

Worth: 2%**Due:** Before 10pm on **Wednesday 15** February 2012.

Remember to write your full name and student number prominently on your submission.

Please read and understand the policy on Collaboration given on the Course Information Sheet. Then, to protect yourself, list on the front of your submission **every** source of information you used to complete this homework (other than your own lecture and tutorial notes, and materials available directly on the course webpage). For example, indicate clearly the **name** of every student with whom you had discussions, the **title** of every additional textbook you consulted, the **source** of every additional web document you used, etc.

For each question, please write up detailed answers carefully. Make sure that you use notation and terminology correctly, and that you explain and justify what you are doing. Marks **will** be deducted for incorrect or ambiguous use of notation and terminology, and for making incorrect, unjustified, ambiguous, or vague claims in your solutions.

1. Let $T(n)$ denote the worst-case running time of the algorithm below on inputs of size n . Write a recurrence relation satisfied by T . Make sure to define n precisely (as a function of the algorithm's parameters) and justify that your recurrence is correct (by referring to the algorithm to describe how you obtained each term in your answer). **Do not write down a closed-form expression for $T(n)$!** Just the recurrence itself.

```

MYSTERY( $A, b, e$ ):
    #  $A$  is a list and  $b, e$  are indices such that  $0 \leq b \leq e + 1 \leq \text{len}(A)$ .
    if  $b > e$ : return 0
     $m \leftarrow \lfloor (e - b + 1) / 4 \rfloor$ 
     $s \leftarrow \text{MYSTERY}(A, b, b + m - 1)$ 
    for  $i \leftarrow b + m$  to  $e - m$ :
         $s \leftarrow s + A[i]$ 
     $s \leftarrow s + \text{MYSTERY}(A, e - m + 1, e)$ 
    return  $s$ 

```

2. Use the method of repeated substitution to find an approximate closed-form expression for $T(n)$ from the previous question. Show your work, *i.e.*, explain what you are doing at each step. **Do not write a formal proof of your answer!**

HINT: Remember that $\forall a, b, c \in \mathbb{R}, a > 1 \wedge b > 1 \wedge c > 1 \Rightarrow a^{\log_b c} = c^{\log_b a}$.