

# Complexity

## Recap

- The run-time of code is usually greater when operating on a larger input.
- There can be massive differences in run-time between different algorithms, even for the same problem.
- Knowing the shape of the run-time growth curve is very valuable.
  - “Can I wait long enough to get the answer for this input?”
  - “Is it even worth writing this code?”

## Ways to determine run-time

- Run the code and measure run-time.  
Run it for different input sizes to determine the growth curve.
- Estimate run-time “on paper.”  
Why would you want to do that?

## *Estimating* run-time

- Benefits of estimating on paper:
  - Can pick among alternative algorithms without having to code them all!
  - Can decide if the one we pick is even worth coding up.
- If all we want to know is the shape of the growth curve, a back-of-the-envelope estimate is fine.

- Technique: pick a representative operation, and calculate how many times it will occur.
- What makes an operation “representative”?
- Let’s try analyzing some example functions.

## General strategy

- **Two chunks of code in sequence:**  
Add the time they take.
- **Loop:**  
Multiply (the time one iteration takes) times (the number of iterations).
- **If-elif statement:**  
One approach is to determine the worst-case scenario by taking the maximum amount of time of any of the branches.

## Computer Science

- Computer science is about much more than programming. Some themes:
- Recognizing commonalities among many problems and creating a general solution.
- Knowing general strategies and recognizing that a problem can be solved using one of them.
- Analyzing and comparing alternative solutions for efficiency -- in time used or space used.