In [1]: import matplotlib.pyplot as plt
          import numpy as np
 In [2]: x1 = np.linspace(0,10,1000)
          x2 = np.linspace(0,5,1000)
          x3 = np.linspace(0,3,1000)
          lognormal distribution
 In [3]: def lognormal(mu, sig):
              return (1 / (x1 * sig * ((2 * np.pi) ** 0.5))) * np.exp(-(((np.log(x1) - mu) ** 2) / (2 * (sig ** 2))))
          weibull distribution
 In [4]: def weibull(c,b):
              return (c * (x2 ** (c - 1))) / ((b ** c) * np.exp((x2 / b) ** c))
          wald distribution
 In [5]: def wald(eta,lam):
              return (((lam) / (2 * np.pi * (x3 ** 3))) ** 0.5) * np.exp((-lam) * (((x3 - eta) ** 2)) / (2 * (eta ** 2) * x3))
          plot lognormal distribution
 In [6]: Log11 = lognormal(0,0.25)
          Log12 = lognormal(0,0.5)
          Log13 = lognormal(0,1)
          Log14 = lognormal(0,2)
          Log21 = lognormal(0,0.5)
          Log22 = lognormal(0.5, 0.5)
          Log23 = lognormal(1,0.5)
          Log24 = lognormal(2,0.5)
          /Users/Chokeunhee/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:2: RuntimeWarning: divide by zero encou
          ntered in true_divide
          /Users/Chokeunhee/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:2: RuntimeWarning: divide by zero encou
          ntered in log
          /Users/Chokeunhee/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:2: RuntimeWarning: invalid value encoun
          tered in multiply
 In [7]: plt.figure(1)
          plt.plot(x1,Log11,label=r'$\sigma$ = 0.25')
          plt.plot(x1,Log12,label=r'$\sigma$ = 0.5')
          plt.plot(x1,Log13,label=r'$\sigma$ = 1')
          plt.plot(x1,Log14,label=r'$\sigma$ = 2')
          plt.title('lognormal distribution (mu=0)')
          plt.xlabel('x')
          plt.ylabel('lognormal(x) density')
          plt.legend()
          plt.show()
                          lognormal distribution (mu=0)
                                                     \sigma = 0.25
             1.50
                                                     \sigma = 0.5
                                                     \sigma = 1
           lognormal(x) density
0.75
0.50
                                                     \sigma = 2
             0.25
             0.00
 In [8]: plt.figure(2)
          plt.plot(x1,Log21,label=r'$\mu$ = 0')
          plt.plot(x1,Log22,label=r'$\mu$ = 0.5')
          plt.plot(x1,Log23,label=r'$\mu$ = 1')
          plt.plot(x1,Log24,label=r'$\mu$ = 2')
          plt.title('lognormal distribution (sigma=0.5)')
          plt.xlabel('x')
          plt.ylabel('lognormal(x) density')
          plt.legend()
          plt.show()
                        lognormal distribution (sigma=0.5)
             0.8
                                                     \mu = 0.5
                                                     \mu = 1
           normal(x) density
9.0
9.0
                                                   -\mu = 2
           od
             0.2
          plot weibull distribution
 In [9]: Weil1 = weibull(0.5,1)
          Wei12 = weibull(1,1)
          Wei13 = weibull(1.5,1)
          Wei14 = weibull(5,1)
          Wei21 = weibull(2,0.25)
          Wei22 = weibull(2,0.5)
          Wei23 = weibull(2,1)
          Wei24 = weibull(2,5)
          /Users/Chokeunhee/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:2: RuntimeWarning: divide by zero encou
          ntered in power
In [10]: plt.figure(3)
          plt.plot(x2,Wei11,label=r'c = 0.5')
          plt.plot(x2,Wei12,label=r'c = 1')
          plt.plot(x2,Wei13,label=r'c = 1.5')
          plt.plot(x2,Wei14,label=r'c = 5')
          plt.title('weibull distribution (b=1)')
          plt.xlabel('x')
          plt.ylabel('weibull(x) density')
          plt.legend()
          plt.show()
                          weibull distribution (b=1)
                                                    c = 5
           weibull(x) density
In [11]: plt.figure(4)
          plt.plot(x2,Wei21,label=r'b = 0.25')
          plt.plot(x2,Wei22,label=r'b = 0.5')
          plt.plot(x2,Wei23,label=r'b = 1')
          plt.plot(x2,Wei24,label=r'b = 5')
          plt.title('weibull distribution (c=2)')
          plt.xlabel('x')
          plt.ylabel('weibull(x) density')
          plt.legend()
          plt.show()
                            weibull distribution (c=2)
             3.5
                                                 b = 0.25
                                                   - b = 0.5
             3.0
                                                   - b = 1
           2.5 2.0 2.0 1.5 1.0 1.0
                                                   b = 5
             0.5
          plot wald distribution
In [12]: Wall1 = wald(0.25,1)
          Wal12 = wald(0.5,1)
          Wal13 = wald(1,1)
          Wal14 = wald(2,1)
          Wal21 = wald(1,0.25)
          Wal22 = wald(1,0.5)
          Wal23 = wald(1,1)
          Wal24 = wald(1,5)
          /Users/Chokeunhee/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:2: RuntimeWarning: divide by zero encou
          ntered in true_divide
          /Users/Chokeunhee/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:2: RuntimeWarning: invalid value encoun
          tered in multiply
In [13]: plt.figure(5)
          plt.plot(x3,Wall1,label=r'$\epsilon = 0.25')
          plt.plot(x3, Wal12, label=r'$\eta$ = 0.5')
          plt.plot(x3, Wal13, label=r'$\eta$ = 1')
          plt.plot(x3,Wal14,label=r'$\epsilon = 2')
          plt.title('wald distribution (lambda=1)')
          plt.xlabel('x')
          plt.ylabel('wald(x) density')
          plt.legend()
          plt.show()
                         wald distribution (lambda=1)
                                                 -\eta = 0.25
                                                   \eta = 0.5
                                                 -\eta = 1
                                                  -\eta = 2
           wald(x) density
                             1.0
                                   1.5
                                          2.0
                                                2.5
                                                       3.0
               0.0
                      0.5
In [14]: plt.figure(5)
          plt.plot(x3, Wal21, label=r'$\lambda$ = 0.25')
          plt.plot(x3,Wal22,label=r'$\lambda = 0.5')
          plt.plot(x3, Wal23, label=r'$\lambda$ = 1')
          plt.plot(x3,Wal24,label=r'$\lambda$ = 5')
          plt.title('wald distribution (eta=1)')
          plt.xlabel('x')
          plt.ylabel('wald(x) density')
          plt.legend()
          plt.show()
                            wald distribution (eta=1)
                                                    \lambda = 0.25
                                                    \lambda = 0.5
             2.0
                                                   -\lambda = 1
                                                   -\lambda = 5
           wald(x) density
             0.5
                 0.0
                       0.5
                              1.0
                                    1.5
                                           2.0
                                                 2.5
                                                        3.0
```

In []:

In []:

In []:

Question2