# **Stock Assessment Using Tuned VPA**

Rob Scott

<rbs/>crobert.scott@jrc.ec.europa.eu>

&

Clara Ulrich

<clu@aqua.dtu.dk>

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# **Table of Contents**

1 Introduction	?
2 Section	
2.1 subsection	••••
3 Final thoughs	∠

[1] "diagnostics"

#### 1 Introduction

#### 1.1 What is VPA

Virtual population analysis (VPA) is a modeling technique commonly used in fisheries science for reconstructing the historical population structure of a fish stock using information on the deaths of individuals in each time step. The time steps are typically, though not necessarily, annual and the deaths are usually partitioned into mortality due to fishing and natural mortality. In some instances natural mortality may be further partitioned into predation mortality and mortality from other causes, such as disease, senesence etc.

VPA is the most commonly used term to refer to cohort reconstruction techniques used in fisheries. It is virtual in the sense that the population size is not observed or measured directly but is inferred or back-calculated to have been a certain size in the past. Several different software implementations of cohort reconstruction for fish populations exist including ADAPT which is often used in Canada and the USA and XSA and ICA which are commonly used in Europe. The back-calculations in these implementations work the same way but they differ in the statistical methods used for "tuning" to indices of population size.

Tuning refers to the use of auxilliary information to determine the terminal fishing mortalities and population numbers. Most tuning approaches involve a regression of fishing mortality against fishing effort to estimate population abundance at age through an iterative convergence to some threshold criterion. Relatively simple techniques, the Laurec-Shepherd method (1983) for example, have been shown to work well with simulated data but there is little theoretical work to justify or validate these approaches (Quinn and Deriso 1999).

A number of assessment methods are made available in <u>FLR</u> as well as the basic VPA tools to enable you to develop your own assessment methods. In this tutorial we will cover the basic VPA tools, simple methods for tuning a VPA and finally show how to run <u>FLXSA</u>. Separable VPA and the implementation of ICA (Integrated Catch at age Analysis) are covered in a separate tutorial.

#### 1.2 Stock assessment methods within the FLR package structure

The package **FLAssess** contains the basic class for age-based stock assessment. It provides a standard class, **FLAssess**, for data input, stock status estimation and diagnostic inspection. The **FLAssess** package has a variety of uses. It can be applied within a stock assessment working group setting or, alternatively, as part of the management procedure in a formal Management Strategy Evaluation (MSE).

FLAssess provides a common interface for existing stock assessment methods (e.g. XSA, ICA, Adapt) allowing methods to be used interchangeably. It also includes various methods of general use such as setting

up a short-term forecast (stf), running VPAs (vpa, sepVPA or cohortAnalysis) and calculating F from catches. There are several steps to be completed when conducting an assessment. This tutorial considers only the process of running the stock assessment model. Additional tutorials are available for reading your data into <u>FLR</u>; analysing and checking your data prior to assessment fitting and for producing graphical output.

We will start by loading the <u>FLR</u> libraries <u>FLCore</u>, <u>FLAssess</u> and <u>FLXSA</u> and by importing the data sets for our North Sea Plaice stock and the fishery independent tuning indices that we will use for tuning the assessment. We will use these example data sets for all of the examples in this tutorial.

```
> library(FLCore)
> library(FLAssess)
> library(FLXSA)
> data(ple4)
> data(ple4.indices)
```

Our North Sea Plaice FLStock object already has values estimated for harvest and stock numbers. We should remove these first and replace them with NA.

```
> harvest(ple4)[] <- NA
> stock.n(ple4)[] <- NA</pre>
```

We should note at this point that the example below should not be considered the definitive assessment for North Sea Plaice. We provide this example merely to show the procedure for conducting assessments using FLR.

#### 2 The VPA method

The VPA method implements Pope's Virtual Population Analysis (VPA). It is called with the command VPA() which returns an object of class FLVPA that is itself an extension of the FLAssess class.

The VPA method estimates population numbers and fishing mortalities at age by back-calculating values down each cohort. To do this, the method requires initial values of harvest for the terminal age and terminal year in the FLStock object. These terminal values must be specified by the user prior to running the VPA. The arguments to the VPA method are the FLStock object for which values are to be calculated and two optional arguments, see table below.

The range method will show details of the age and year range of the ple4 FLStock object. We can use this information to manually specify the terminal values in the harvest slot. In this instance we will set these values to 1.0. Remember to convert the values to be of type character when indexing the FLQuants.

```
> harvest(ple4)[ac(range(ple4)["max"]), ] <- 1</pre>
> harvest(ple4)[, ac(range(ple4)["maxyear"])] <- 1</pre>
> ple4.vpa <- VPA(ple4, fratio = 1, fit.plusgroup = T)
> stock.n(ple4.vpa)[, ac(2002:range(ple4)["maxyear"])]
An object of class "FLQuant"
, , unit = unique, season = all, area = unique
    year
age 2002
                                                                 2008
               2003
                         2004
                                   2005
                                             2006
                                                       2007
               477260.9 1026381.9
  1
    1561386.4
                                   617107.6 651356.8
                                                       562832.6
                                                                 223891.7
                                                                 434637.0
     426627.8 1117664.8 366981.0
                                   707289.2 466784.2 380163.8
      289131.4
               202568.1
                         481341.6 151485.3 316039.3 191802.6
                                                                 132333.9
                         87311.1 226211.3
  4
     128476.9
               132766.6
                                              68925.0 118240.4
                                                                   72891.0
      73093.0
                          55099.3
  5
               57884.0
                                    38136.3 107157.4
                                                         28441.5
                                                                   52364.4
  6
       78822.1
                29600.5
                         22780.7
                                    28841.9 13983.0
                                                         53883.2
                                                                 10250.9
               34799.6
                         11249.7
                                     9605.1
  7
        8110.0
                                             11355.9
                                                          6069.8
                                                                   25778.2
                                               3510.6
  8
        3345.4
               2844.5
                         9990.7
                                     5609.2
                                                          4868.9
                                                                   2972.9
  9
        1397.1
                 1337.4
                           1055.0
                                      4731.0
                                                2602.7
                                                          1059.0
                                                                   1109.7
  10
        2986.3
                 1767.4
                            1382.8
                                      1304.6
                                                2779.7
                                                          2455.4
                                                                    1477.4
units:
       NA
> harvest(ple4.vpa)[, ac(2002:range(ple4)["maxyear"])]
An object of class "FLQuant"
, , unit = unique, season = all, area = unique
    year
    2002
             2003
                    2004
                             2005
                                     2006
                                             2007
                                                     2008
age
    0.23433 0.16275 0.27236 0.17918 0.43846 0.15847 1.00000
    0.64484 0.74242 0.78482 0.70557 0.78940 0.95527 1.00000
    0.67829 0.74160 0.65511 0.68747 0.88315 0.86750 1.00000
    0.69731 0.77946 0.72831 0.64717 0.78517 0.71449 1.00000
    0.80394 0.83253 0.54731 0.90333 0.58748 0.92048 1.00000
    0.71759 0.86745 0.76362 0.83209 0.73452 0.63729 1.00000
    0.94773 1.14796 0.59593 0.90651 0.74687 0.61378 1.00000
    0.81688 0.89180 0.64751 0.66787 1.09844 1.37879 1.00000
    0.80833 0.70880 0.52522 0.67534 0.68483 0.76661 1.00000
  10 0.80833 0.70880 0.52522 0.67534 0.68483 0.76661 1.00000
units: f
```

The estimated population numbers and fishing mortality values at age from the VPA are now available in the returned object. Note that the terminal values for fishing mortality are the user defined values that were specified prior to running the VPA.

# 3 A simple method for tuning a VPA

As noted above the VPA method requires user defined terminal estimates of fishing mortality. This dependency limits the usefulness of the method since it is often the most recent, terminal, estimates that are of most concern to fishery managers. Additional catch at age and effort information, derived either from a sub component of the fishery or from a fishery independent source such as a research survey, can be used to 'tune' the assessment, as described above, and thereby obtain better estimates of fishing mortality and stock numbers in the most recent years. Several so-called *ad hoc* techniques for tuning a VPA have been

developed. A relatively simple technique that has been widely used is the Laurec Shepherd method. This method can be easily implemented in FLR using the basic VPA tools that are provided in the <u>FLAssess</u> package.

The example shown below is a simple implementation that allows for a single tuning fleet. With a little extra effort it could be easily extended to accommodate multiple tuning fleets. The technical details of the method are not explained here.

```
> lsm <- function(stock, index, fratio = 1, fit.plusgroup = T) {</pre>
      harvest(stock)[, ac(range(stock)["maxyear"])] <- 0.5</pre>
+
      diff <- 1
+
      while (diff > 1e-06) {
+
           stock <- stock + VPA(stock, fratio = fratio)</pre>
+
           ages <- range(index)["min"]:range(index)["max"]</pre>
           yrs <- range(index)["minyear"]:range(index)["maxyear"]</pre>
           stk <- trim(stock, year = yrs, age = ages)</pre>
           Cp <- catch.n(index)/catch.n(stk)</pre>
           q <- sweep(Cp * harvest(stk), 2, effort(index), "/")</pre>
           gmq \leftarrow apply(q, 1, function(x) exp(mean(log(x), na.rm = T)))
           mFp <- gmq * c(apply(effort(index), 1, mean))</pre>
          Fr <- mFp * (apply(Cp, 1, mean, na.rm = T))^-1
          Fnew <- c(Fr, rep(Fr[ac(max(ages)), ], 2))</pre>
           diff <- sum(abs(harvest(stock)[, ac(range(stock)["maxyear"])] -</pre>
+
           harvest(stock)[, ac(range(stock)["maxyear"])] <- c(Fnew)</pre>
      }
      res <- VPA(stock, fratio = fratio, fit.plusgroup = fit.plusgroup)
+
      index.res(res) <- FLQuants(q)</pre>
+
      return (res)
```

Our new Laurec-Shepherd function can now be called without having to specify terminal values in the harvest slot. The arguments to the VPA method are also formally declared as arguments to our new function. Note that the function returns an object of class FLVPA that has been created from a call to the VPA method and that the catchability residuals are stored in the index.res slot of the returned object.

```
> harvest(ple4)[] <- NA
> stock.n(ple4)[] <- NA
> ple4.LSvpa <- lsm(ple4, ple4.indices[[1]], fratio = 1, fit.plusgroup = T)</pre>
```

### 4 FLXSA

The Laurec-Shepherd method above is a relatively simple technique for tuning a VPA. In recent years many other, more sophisticated stock assessment methods have been developed. XSA, for example, is a more complex implementation that uses information on individual cohort sizes to estimate survivors at each age in the terminal population. Although the modelling approach is more involved the method requires the same

input of catch numbers at age and indices of catch per unit effort and it retains at its core the basic VPA method. The details of the XSA method are too complex to show here, or to code individually as we have for the Laurec-Shepherd approach. Instead the FLXSA method has been developed as an additional subpackage to **FLAssess**.

FLXSA(stock, indices, control, desc, diag.flag=TRUE)

stock

An object of class FLStock.

indices

An object of class FLIndices that contains one or more indices of catch at age and effort.

control

An object of class FLXSA.control that specifies the model parameters.

desc

An optional character string holding a short description of the data and model diag.flag

Boolean. If true the method will return the full diagnostics for the analysis. If false, only the estimated stock numbers and harvest values will be returned. Defalut setting is True.

A number of such packages have been developed to implement specific stock assessment methods in <u>FLR</u>. These currenly include XSA, ICA and the Gavaris implementation of Adapt as used by ICCAT. These methods have a common calling convention in <u>FLR</u> and require as inputs three specific objects. An FLStock object that contains the catch numbers at age and estimates of natural mortality. An FLIndices object that contains one or more indices of populaton abundance and effort, and a control object that specifies the various parameter values and model settings for the analysis.

## 4.1 The FLXSA control object

The FLXSA.control object contains all of the user defined model settings for running an XSA analysis. It can be created in several different ways. The simplest method is to accept all of the default settings by calling the FLXSA.control function without any extra arguments.

FLXSA.control(x=NULL, tol=1e-09, maxit=30, min.nse=0.3, fse=0.5,		
rage=0, qage=10, shk.n=TRUE, shk.f=TRUE, shk.yrs=5, shk.ages=5,		
window=100, tsrange=20, tspower=3, vpa=FALSE)		
х	An object of class FLXSA. If specified the control object is initialised with the same settings as the XSA analysis stored in the object.	
tol	The convergence tolerance. The model is considered to have converged once the sum of the absolute differences in terminal F values between two successive iterations is less than the specified value.	
maxit	The maximum number of iterations that the model can run	
min.nse	The minimum standard error to be used for inverse variance weghting of the survivors estimates.	
fse	User defined standard error when shrinking the mean F	
rage	The oldest age for which the two parameter model is used for determining catchability at age	
qage	The age after which catchability is no longer estimated. Catchability at older ages will be set to the value of catchability at this age.	
shk.n	Boolean. If TRUE apply shrinkage to the population mean. Applies to the recruiting ages only.	
shk.f	Boolean. If TRUE apply shrinkage to the mean F.	
shk.yrs	The number of years to be used for shrinkage to the mean F.	
shk.ages	The ages over which shrinkage to the mean F should be applied.	
window	The specific year range for which the model should be run.	
tsrange	The number of years to be used in the time series weighting.	
tspower	The power to be used in the time series taper weighting.	
vpa	Boolean. If TRUE, use VPA to calculate historical values of F and population abundance. If FALSE, use cohort approximation.	

Alternatively the default settings can be over-written by specifying values at the point of creation or by overwriting them afterwards.

```
> control <- FLXSA.control()
> control <- FLXSA.control(maxit = 50, fse = 2.5, qage = 9)
> slot(control, "qage") <- as.integer(7)</pre>
```

Note that in the example above, when modifying the control object after creation, it is necessary to coerce the value 7 to type integer. This is because the default type numeric cannot be used in this slot. Such coercion is not necessary when using the FLXSA.control() function as this check is performed internally by the function. You can use the getSlots function to determine the class of object associated with any given slot.

Once the control object has been created, the XSA analysis can be run as a simple one-line command. The FLXSA function returns an object of class FLXSA which extends the FLAssess class. The FLXSA object contains all of the information in the FLAssess class plus additional information specific to the XSA assessment method, such as the survivors estimates and their internal and external standard errors. The control object used for the assessment is also stored in the returned FLXSA object to provide a record of what settings were used for that particular run. All of the settings in the returned control object will remain the same except for the maxit slot that contains the maximum number of iterations for the analysis. This value will be overwritten with the actual number of iterations taken to reach convergence, if indeed the model had converged before the maximum number initially specified.

```
> xsa.control <- FLXSA.control(maxit = 50, fse = 2.5)
> ple4.xsa <- FLXSA(ple4, ple4.indices, xsa.control)
> ple4.xsa.t1 <- FLXSA(ple4, ple4.indices[[1]], xsa.control)</pre>
```

#### 4.2 XSA Results

Appart from the model diagnostics, the FLXSA method returns two important results, namely the estimated values of fishing mortality and population numbers at age. These are returned as FLQuants and are stored in the harvest and stock.n slots, respectively, of the FLXSA object. These estimated values can be very easilly read back into an FLStock object using the + operator. Once the results have been read back into a FLStock object we can look at some of the key information such as SSB, recruitment and mean fishing mortality values. But before concentrating too much on the results of the assessment it is advisable to first investigate some of the model diagnostics.

```
> ple4.new <- ple4 + ple4.xsa
> ple4.ssb <- ssb(ple4.new)
> ple4.rec <- rec(ple4.new)
> ple4.fbar <- fbar(ple4.new)</pre>
```

#### 4.3 XSA Diagnostics

There are many diagnostic checks that one might be interested in conducting to examine the model fit. The first might be to see if the model has reached convergence within the specified number of iterations.

```
> slot(slot(ple4.xsa, "control"), "maxit")
[1] 50
```

Additionally one can check for discrepancies between the internal and external standard errors of the survivors estimates. Very often plots of the catchability residuals are made to inspect for any obvious trends or departures from the assumption of constant catchability over time. Some examples of these plots and details of their creation from FLR objects are provided below but you should also consult the tutorial on lattice plotting and advanced graphics for FLR to see examples of other ways to graphically display your data.

There are several ways to access diagnostic information about your fitted XSA model. The easiest is perhaps to use the diagnostics function, which will replicate the diagnostic output produced by the original VPA suite (developed in the early 1990's). Note that this function merely outputs the results to the screen and no object is created by the method. The function was created to allow the user to cut and paste the information from the console to a report. The output can be quite long, particularly if the assessment comprises a large number of ages and many tuning indices. The standard output can be divided roughly into eight sections each providing different information about the model and the fit. These sections comprise the model dimensions; parameter settings; regression weights; the estimated fishing mortalities and population numbers for the last 10 years; the aggregated survivors estimates; the log catchability residuals for each of the tuning indices and finally the individual survivors estimates for each year-class represented in the terminal year.

In order to make this document more readable we will print out only a few sections of the diagnostic output at a time (this feature is not yet distributed with FLXSA). We can do this by passing a vector of TRUE and FALSE values to the sections argument of the diagnostics method. By default all sections are set to TRUE so that all of the information is output to the screen. In order to reduce the quantity of output further we will run a new XSA for a reduced number of ages and with only one tuning index and will start by outputting only the dimension information and the parameter settings from our diagnostics.

```
> ple4.xsa2 <- FLXSA(trim(ple4, age = 1:4), ple4.indices[[3]],</pre>
+ xsa.control)
> diagnostics(ple4.xsa2, sections = c(T, T, rep(F, 6)))
FLR XSA Diagnostics 2010-12-02 12:45:03
CPUE data from ple4.indices[[3]]
Catch data for 52 years 1957 to 2008. Ages 1 to 4.
 fleet first age last age first year last year alpha beta
1 SNS 1 3 1982
                                    2008 <NA> <NA>
Time series weights:
   Tapered time weighting applied
  Power = 3 over 20 years
Catchability analysis:
    Catchability independent of size for all ages
    Catchability independent of age for ages > 3
Terminal population estimation :
    Survivor estimates shrunk towards the mean F
   of the final 5 years or the 5 oldest ages.
   S.E. of the mean to which the estimates are shrunk = 2.5
   Minimum standard error for population
   estimates derived from each fleet = 0.3
   prior weighting not applied
```

Next we can output the regression weights and the fishing mortalities and population numbers for the last 10 years and also the aggregated survivors estimates.

```
> diagnostics(ple4.xsa2, sections = c(F, F, T, T, T, T, F, F))
Regression weights
    year
      1999 2000 2001 2002 2003 2004 2005 2006 2007 2008
age
 all 0.751 0.82 0.877 0.921 0.954 0.976 0.99 0.997
Fishing mortalities
  year
age 1999 2000 2001 2002 2003 2004 2005 2006 2007 2008
 1 0.157 0.126 0.078 0.177 0.160 0.257 0.180 0.297 0.105 0.188
 2 0.199 0.323 0.783 0.692 0.487 0.766 0.644 0.805 0.491 0.532
 3 0.059 0.109 0.778 0.616 0.862 0.320 0.653 0.729 0.910 0.289
 4 0.059 0.109 0.778 0.616 0.862 0.320 0.653 0.729 0.910 0.289
XSA population number (Thousand)
year
            1
                    2
                           3
 1999 923227 1263858 7080877 1728304
 2000 943622 713736 937084 2344103
 2001 487694 752940 467320 238728
 2002 2016895 408177 311443 140324
 2003 486915 1529127 184816 124328
 2004 1084190 375601 850173 165566
 2005 614183 759001 158039 224799
 2006 903854 463963 360804
                              72453
 2007 825289 607783 187650 100907
 2008 834079 671988 336541 184849
Estimated population abundance at 1st Jan 2009
    age
              2
      1
year
 2009 NA 627021 358724 229377
```

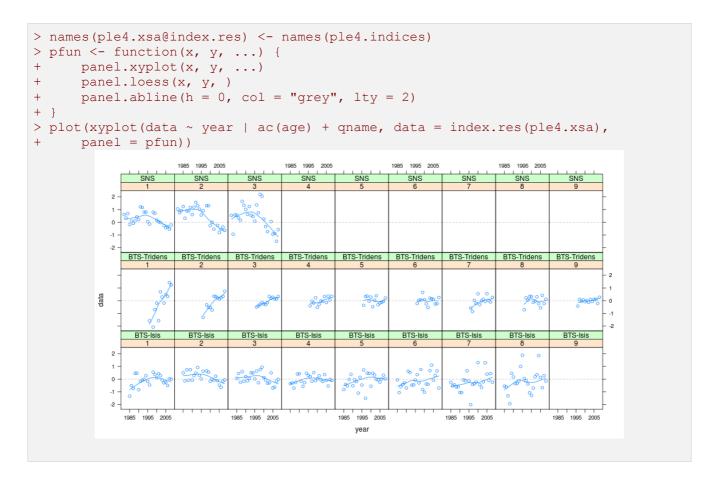
And finally we can output the catchability residuals and the individual survivors estimates. Note that very little thought went into the parameter settings for this particular model fit so please don't interrogate the output presented here too closely. Also note that we do not normally expect the diagnostics output to be broken up as we have here. We present it in this way purely to make it more presentable in this document. By default all sections are set to TRUE so it is very likely that you won't need to give this argument at all when calling the diagnostics method.

```
> diagnostics(ple4.xsa2, sections = c(F, F, F, F, F, F, T, T))
Fleet: SNS
Log catchability residuals.
  year
age 1982
            1983 1984
                        1985
                               1986
                                      1987
                                             1988
                                                    1989
                                                           1990
                                                                   1991 1992
    0.161 -0.157 0.129 -0.790 -0.526 -0.769 -0.644 -0.139 -0.638
                                                                  0.544 0.523
  2 \quad 0.432 \quad 0.161 \quad 0.276 \quad 0.536 \quad -0.495 \quad 0.045 \quad -0.023 \quad 0.201 \quad -0.085 \quad 0.107 \quad 0.701
  3 - 0.273 - 1.504 \ 0.056 - 0.001 - 0.352 - 0.718 \ 0.719 \ 0.357 \ 0.024 - 0.074 \ 0.051
  year
                         1996
                                1997
                                                            2001
    1993
           1994 1995
                                       1998 1999
                                                    2000
                                                                   2002 2003
aσe
                                NA 0.163 0.688 0.278 0.219 -0.146
 1 0.403 -0.024 -0.447 -1.170
                                  NA -0.379 0.530 -0.227 0.194 -0.223
  2 0.511 0.531 -0.429 0.268
                                                                          NA
  3 - 0.349 - 0.334 - 0.378 0.267 - 0.055 0.383 0.302 - 0.380 - 0.091 - 0.133
                                                                          NA
  year
age 2004
           2005
                 2006
                         2007 2008
 1 0.004 -0.068 -0.189 -0.080 0.005
  3 0.060 -0.053 0.170 -0.058 0.119
Mean log catchability and standard error of ages with catchability
independent of year class strength and constant w.r.t. time
                       2
Mean Logg -3.8398 -5.1320 -6.4314
S.E Logg 0.4615 0.3343 0.4171
Terminal year survivor and F summaries:
Age 1 Year class =2007
source
    scaledWts survivors yrcls
              628413 2007
       0.971
        0.029
                 582833 2007
fshk
Age 2 Year class =2006
source
    scaledWts survivors yrcls
SNS
        0.973
               379472
                         2006
                 278972
        0.027
                         2006
Age 3 Year class =2005
source
    scaledWts survivors yrcls
SNS
      0.981
               256941
                         2005
        0.019
                 175760
fshk
                         2005
```

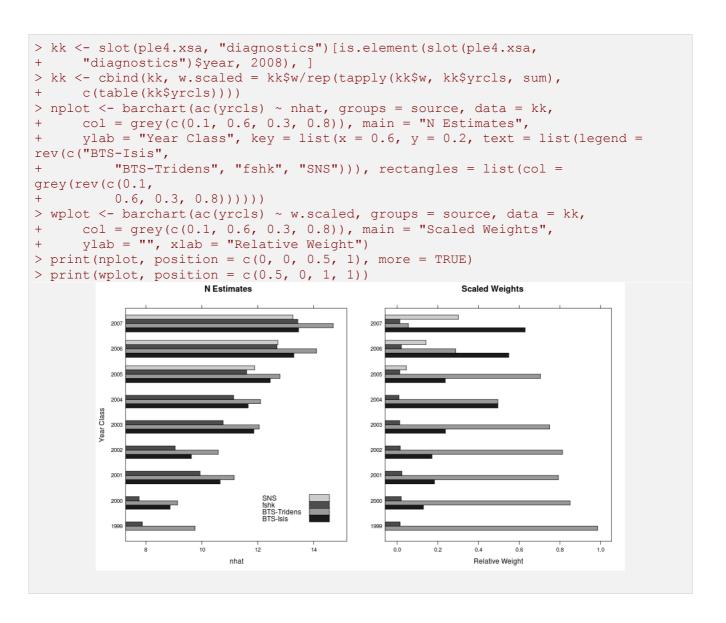
Remember that the diagnostics method will only output text to the console, enabling you to copy and paste the output to a report or other document. If you want to access the diagnostic data you will need to access the specific slots of the returned FLXSA object. The information that you will requie is contained in various slots. The individual estimates of population number from each source (ie. tuning series and F shrinkage) and their individual weightings are stored as a dataframe in the diagnostics slot of the returned object. Other slots contain the internal and external standard errors; the log catchability residuals. For a more thorough description of the XSA diagnostics you should consult the VPA users manaual.

#### 4.4 Plotting Diagnostics

Very often the quickest and simplest way to determine the fit of the model is through visual inspection of the various diagnostic outputs. Here we provide examples of how to extract the relevant information from the return FLXSA object and to plot it using a variety of lattice functions available to R. We start by plotting the log catchability residuals at age from each of the three tuning series. The data are stored as an FLQuants object in the index.res slot of the FLXSA object. First we need to assign names to each of the FLQuant objects so we know which fleet they represent.



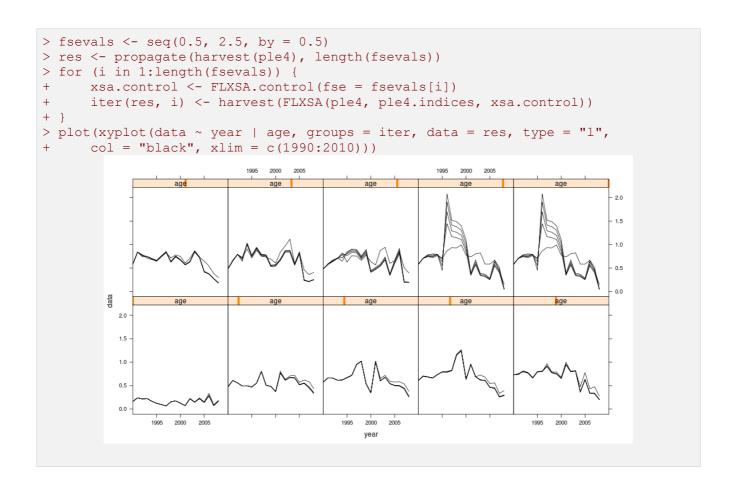
A simple comparison of the terminal year survivors estimates can be obtained from the information stored in the diagnostics slot of the FLXSA object. In the following example we first extract the information relevant to the survivors estimates in the final year and store it as a temporary object. The weights values contained in this data set are the raw fleet based weights that have been calculated from the standard errors of the fleet based survivors estimates at each age in the cohort. To aid visualisation and to see the relative contribution of each fleets estimate to the final estimated value of survivors we re-scale the weights to a maximum value of 1 and plot both the fleet based survivors estimates from each fleet and their scaled weight. The results show relatively consistent estimates of survivors from all fleets across most ages. The scaled weights show the some series to have the greatest influence on the terminal estimates at the younger ages whilst others have greater influence at older ages and that throughout all ages F shrinkage recieves very little weighting.



## 4.5 Sensitivity Analyses

The simplified calling format of FLXSA makes it very easy to run multiple analyses to investigate model sensitivity to parameter settings. A wide variety of such investigations are possible. In this simple example we will look at the effect that different F shrinkage standard errors have on the terminal estimates of fishing mortality. We start by creating a vector of F shrinkage values to be used in the anlyses and by creating an FLQuant with sufficient dimensions to store the results. To do this we use the propagate function to

extend an FLQuant in the  $6^{th}$  dimension by the number of runs that we are going to perform. The estimates of fishing mortality for each XSA run are stored in the FLQuant using the  $6^{th}$  dimension to hold each iteration. The results show little sensitivity to increasing F shrinkage values at values between 1.0 and 2.5.



### 4.6 Retrospective Analyses

An important diagnostic check is to see how the estimated values vary as the time series of the input data changes. We can make use of existing R functions to apply the same assessment model to successively truncated the time series of input data. In this example we are using window to truncate the FLStock object to the specified year range, the + operator to pass the results of the XSA into the FLStock object and the tapply function to perform this action over the year range 2004:2008. Note that the resulting object, called ple4.ret, is of class FLStocks ie. a list of FLStock objects, each one having a separate year range.

```
> retro.yrs <- 2004:2008
> ctrl <- FLXSA.control(fse = 2.5)
> ple4.ret <- FLStocks(tapply(retro.yrs, 1:length(retro.yrs), function(x) return(window(ple4, end = x), ple4.indices, ctrl))))
> plot(plot(ple4.ret, lty = 1, col = "black", lwd = 1, xlim = c(1990, + 2010))[-1])

**The proof of the proof of the
```