

**RESEARCH SCHOOL OF FINANCE, ACTUARIAL STUDIES AND APPLIED
STATISTICS**

Second Semester Mid-Semester Exam 2013

Survival Models / Biostatistics

(STAT3032/7042/8003)

Writing period: 1 Hour duration

Permitted materials: Calculators, lecture notes, dictionary

You must attempt to answer all questions.

All questions are to be completed in the script book provided.

Question 1 (5 marks)

Given that $l_x = (1 - x/100)^{1/2}$, compute the force of mortality at age 50 years.

$$\begin{aligned}\mu_x &= -\frac{1}{l_x} \frac{dl_x}{dx} \\ &= \frac{1}{\sqrt{1-x/100}} \frac{1}{2} \frac{1}{\sqrt{1-x/100}} \frac{1}{100} \\ &= \frac{1}{200} \frac{1}{1-\frac{x}{100}} \\ \mu_{50} &= \frac{1}{200} \frac{1}{1-\frac{50}{100}} = 1/100\end{aligned}$$

Question 2 (2+2+2+2+2=10 marks)

(For each part, you will gain 2 marks for a correct answer, be penalized 2 marks for an incorrect answer, and score 0 if no answer is given.)

Answer each question “TRUE” or “FALSE”. In each case, write the whole word. It is **not** acceptable to write only “T” or “F” and answers presented in this form **will be graded incorrect**.

- a) ${}_5p_{34}$ must be less than or equal to ${}_7p_{33}$.
FALSE
- b) Parameter estimates obtained using method of moments estimation will be the same as those obtained from maximum likelihood estimation.
FALSE
- c) For human populations a force of mortality function (μ_x) for which $\lim_{x \rightarrow \infty} \int_0^x \mu_s ds \neq \infty$ is plausible.
FALSE
- d) $e_x = p_x(1 + e_{x+1})$.
TRUE
- e) The coefficient estimate for a particular covariate in a fitted Cox proportional hazards regression model is -0.5. This means that, everything else constant, it is estimated that a one unit increase in the particular covariate results in the hazard decreasing by more than 50%.
FALSE

Question 3 (5+5=10 marks)

The results of a clinical trial to study the time to relapse for a group of cancer patients given a new treatment are shown below. The times denoted with a * represent censored observations.

6, 6, 6, 6, 7*, 9, 10*, 10*, 16, 16, 17*, 19*, 20*, 22

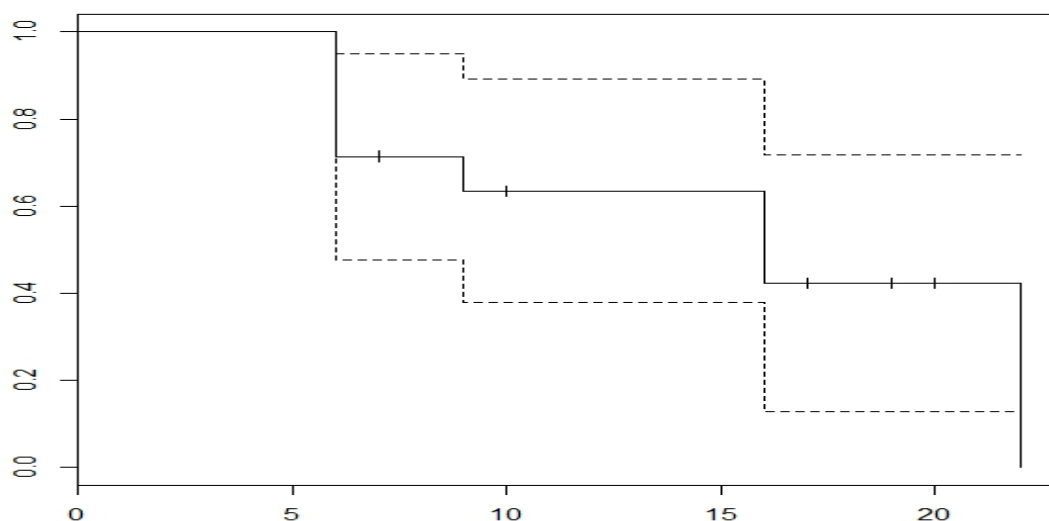
- a) Compute the Kaplan-Meier estimate of the survival function for relapse times less than 12. You should also provide standard errors for your estimated function.

```
> summary(km.est)
```

```
Call: survfit(formula = Surv(times, ind) ~ 1, conf.type = "plain")
```

| time | n.risk | n.event | survival | std.err | lower 95% CI | upper 95% CI |
|------|--------|---------|----------|---------|--------------|--------------|
| 6 | 14 | 4 | 0.714 | 0.121 | 0.478 | 0.951 |
| 9 | 9 | 1 | 0.635 | 0.131 | 0.378 | 0.891 |
| 16 | 6 | 2 | 0.423 | 0.150 | 0.129 | 0.718 |
| 22 | 1 | 1 | 0.000 | NaN | NaN | NaN |

- b) Provide an estimate of the mean time to relapse for cancer patients.



Expected value can be estimated as area under the survival curve. The area is approximately: 15.

Question 4 (5 marks)

The following force of mortality is assumed to hold for an individual aged x :

$$\mu_x = \frac{1}{100-x}, \quad 0 \leq x < 100$$

Assuming this force of mortality holds, calculate $S(50)$ the probability that an individual aged 0 survives to age 50.

$$\begin{aligned} S(x) &= \exp\left\{-\int_0^x (\mu - t)^{-1} dt\right\} \\ &= \exp\{-[-\log(100-t)]_0^x\} \\ &= \exp\{-[-\log(100-x) + \log(100)]\} \\ &= \exp\{\log(100-x) - \log(100)\} \\ &= \frac{100-x}{100} = 1 - \frac{x}{100} \\ S(50) &= 1/2. \end{aligned}$$

End of Examination
