#### APM 236H1F term test 2

10 November, 2010

FAMILY NAME		 	
GIVEN NAME(S)			
STUDENT NUMBER			
SIGNATURE	 		

### Instructions: No calculators or other aids allowed.

This test has 3 questions whose values are given immediately after the question numbers. Total marks = 40.

Write solutions in the spaces provided, using the backs of the pages if necessary. (Suggestion: If you have to continue a question, you may use the back of the **previous** page.) Aspects of any question which are indicated in **boldface** will be regarded as crucial during grading. Show your work.

The duration of this test is 50 minutes.

$\begin{array}{cccccccccccccccccccccccccccccccccccc$
$4x_1 + x_2 + 2x_3 \ge 7$ , $x_1 \ge 0$ , $x_2 \ge 0$ , $x_3 \ge 0$ . (a) (2 marks) Put the problem in <b>canonical form</b> .
(b) (7 marks) Find all basic solutions (feasible and infeasible) of the canonical form
of the problem.
(c) (2 marks) Find all extreme points of the feasible region of the problem given above.
Note that the above problem has 3 decision variables. (d) (2 marks) Solve the problem given above.
a) Marcinize $Z = -x_1 - x_2 - x_3$ s.t.
t X3
$4x_1 + x_0 + 2x_3 - x_4 = 7$
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have coefficient matrix [3, 0, 1, 2, -1].
have coefficient motion 13 0 1 0 1.
4 1 2 -1
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seto, so the problem in (a) has only 4 basic solutions:
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(C) Owiarding the infeaseble basis solutions.
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the extreme points are [ ] = [ ] and [ ] .
(d) The respective objective values are 4 and 5.  [3] is the gotimal solution.
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1. (13 marks) Consider the following linear programming problem. Minimize  $z=x_1+x_2+x_3$  subject to the constraints

2. (13 marks) Solve the problem: Maximize  $z=-x_1+2x_2+3x_3$  subject to the constraints  $2x_1-x_2+x_3 \leq 5$   $-x_1+2x_2+x_3 \leq 2$ ,  $x_1\geq 0, x_2\geq 0, x_3\geq 0$ .  $2x_1+x_2+2x_3\leq 12$ 

### Tellery (D)

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## Tableau 2

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# Tableau 3

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 $2x_{3}$ phase 1, Tableau 1 phase 1, Tableau (2) phase 1, tableau 3 phase 2 Tableau ( phase 2 Tableau (2) Page 4 of 4 aptimal

3. (14 marks) Solve the problem: Maximize  $z = 3x_1 + x_2 + 2x_3$  subject to the constraints