

University of Toronto Mississauga

STA304H5F - Fall 2012

Instructor: Ramya Thinniyam

Term Test #1 - October 11th, 2012

Version 2

Family Name (print): <i>(the name in large print on your T-card)</i>	
Given Names (print): <i>(the names in small print on your T-card)</i>	
Signature:	
Student Number:	
Tutorial (circle one):	Fraturdays 12-1pm Fraturdays 2-3pm

Aids Allowed: Non-programmable Calculator (without a text keyboard)

Aids Provided: Formula sheet

INSTRUCTIONS:

- There are 5 questions – answer all questions.
- There are 7 pages total. Make sure you have all pages before starting the test.
- For all true/false and fill in the blank questions, circle or put your final answers in blanks as instructed. Only final answers will be marked.
- For all other questions, show your work to earn full marks and then circle the final answer. Correct answers with no justifications will not receive any marks.
- You may use formulas/results from formula sheet without proof unless you are asked to specifically prove that formula.
- Simplify answers and round to **4 decimal places** where appropriate.
- Recall: **SRS**=Simple Random Sample without replacement
- SRSWR**=Simple Random Sample With Replacement

BEST WISHES! ☺

Question	1. (/5)	2. (/15)	3. (/10)	4. (/10)	5. (/10)	TOTAL:(/50)
Marks						

[5 marks]

1. TRUE/FALSE: If the statement is true under all conditions, circle T ; otherwise circle F.

- (a) A careful survey design will reduce sampling error. T F
- (b) Sample estimates are often more accurate than those based on a census. T F
- (c) A 95% CI for the population proportion yields [0.78,1.00]. There is only a 5% chance that the true proportion is below 0.78. T F
- (d) A bank asks this on their survey: "How high would you rate our customer service?"
This is an example of a double-barreled question. T F
- (e) Probability sampling does not guarantee representative samples. T F

[15 marks]

2. . A survey is conducted to determine if test marks in STA304 is associated with major. There are 80 students in the class - 50 Statistics majors and 30 from other majors. Suppose that 30 Statistics majors and 20 majors from other disciplines attend the STA304 study group this week. The investigator attends this study group meeting and randomly selects 3 of the Statistics majors and then chooses at random 2 of the other majors and asks the selected 5 students to report their test mark.

a) The investigator has given every student the same chance of being selected (10% chance) so this is a Simple Random Sample. TRUE/FALSE?

If true, write 'TRUE' and find $P(S)$ and π_i . If false, write 'FALSE' and explain why the above does not meet the conditions of a SRS by showing the necessary calculations.

b) Identify the following for this survey:

Target Population -

Sampling Frame -

Observation Unit -

Sample -

c) Briefly discuss 2 sources of non-sampling error in this survey. Use the correct statistical terminology and explain them in plain English.

d) Explain sampling error in this survey.

e) Briefly explain how the survey design could be improved to obtain more accurate results in order to answer the question of interest. [ie. how you would reduce non-sampling errors]

[10 marks]

3. Fill in the blanks: *You may do rough work on the back of the pages or in empty space, but only answers filled in the blanks will be marked.*

We are interested in taking a SRS from the population of all golf courses in Toronto and estimating the mean course rating. Below is some 'R' output:

```
>golfddata <- read.csv("golfsrs.csv")
>golfpopulationratings <- golfddata$rating
> length(golfpopulationratings)

[1] 120
> mean(golfpopulationratings)

[1] 70.27187
> var(golfpopulationratings)

[1] 5.851095
>golfsample1<-sample(golfpopulationratings,25,replace=T)
> [1] 71.6 67.3 67.4 67.4 73.2 69.4 73.4 67.9 66.0 70.5 70.9 70.0 70.0
[14] 71.1 67.3 70.1 73.2 71.2 71.6 65.9 67.3 71.9 69.8 69.9 71.9
> units <- sample(1:120,25,replace=F)
> units

[1] 17 28 60 57 66 89 25 47 104 44 108 107 109 82 27 71 97 91 68 101 87 99 96 118 55
> golfsample2 <- golfpopulationratings[units]
[1] 67.6 72.0 67.4 67.9 71.2 69.4 73.4 67.9 66.0 72.5 70.9 70.2 70.0
[14] 71.1 67.3 70.1 72.5 70.7 71.6 73.2 67.3 65.9 69.8 69.9 71.9
> mean(golfsample1)

[1] 69.848
> var(golfsample1)

[1] 5.0226
> mean(golfsample2)

[1] 69.908
> var(golfsample2)

[1] 4.8916
```

- (a) The population size is _____ and the sample size is _____.
- (b) The 17th selected rating measurement for the sample is _____ which corresponds to the _____ unit in the population.
- (c) The population mean is _____.
- (d) The expected value of the sample mean is _____ with estimated variance _____.
- (e) The expected value of the sample variance is _____.
- (f) An approximate 99% CI for the population mean rating is [_____ , _____].
- (assume the sample size is large enough and that you do not know any of the population parameters even if they are given in the output.)

[10 marks]

4. We wish to take a sample of 2 from a population of size 8. Assume the sampling units equal the elements. **Show your work and then circle the final answer** for the following questions:

a) If we take a SRSWR, what is the probability that both i and j are selected in the sample?

b) In a SRS, what is the probability that both i and j are selected in the sample?

c) For a SRS, how many different samples contain the i th population unit?

d) In a SRS, what is the probability that units i, j , and k are included in the sample?

[10 marks]

5. A library suspects that the percentage of patrons with overdue books has increased to at least 30%. They plan to take a SRS from their 580 current patrons and record whether or not the person had at least one overdue book this year.

a) At minimum, how many patrons should be sampled to estimate the percentage of interest within 5% of the true value using 99% confidence? **Show your work and circle the final answer.**

b) Now suppose the library takes a SRS of 120 patrons from their library, of which 93 had no overdue books.

Find a 99% CI to answer the question of interest and comment on the library's suspicion.

Show your work and circle your final answer.

c) Prove that for binary data like this, s^2 is unbiased for S^2 . **Show your work and justify steps.**

Hint: Look at formulas for $E(\hat{p})$ and $V(\hat{p})$ and recall that in this case, $s^2 = \frac{n}{n-1} \hat{p} (1 - \hat{p})$.
(You may use the above s^2 formula without proof).