

Paul Kergin SS A1071 Tel: 4169783361

APM236H1F Applications of Linear Programming

<http://www.math.toronto.edu/cms/courses-2/>

Office hours: Mondays: 1:10 pm - 2:00 pm

Fridays: 1:10 pm - 2:00 pm

Marking scheme: Term 1 (20%) + Term 2 (20%) + Final(60%). No tutorials

a quick review of linear algebra chp. 0

convex analysis and basic solutions chp. 1

the simplex method chp. 2. omitting "big M method", pages 147-150

Duality chp. 3, omitting "Now let us consider...", to page 201 inclusive, 3.6 and 3.7.

First week on linear programming problems

See Kolman and Beck section 1.3 for elementary solution methods ("graphical methods")

See page 51 for the definition of a general linear programming problem.

These are problems that may be stated

"Find x_1, \dots, x_n

which maximizes (or minimizes) $z = c_1 x_1 + \dots + c_n x_n$

subject to the constraints $a_{11} x_1 + \dots + a_{1n} x_n \leq b_1$

\vdots

$a_{m1} x_1 + \dots + a_{mn} x_n \leq b_n$ "

The linear function of $x_1, \dots, x_n : z = c_1 x_1 + \dots + c_n x_n$ is the objective function (all linear programming have one)

x_1, \dots, x_n are the decision variables of the problem.

The coefficients c_1, \dots, c_n and a_{ij} ($i = 1, \dots, m; j = 1, \dots, n$) are given data, as well as b_1, \dots, b_n .

To solve a problem means either

1. Find x_1, \dots, x_n which maximizes (or minimizes) the objective function while satisfying all the constraints, and verify that your x_1, \dots, x_n actually does maximizes (or minimizes) z . In case of a "maximize" problem, this means $c_1 x_1 + \dots + c_n x_n \geq c_1 u_1 + \dots + c_n u_n$, when u_1, \dots, u_n are any values of the decision variables which also satisfy the constraints.

2. Verify that there is no x_1, \dots, x_n which maximizes z subject to the constraints.

The solution set of the constraints

$$a_{11}x_1 + \dots + a_{1n}x_n \leq b_1$$

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$$a_{m1}x_1 + \dots + a_{mn}x_n \leq b_m$$

is called the feasible region of the problem. The feasible x_1, \dots, x_n that maximizes (or minimizes) z (if there is such an x_1, \dots, x_n) is called an optimal solution of the problem. The points in the feasible region are called feasible solutions.