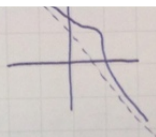


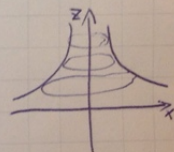
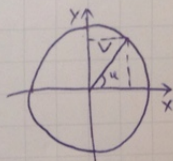
$$y = (1-x^2)^{\frac{1}{p}} \quad y' = \frac{1}{p}(1-x^2)^{\frac{1}{p}-1}(-2x) = -\frac{2x}{p}(1-x^2)^{\frac{1}{p}-1}$$

$$(a) \nabla F = (P_x^{p-1}, P_y^{p-1}) = 0 \Leftrightarrow \text{at } (0,0).$$

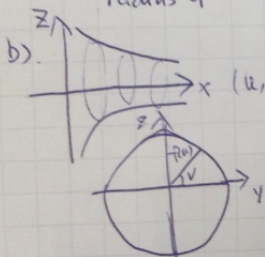


July 11.
P32/#3. $(u,v) \rightarrow (f_1(u,v), f_2(u,v), f_3(u,v)).$

a). $(u,v) \rightarrow (v \cos u, v \sin u, f(u)).$
radius of a cross section. u is angle.



b). $(u,v) \rightarrow (u, f(u) \cos v, f(u) \sin v).$



$$\begin{cases} a_1 x + a_2 y + a_3 z = c \\ b_1 x + b_2 y + b_3 z = d \end{cases}$$

$$(a_1, a_2, a_3) \times (b_1, b_2, b_3) \neq (0, 0, 0)$$

P33/4b).

$$a) \det(Df(u)) \neq 0 \quad \forall u \in U.$$

$$(r, \theta) \quad r > 0$$

$$\rightarrow (r \cos \theta, r \sin \theta)$$

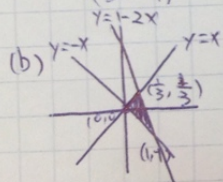
$$\det \begin{pmatrix} \cos \theta & -r \sin \theta \\ \sin \theta & r \cos \theta \end{pmatrix} = r > 0.$$

$$(u,v) = f(x,y) = (x-2y, 2x-y).$$

a) f^{-1}

b). Find image in uv -plane of triangle bounded by $y=x$, $y=-x$, $y=1-2x$
c). Find region in xy plane that is mapped to the triangle with vertices $(0,0)$, $(-1,2)$, $(2,1)$.

$$(a) \det \begin{pmatrix} 1 & -2 \\ 2 & -1 \end{pmatrix} = 3. \quad \frac{1}{3} \begin{pmatrix} -1 & 2 \\ -2 & 1 \end{pmatrix} \begin{pmatrix} u \\ v \end{pmatrix} = \begin{pmatrix} -\frac{1}{3}u + \frac{2}{3}v \\ -\frac{2}{3}u + \frac{1}{3}v \end{pmatrix}$$



$$f(0,0) = (0,0)$$

$$f(-1,2) = (-\frac{1}{3}, \frac{2}{3})$$

$$f(2,1) = (\frac{2}{3}, -\frac{1}{3})$$

$$f(0,0) = (0,0)$$