

$$\begin{aligned}
In[*] &:= Q[bj\_ , bh\_ ] := \sqrt{E^{2*bj} * Cosh[bh]^2 - 2 Sinh[2 bj]} ; \\
lp[bj\_ , bh\_ ] &:= E^{bj} Cosh[bh] + Q[bj, bh] ; \\
&\quad \text{гиперболический косинус} \\
lm[bj\_ , bh\_ ] &:= E^{bj} Cosh[bh] - Q[bj, bh] ; \\
&\quad \text{гиперболический косинус} \\
Zobc[bj\_ , bh\_ , n\_ ] &:= lp[bj, bh]^{(n-1)} * \left( \frac{E^{bj} Sinh[bh]^2}{Q[bj, bh]} + \frac{1}{E^{bj} Q[bj, bh]} + Cosh[bh] \right) - \\
&\quad lm[bj, bh]^{(n-1)} * \left( \frac{E^{bj} Sinh[bh]^2}{Q[bj, bh]} + \frac{1}{E^{bj} Q[bj, bh]} - Cosh[bh] \right) ; \\
&\quad \text{гиперболический косинус}
\end{aligned}$$

$$Zpbc[bj\_ , bh\_ , n\_ ] := lp[bj, bh]^n + lm[bj, bh]^n$$

$$In[*] := m2 = \frac{D[Zobc[bj, bh, n], \{bh, 2\}]}{Zobc[bj, bh, n] * n^2} /. \{bh \rightarrow 0, bj \rightarrow 1/2.269\}$$

$$m4 = \frac{D[Zobc[bj, bh, n], \{bh, 4\}]}{Zobc[bj, bh, n] * n^4} /. \{bh \rightarrow 0, bj \rightarrow 1/2.269\}$$

$$\begin{aligned}
Out[*] &:= \left( 0. + 2.00049 \times 0.910259^{-1+n} - 0.000491583 \times 2.1974^{-1+n} + 1.11022 \times 10^{-16} \right. \\
&\quad \left( 0. - 2.19772 \times 0.910259^{-2+n} (-1+n) \right) + 2. \left( 0. + 5.30538 \times 2.1974^{-2+n} (-1+n) \right) \Big) / \\
&\quad \left( (1.11022 \times 10^{-16} \times 0.910259^{-1+n} + 2. \times 2.1974^{-1+n}) n^2 \right)
\end{aligned}$$

$$\begin{aligned}
Out[*] &:= \frac{1}{\left( 1.11022 \times 10^{-16} \times 0.910259^{-1+n} + 2. \times 2.1974^{-1+n} \right) n^4} \\
&\quad \left( 0. - 131.932 \times 0.910259^{-1+n} + 133.932 \times 2.1974^{-1+n} + \right. \\
&\quad \left. 12.0029 \left( 0. - 2.19772 \times 0.910259^{-2+n} (-1+n) \right) - \right. \\
&\quad \left. 0.0029495 \left( 0. + 5.30538 \times 2.1974^{-2+n} (-1+n) \right) + 1.11022 \times 10^{-16} \right. \\
&\quad \left( 0. + 52.1539 \times 0.910259^{-2+n} (-1+n) + 14.4899 \times 0.910259^{-3+n} (-2+n) (-1+n) \right) + \\
&\quad \left. 2. \left( 0. - 49.0463 \times 2.1974^{-2+n} (-1+n) + 84.4411 \times 2.1974^{-3+n} (-2+n) (-1+n) \right) \right)
\end{aligned}$$

$$In[*] := N\left[1 - \frac{m4}{3 * m2^2} /. \{n \rightarrow 50\}\right]$$

численное приближение

$$Out[*] = 0.0448609$$

$$In[*] := N\left[1 - \frac{m4}{3 * m2^2} /. \{n \rightarrow 100\}\right]$$

численное приближение

$$Out[*] = 0.0226025$$

$$In[*] := N\left[1 - \frac{m4}{3 * m2^2} /. \{n \rightarrow 200\}\right]$$

численное приближение

$$Out[*] = 0.0113421$$

$$In[*] := N\left[1 - \frac{m4}{3 * m2^2} /. \{n \rightarrow 400\}\right]$$

численное приближение

$$Out[*] = 0.00568103$$

In[ ]:= m4

Out[ ]:= 
$$\begin{aligned} & 0. - 131.932 \times 0.910259^{-1+n} + 133.932 \times 2.1974^{-1+n} + \\ & 12.0029 \left( 0. - 2.19772 \times 0.910259^{-2+n} (-1+n) \right) - \\ & 0.0029495 \left( 0. + 5.30538 \times 2.1974^{-2+n} (-1+n) \right) + 1.11022 \times 10^{-16} \\ & \left( 0. + 52.1539 \times 0.910259^{-2+n} (-1+n) + 14.4899 \times 0.910259^{-3+n} (-2+n) (-1+n) \right) + \\ & 2. \left( 0. - 49.0463 \times 2.1974^{-2+n} (-1+n) + 84.4411 \times 2.1974^{-3+n} (-2+n) (-1+n) \right) \end{aligned}$$

In[ ]:= m2 = 
$$\frac{D[Zpbc[bj, bh, n], \{bh, 2\}]}{Zobc[bj, bh, n] * n^2} /. \{bh \rightarrow 0, bj \rightarrow 1/2.269\}$$

m4 = 
$$\frac{D[Zpbc[bj, bh, n], \{bh, 4\}]}{Zobc[bj, bh, n] * n^4} /. \{bh \rightarrow 0, bj \rightarrow 1/2.269\}$$

Out[ ]:= 
$$\frac{0. - 2.19772 \times 0.910259^{-1+n} n + 5.30538 \times 2.1974^{-1+n} n}{\left( 1.11022 \times 10^{-16} \times 0.910259^{-1+n} + 2. \times 2.1974^{-1+n} \right) n^2}$$

Out[ ]:= 
$$\begin{aligned} & \left( 0. + 52.1539 \times 0.910259^{-1+n} n - 49.0463 \times 2.1974^{-1+n} n + \right. \\ & \left. 14.4899 \times 0.910259^{-2+n} (-1+n) n + 84.4411 \times 2.1974^{-2+n} (-1+n) n \right) / \\ & \left( \left( 1.11022 \times 10^{-16} \times 0.910259^{-1+n} + 2. \times 2.1974^{-1+n} \right) n^4 \right) \end{aligned}$$

In[ ]:= N[1 - 
$$\frac{m4}{3 m2^2} /. \{n \rightarrow 50\}$$
 ]  
 численный приближение

Out[ ]:= 0.131271

In[ ]:= N[1 - 
$$\frac{m4}{3 m2^2} /. \{n \rightarrow 100\}$$
 ]  
 численный приближение

Out[ ]:= 0.110552

In[ ]:= N[1 - 
$$\frac{m4}{3 m2^2} /. \{n \rightarrow 200\}$$
 ]  
 численный приближение

Out[ ]:= 0.100193

In[ ]:= N[1 - 
$$\frac{m4}{3 m2^2} /. \{n \rightarrow 400\}$$
 ]  
 численный приближение

Out[ ]:= 0.0950134

In[ ]:= **ListPlot**[**Table**[ $1 - \frac{m^4}{3 * m^2}$ , {n, 10, 10 000, 1}], **PlotRange** → **Full**]

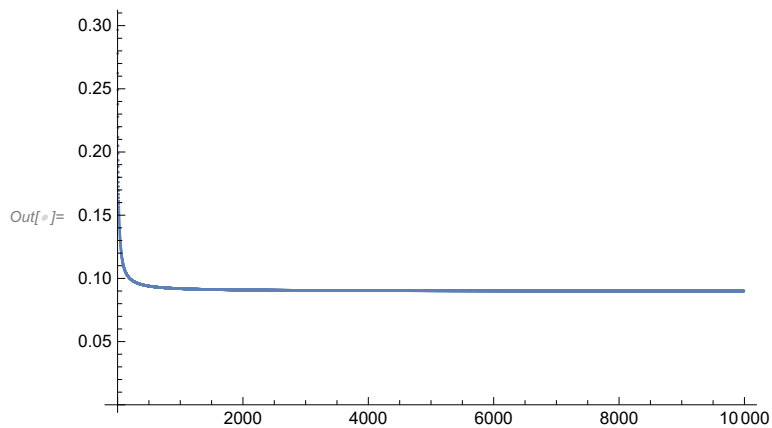
[\[диаграмм...\]](#) [\[таблица значений...\]](#) [\[отображаем...\]](#) [\[в полно...](#)

General:  $\frac{8.85956 \times 10^{-297}}{562434001936}$  is too small to represent as a normalized machine number; precision may be lost.

General:  $\frac{4.03184 \times 10^{-297}}{565036352721}$  is too small to represent as a normalized machine number; precision may be lost.

General:  $\frac{1.83482 \times 10^{-297}}{567647723776}$  is too small to represent as a normalized machine number; precision may be lost.

General: Further output of General::munfl will be suppressed during this calculation.



In[ ]:= **n = 10 000 000**

$$1 - \frac{m^4}{3 * m^2}$$

Out[ ]:= 10 000 000

General: 0.910259<sup>9999999</sup> is too small to represent as a normalized machine number; precision may be lost.

General: 0.910259<sup>9999999</sup> is too small to represent as a normalized machine number; precision may be lost.

General: 0.910259<sup>9999998</sup> is too small to represent as a normalized machine number; precision may be lost.

General: Further output of General::munfl will be suppressed during this calculation.

Out[ ]:= 0.089834055692997