

**Table 2.1** Summary of Group Examples ( $F$  can be any of  $\mathbb{Q}$ ,  $\mathbb{R}$ ,  $\mathbb{C}$ , or  $\mathbb{Z}_p$ ;  $L$  is a reflection)

Group	Operation	Identity	Form of Element	Inverse	Abelian
$\mathbb{Z}$	Addition	0	$k$	$-k$	Yes
$\mathbb{Q}^+$	Multiplication	1	$m/n$ , $m, n > 0$	$n/m$	Yes
$\mathbb{Z}_n$	Addition mod $n$	0	$k$	$n - k$	Yes
$\mathbb{R}^*$	Multiplication	1	$x$	$1/x$	Yes
$GL(2, F)$	Matrix multiplication	$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$	$\begin{bmatrix} a & b \\ c & d \end{bmatrix}$ $ad - bc \neq 0$	$\begin{bmatrix} \frac{d}{ad - bc} & \frac{-b}{ad - bc} \\ \frac{-c}{ad - bc} & \frac{a}{ad - bc} \end{bmatrix}$	No
$U(n)$	Multiplication mod $n$	1	$k$ , $\gcd(k, n) = 1$	Solution to $kx \bmod n = 1$	Yes
$\mathbb{R}^n$	Componentwise addition	$(0, 0, \dots, 0)$	$(a_1, a_2, \dots, a_n)$	$(-a_1, -a_2, \dots, -a_n)$	Yes
$SL(2, F)$	Matrix multiplication	$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$	$\begin{bmatrix} a & b \\ c & d \end{bmatrix}$ $ad - bc = 1$	$\begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$	No
$D_n$	Composition	$R_0$	$R_\alpha, L$	$R_{360 - \alpha}, L$	No