

Notation : population - random variables

(Roman) X, Y, Y_1, X_1, Y_2, X_2

- parameters

(Greek) μ, σ, π

Sample (observations / measurements)

→ sample instances of random variables

x, y, y_1, x_1, y_2, x_2

Data (x_i, y_i) $i=1, 2, 3, \dots$ $n=138$

Summary statistics

sample mean of y = $\frac{y_1 + y_2 + \dots + y_n}{n}$

Notation $\bar{y} = \frac{\sum_{i=1}^n y_i}{n}$ point estimate of μ_Y (population mean)

Sample variance of y

Notation Δ_y^2 or $s_y^2 = \frac{\sum y_i^2}{n-1}$ ← sum of squares
← degrees of freedom

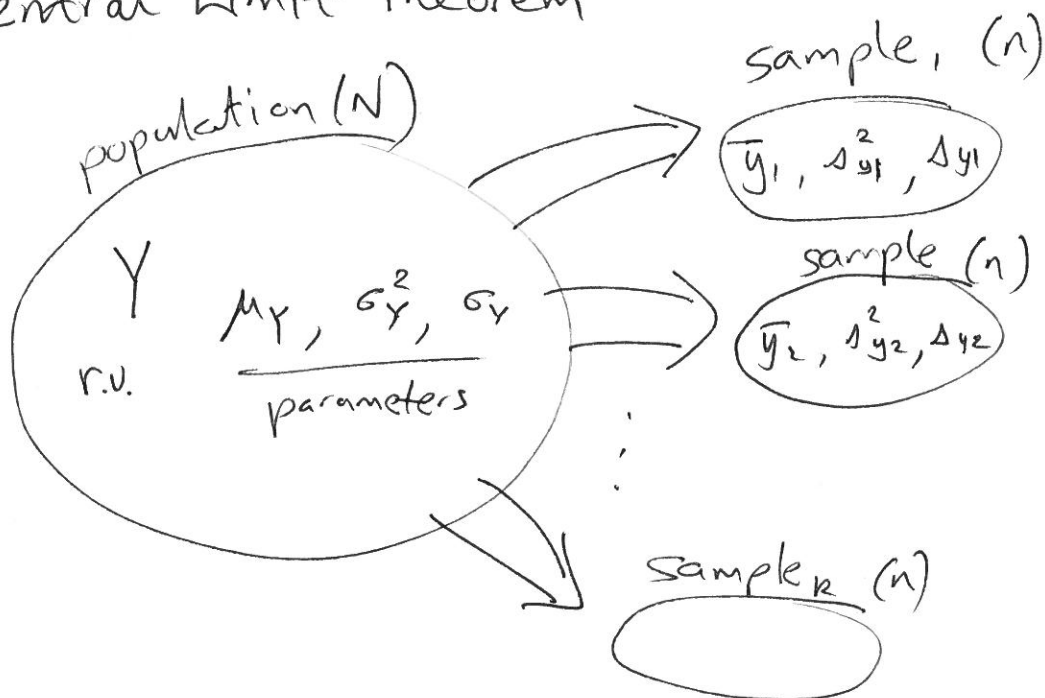
$$= \frac{1}{(n-1)} \sum_{i=1}^n (y_i - \bar{y})^2$$

Unbiased point estimate of σ_Y^2 (population variance)

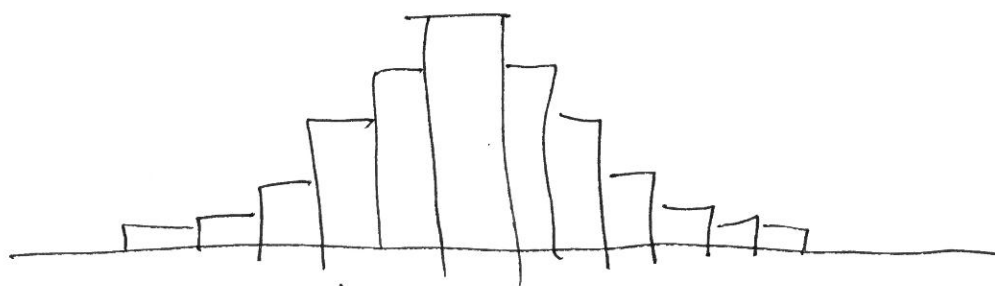
→ we could do the same for x

more often we work with $s_y = \sqrt{\Delta_y^2}$ — in °C
sample standard deviation

Central Limit Theorem



histogram of $\bar{y}_1, \bar{y}_2, \bar{y}_3 \dots$ (sample means under repeated sampling)



sampling distribution of the mean

CLT: if we are sampling from a population with mean μ_Y & variance σ_Y^2 then as $n \rightarrow \infty$ the sampling distribution of the mean will

$$\rightarrow N\left(\mu_Y, \frac{\sigma_Y^2}{n}\right)$$

standard deviation of the sampling distribution is $\frac{\sigma_Y}{\sqrt{n}}$

standard error