

# Natural Mortality Modelling

Assessment for All initiative (a4a)

18 September, 2017

The document explains the approach being developed by a4a to integrate uncertainty in natural mortality into stock assessment and advice. It presents a mixture of text and code, where the former explains the concepts behind the methods, while the latter shows how these can be run with the software provided.

## Required packages

To follow this tutorial you should have installed the following packages:

- CRAN: copula, triangle, coda, XML, reshape2, latticeExtra
- FLR: FLCore, FLa4a

You can do so as follows,

```
install.packages(c("copula", "triangle", "coda", "XML", "reshape2", "latticeExtra"))  
# from FLR  
install.packages(c("FLCore", "FLa4a"), repos="http://flr-project.org/R")
```

```
# Load all necessary packages and datasets, trim pkg messages  
library(FLa4a)  
library(XML)  
library(reshape2)  
library(latticeExtra)  
data(ple4)  
data(ple4.indices)  
data(ple4.index)  
data(rfLen)
```

## Background

In a4a, natural mortality is dealt with as an external parameter to the stock assessment model. The rationale for modelling natural mortality is similar to that for growth: one should be able to obtain information from a range of sources and feed it into the assessment.

The mechanism used by a4a is to build an interface that is transparent and flexible, and makes it easy to explore different options. In relation to natural mortality, it means that the analyst should be able to use distinct models like Gislason's, Charnov's, Pauly's, etc., in a coherent framework, making it possible to compare the outcomes of the assessment.

Within the a4a framework, the general method for inserting natural mortality in the stock assessment is to:

- Create an object of class **a4aM** which holds the natural mortality model and parameters.
- Add uncertainty to the parameters in the **a4aM** object.
- Apply the **m()** method to the **a4aM** object to create an age or length based **FLQuant** object of the required dimensions.

The resulting **FLQuant** object can then be directly inserted into an **FLStock** object to be used for the assessment.

In this section we go through each of the steps in detail using a variety of different models.

For more information on the a4a methodologies refer to Jardim, et.al, 2014, Millar, et.al, 2014 and Scott, et.al, 2016.

## a4aM - The M class

Natural mortality is implemented in a class named **a4aM**. This class is made up of three objects of the class **FLModelSim**. Each object is a model that represents one effect: an age or length effect, a scaling (level) effect and a time trend, named *shape*, *level* and *trend*, respectively. The impact of the models is multiplicative, i.e. the overall natural mortality is given by *shape* x *level* x *trend*. Check the help files for more information.

```
showClass("a4aM")
```

```
Class "a4aM" [package "FLa4a"]
```

```
Slots:
```

```
Name:      shape      level      trend      name      desc      range
Class: FLModelSim FLModelSim FLModelSim character character numeric
```

```
Extends: "FLComp"
```

The **a4aM** constructor requires that the models and parameters are provided. The default method will build each of these models as a constant value of 1.

As a simple example, the usual “0.2” guesstimate could be set up by setting the *level* model to have a single parameter with a fixed value, while the other two models, *shape* and *trend*, have a default value of 1 (meaning that they have no effect).

```
mod02 <- FLModelSim(model=~a, params=FLPar(a=0.2))
m1 <- a4aM(level=mod02)
m1
```

```
a4aM object:
```

```
  shape: ~1
  level: ~a
  trend: ~1
```

More interesting natural mortality shapes can be set up using biological knowledge. The following example uses an exponential decay over ages (implying that the resulting **FLQuant** generated by the **m()** method will be age based). We also use Jensen’s second estimator Kenchington, 2013 as a scaling *level* model, which is based on the von Bertalanffy *k* parameter,  $M = 1.5k$ .

```
shape2 <- FLModelSim(model=~exp(-age-0.5))
level2 <- FLModelSim(model=~1.5*k, params=FLPar(k=0.4))
m2 <- a4aM(shape=shape2, level=level2)
m2
```

```
a4aM object:
```

```
  shape: ~exp(-age - 0.5)
  level: ~1.5 * k
  trend: ~1
```

Note that the *shape* model has *age* as a parameter, but is not set using the *params* argument.

The *shape* model does not have to be age-based. For example, here we set up a *shape* model using Gislason’s second estimator Kenchington, 2013:  $M_l = K(\frac{L_{inf}}{l})^{1.5}$ . We use the default *level* and *trend* models. The

current `m()` method is not ideal for length-based methods because you cannot specify length ranges and half-widths to make compatible with `FLStockLen`

```
shape_len <- FLModelSim(model=~k*(linf/len)^1.5, params=FLPar(linf=60, k=0.4))
m_len <- a4aM(shape=shape_len)
```

Another option is to model how an external factor may impact the natural mortality. This can be added through the *trend* model. Suppose natural mortality can be modelled with a dependency on the NAO index, due to some mechanism that results in having lower mortality when NAO is negative and higher when it's positive. In this example, the impact is represented by the NAO value in the quarter before spawning, which occurs in the second quarter.

We use this to make a complicated natural mortality model with an age based *shape* model, a *level* model based on *k* and a *trend* model driven by NAO, where mortality increases by 50% if NAO is positive in the first quarter. Note, this example needs an internet connection to access the NAO data.

```
# Get NAO
nao.orig <- read.table("https://www.esrl.noaa.gov/psd/data/correlation/nao.data", skip=1, nrow=62, na.s
dnms <- list(quant="nao", year=1948:2009, unit="unique", season=1:12, area="unique")
# Build an FLQuant from the NAO data, with the season slot representing months
nao.flq <- FLQuant(unlist(nao.orig[, -1]), dimnames=dnms, units="nao")
# Build covar by calculating the mean over the first 3 months
nao <- seasonMeans(nao.flq[, , 1:3])
# Turn into Boolean
nao <- (nao>0)
# Constructor
trend3 <- FLModelSim(model=~1+b*nao, params=FLPar(b=0.5))
shape3 <- FLModelSim(model=~exp(-age-0.5))
level3 <- FLModelSim(model=~1.5*k, params=FLPar(k=0.4))
m3 <- a4aM(shape=shape3, level=level3, trend=trend3)
m3

a4aM object:
  shape: ~exp(-age - 0.5)
  level: ~1.5 * k
  trend: ~1 + b * nao
```

## Adding uncertainty to natural mortality parameters with a multi-variate normal distribution

Uncertainty in natural mortality is added through uncertainty in the parameters.

In this section we'll show how to add multivariate normal uncertainty. We make use of method `mvnrm()` from class `FLModelSim`, which is a wrapper for the method `mvnrm()` distributed by the package **MASS**.

We'll create an `a4aM` object with an exponential *shape*, a *level* model based on *k* and temperature (Jensen's third estimator), and a *trend* model driven by the NAO (as above). Afterwards, a variance-covariance matrix for the *level* and *trend* models will be included. Finally, we create an object with 100 iterations using the `mvnrm()` method.

```
# Create the object using shape, level and trend models
shape4 <- FLModelSim(model=~exp(-age-0.5))
level4 <- FLModelSim(model=~k^0.66*t^0.57, params=FLPar(k=0.4, t=10), vcov=array(c(0.002, 0.01, 0.01, 1,
trend4 <- FLModelSim(model=~1+b*nao, params=FLPar(b=0.5), vcov=matrix(0.02))
m4 <- a4aM(shape=shape4, level=level4, trend=trend4)
# Call mvnrm()
```

```
m4 <- mvrnorm(100, m4)
m4
```

```
a4aM object:
```

```
  shape: ~exp(-age - 0.5)
  level: ~k^0.66 * t^0.57
  trend: ~1 + b * nao
```

```
# Inspect the models (e.g. level)
```

```
level(m4) #can also be done with m4@level
```

```
An object of class "FLModelSim"
```

```
Slot "model":
```

```
~k^0.66 * t^0.57
```

```
Slot "params":
```

```
An object of class "FLPar"
```

```
iters: 100
```

```
params
```

```

           k           t
0.39811(0.0457) 9.87074(0.8623)
units:  NA
```

```
Slot "vcov":
```

```

      [,1] [,2]
[1,] 0.002 0.01
[2,] 0.010 1.00
```

```
Slot "distr":
```

```
[1] "norm"
```

```
# Note the variance in the parameters (e.g. trend)
```

```
params(trend(m4))
```

```
An object of class "FLPar"
```

```
iters: 100
```

```
params
```

```

           b
0.50488(0.136)
units:  NA
```

```
# Note the shape model has no parameters and no uncertainty
```

```
params(shape(m4))
```

```
An object of class "FLPar"
```

```
[1] NA
```

```
units:  NA
```

In this particular case, the *shape* model will not be randomized because it doesn't have a variance-covariance matrix. Also note that because there is only one parameter in the *trend* model, the randomisation will use a univariate normal distribution.

The same model could be achieved by using `mvrnorm()` on each model component:

```
m4 <- a4aM(shape=shape4, level=mvrnorm(100, level4), trend=mvrnorm(100, trend4))
```

%Note: How to include ageing error ???

## Adding uncertainty to natural mortality parameters with statistical copulas

We can also use copulas to add parameter uncertainty to the natural mortality model, similar to the way we use them for the growth model. Using a triangle distribution. We use the package triangle, where this distribution is parametrized using the minimum, maximum and median values. This can be very attractive if the analyst needs to, for example, obtain information from the web or literature and perform a meta-analysis. As stated above, these processes make use of the methods implemented for the `FLModelSim` class.

In the following example, we'll use Gislason's second estimator,  $M_l = K(\frac{L_{inf}}{l})^{1.5}$ , and a triangle copula to model parameter uncertainty. The method `mvrtriangle()` is used to create 1000 iterations.

```
linf <- 60
k <- 0.4
# vcov matrix (make up some values)
mm <- matrix(NA, ncol=2, nrow=2)
# calculate variances assuming a 10% cv
diag(mm) <- c((linf*0.1)^2, (k*0.1)^2)
# calculate covariances assuming a correlation of 0.2
mm[upper.tri(mm)] <- mm[lower.tri(mm)] <- sqrt(prod(diag(mm)))*0.2
# a good way to check is using cov2cor
cov2cor(mm)
```

	linf	k
linf	1.0	0.2
k	0.2	1.0

```
# create the FLModelSim object
mgis2 <- FLModelSim(model=~k*(linf/len)^1.5, params=FLPar(linf=linf, k=k), vcov=mm)
# set the lower (a), upper (b) and (optionally) centre (c) of the parameters linf and k (note, without
pars <- list(list(a=55,b=65), list(a=0.3, b=0.6, c=0.35))
# generate 1000 sample sets using mvrtriangle
mgis2 <- mvrtriangle(1000, mgis2, paramMargins=pars)
mgis2
```

```
An object of class "FLModelSim"
Slot "model":
~k * (linf/len)^1.5
```

```
Slot "params":
An object of class "FLPar"
iters: 1000
```

```
params
      linf      k
59.94387(2.1843) 0.41208(0.0749)
units: NA
```

```
Slot "vcov":
```

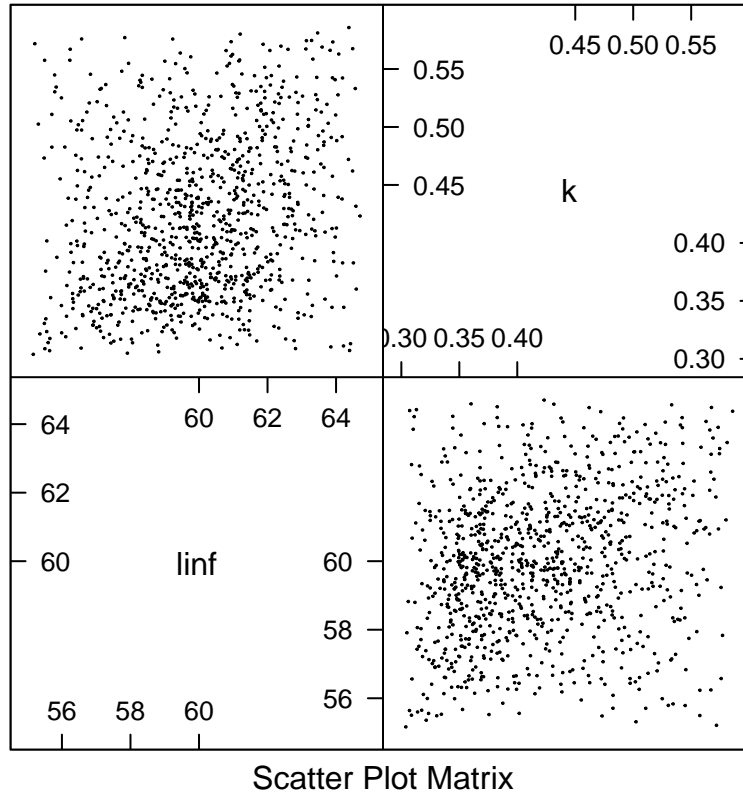


Figure 1: Parameter estimates for Gislason's second natural mortality model based on a triangle distribution.

```
      [,1]      [,2]
[1,] 36.000 0.0480
[2,]  0.048 0.0016
```

```
Slot "distr":
[1] "un <deprecated slot> triangle"
```

The resulting parameter estimates and marginal distributions can be seen in Figure 1 and Figure 2.

We now have a new model that can be used for the *shape* model. You can use the constructor or the set method to add the new model. Note that we have quite a complex method now for M. A length based *shape* model from Gislason's work, Jensen's third model based on temperature *level* and a time *trend* depending on an environmental index, NAO. All of the component models have uncertainty in their parameters.

```
#Using the constructor
m5 <- a4aM(shape=mgis2, level=level4, trend=trend4)
# or the set method for shape to change m4 previously created
m5 <- m4
shape(m5) <- mgis2
```

## Computing natural mortality time series - the m() method

Now that we have set up the natural mortality **a4aM** model and added parameter uncertainty to each component, we are ready to generate the FLQuant for natural mortality. For that we need the **m()** method.

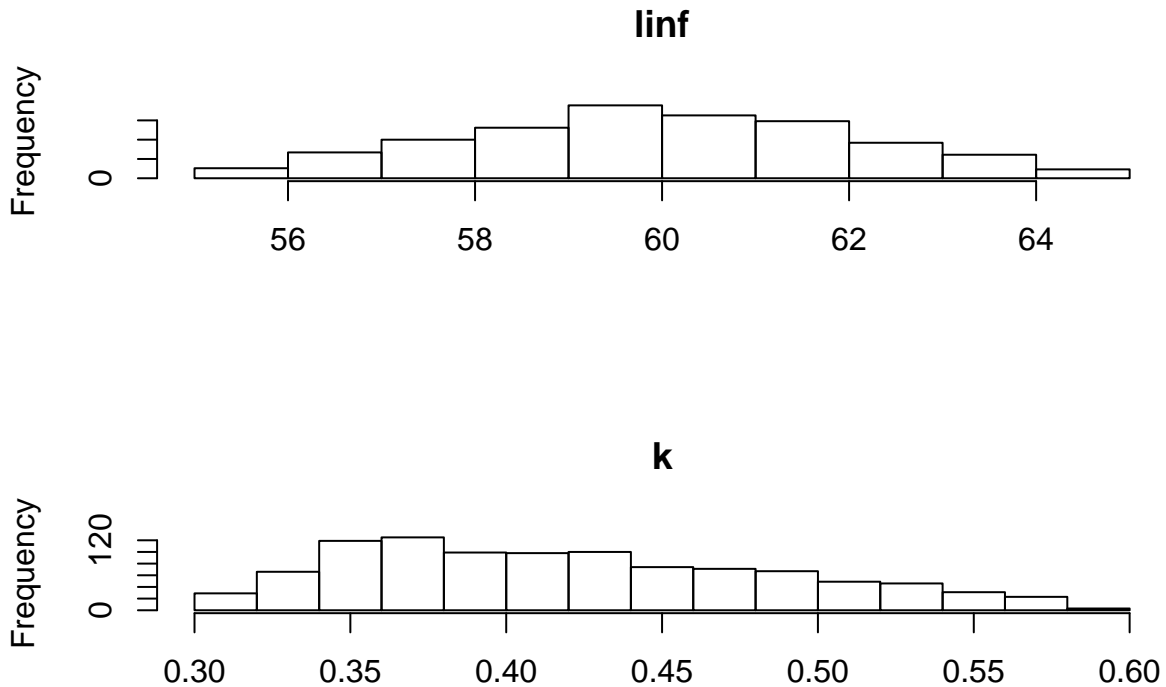


Figure 2: Marginal distributions of the parameters for Gislason's second natural mortality model using a triangle distribution.

The `m()` method is the workhorse method for computing natural mortality. The method returns an `FLQuant` that can be inserted in an `FLStock` for usage by the assessment method.

The method uses the `range` slot to work out the dimensions of the `FLQuant` object. % Future developments will also allow for easy insertion into `FLStockLen` objects.

The size of the `FLQuant` object is determined by the `min`, `max`, `minyear` and `maxyear` elements of the `range` slot of the `a4aM` object. By default the values of these elements are set to 0, giving an `FLQuant` with length 1 in the `quant` and `year` dimension. The `range` slot can be set by hand, or by using the `rngquant()` and `rngyear()` methods.

The name of the first dimension of the output `FLQuant` (e.g. 'age' or 'len') is determined by the parameters of the `shape` model. If it is not clear what the name should be then the name is set to 'quant'.

Here we demonstrate `m()` using the simple `a4aM` object we created above that has constant natural mortality.

```
# Start with the simplest model
m1
```

`a4aM` object:

```
shape: ~1
level: ~a
trend: ~1
```

```
# Check the range
```

```
range(m1) # no ages or years...
```

min	max	plusgroup	minyear	maxyear	minmbar	maxmbar
0	0	0	0	0	0	0

```
m(m1) # confirms no ages or years
```

An object of class "FLQuant"

```
An object of class "FLQuant"
, , unit = unique, season = all, area = unique
```

```
      year
quant 0
      0 0.2
```

```
units: NA
```

```
# Set the quant and year ranges
range(m1, c('min', 'max')) <- c(0,7)           # set the quant range
range(m1, c('minyear', 'maxyear')) <- c(2000, 2010) # set the year range
range(m1)
```

```
      min      max plusgroup  minyear  maxyear  minmbar  maxmbar
      0        7          0    2000    2010         0         0
```

```
# Show the object with the M estimates by age and year
# (note the name of the first dimension is 'quant')
m(m1)
```

```
An object of class "FLQuant"
, , unit = unique, season = all, area = unique
```

```
      year
quant 2000 2001 2002 2003 2004
      0 0.2  0.2  0.2  0.2  0.2
      1 0.2  0.2  0.2  0.2  0.2
      2 0.2  0.2  0.2  0.2  0.2
      3 0.2  0.2  0.2  0.2  0.2
      4 0.2  0.2  0.2  0.2  0.2
      5 0.2  0.2  0.2  0.2  0.2
      6 0.2  0.2  0.2  0.2  0.2
      7 0.2  0.2  0.2  0.2  0.2
```

```
[ ... 1 years]
```

```
      year
quant 2006 2007 2008 2009 2010
      0 0.2  0.2  0.2  0.2  0.2
      1 0.2  0.2  0.2  0.2  0.2
      2 0.2  0.2  0.2  0.2  0.2
      3 0.2  0.2  0.2  0.2  0.2
      4 0.2  0.2  0.2  0.2  0.2
      5 0.2  0.2  0.2  0.2  0.2
      6 0.2  0.2  0.2  0.2  0.2
      7 0.2  0.2  0.2  0.2  0.2
```

The next example has an age-based shape. As the *shape* model has 'age' as a variable which is not included in the *FLPar* slot, it is used as the name of the first dimension of the resulting *FLQuant*. Note that in this case, the *mbar* values in the range become relevant, once that *mbar* is used to compute the mean level. This mean level will match the value given by the *level* model. The *mbar* range can be changed with the *rngmbar()* method. We illustrate this by making an *FLQuant* with age-varying natural mortality.

```
# Check the model and set the ranges
m2
```



a4aM object:

```
shape: ~exp(-age - 0.5)
level: ~1.5 * k
trend: ~1
```

```
range(m2, c('min', 'max')) <- c(0,7)           # set the quant range
range(m2, c('minyear', 'maxyear')) <- c(2000, 2010) # set the year range
range(m2)
```

min	max	plusgroup	minyear	maxyear	minmbar	maxmbar
0	7	0	2000	2010	0	0

m(m2)

An object of class "FLQuant"

, , unit = unique, season = all, area = unique

	year				
age	2000	2001	2002	2003	2004
0	0.60000000	0.60000000	0.60000000	0.60000000	0.60000000
1	0.22072766	0.22072766	0.22072766	0.22072766	0.22072766
2	0.08120117	0.08120117	0.08120117	0.08120117	0.08120117
3	0.02987224	0.02987224	0.02987224	0.02987224	0.02987224
4	0.01098938	0.01098938	0.01098938	0.01098938	0.01098938
5	0.00404277	0.00404277	0.00404277	0.00404277	0.00404277
6	0.00148725	0.00148725	0.00148725	0.00148725	0.00148725
7	0.00054713	0.00054713	0.00054713	0.00054713	0.00054713

[ ... 1 years]

	year				
age	2006	2007	2008	2009	2010
0	0.60000000	0.60000000	0.60000000	0.60000000	0.60000000
1	0.22072766	0.22072766	0.22072766	0.22072766	0.22072766
2	0.08120117	0.08120117	0.08120117	0.08120117	0.08120117
3	0.02987224	0.02987224	0.02987224	0.02987224	0.02987224
4	0.01098938	0.01098938	0.01098938	0.01098938	0.01098938
5	0.00404277	0.00404277	0.00404277	0.00404277	0.00404277
6	0.00148725	0.00148725	0.00148725	0.00148725	0.00148725
7	0.00054713	0.00054713	0.00054713	0.00054713	0.00054713

*# Note that the level value is*

```
c(predict(level(m2)))
```

[1] 0.6

*# which is the same as*

```
m(m2)["0"]
```

An object of class "FLQuant"

, , unit = unique, season = all, area = unique

	year				
age	2000	2001	2002	2003	2004
0	0.6	0.6	0.6	0.6	0.6

[ ... 1 years]

```

      year
age 2006 2007 2008 2009 2010
    0 0.6  0.6  0.6  0.6  0.6

```

```

# This is because the mbar range is currently set to "0" and "0" (see above)
# and the mean natural mortality value over this range is given by the level model.
# We can change the mbar range
range(m2, c('minmbar', 'maxmbar')) <- c(0,7)           # set the quant range
range(m2)

```

```

      min      max plusgroup  minyear  maxyear  minmbar  maxmbar
      0        7          0    2000    2010        0        7

```

```

# which rescales the the natural mortality at age
m(m2)

```

```

An object of class "FLQuant"
, , unit = unique, season = all, area = unique

```

```

      year
age 2000      2001      2002      2003      2004
    0 3.0351969 3.0351969 3.0351969 3.0351969 3.0351969
    1 1.1165865 1.1165865 1.1165865 1.1165865 1.1165865
    2 0.4107692 0.4107692 0.4107692 0.4107692 0.4107692
    3 0.1511136 0.1511136 0.1511136 0.1511136 0.1511136
    4 0.0555916 0.0555916 0.0555916 0.0555916 0.0555916
    5 0.0204510 0.0204510 0.0204510 0.0204510 0.0204510
    6 0.0075235 0.0075235 0.0075235 0.0075235 0.0075235
    7 0.0027677 0.0027677 0.0027677 0.0027677 0.0027677

```

```

[ ... 1 years]

```

```

      year
age 2006      2007      2008      2009      2010
    0 3.0351969 3.0351969 3.0351969 3.0351969 3.0351969
    1 1.1165865 1.1165865 1.1165865 1.1165865 1.1165865
    2 0.4107692 0.4107692 0.4107692 0.4107692 0.4107692
    3 0.1511136 0.1511136 0.1511136 0.1511136 0.1511136
    4 0.0555916 0.0555916 0.0555916 0.0555916 0.0555916
    5 0.0204510 0.0204510 0.0204510 0.0204510 0.0204510
    6 0.0075235 0.0075235 0.0075235 0.0075235 0.0075235
    7 0.0027677 0.0027677 0.0027677 0.0027677 0.0027677

```

```

# Check that the mortality over the mean range is the same as the level model
quantMeans(m(m2)[as.character(0:5)])

```

```

An object of class "FLQuant"
, , unit = unique, season = all, area = unique

```

```

      year
age 2000      2001      2002      2003      2004
all 0.79828 0.79828 0.79828 0.79828 0.79828

```

```

[ ... 1 years]

```

```

      year
age 2006    2007    2008    2009    2010
all 0.79828 0.79828 0.79828 0.79828 0.79828

```

The next example uses a time trend for the *trend* model. We use the *m3* model we derived earlier. The *trend* model for this model has a covariate, 'nao'. This needs to be passed to the *m()* method. The year range of the 'nao' covariate should match that of the *range* slot.

```

# Pass in a single nao value (only one year, because the trend model needs
# at least one value)
m(m3, nao=1)

```

```

An object of class "FLQuant"
An object of class "FLQuant"
, , unit = unique, season = all, area = unique

```

```

      year
age 0
0 0.9

```

```

units: NA

```

```

# Set ages
range(m3, c('min', 'max')) <- c(0,7)          # set the quant range
m(m3, nao=0)

```

```

An object of class "FLQuant"
An object of class "FLQuant"
, , unit = unique, season = all, area = unique

```

```

      year
age 0
0 0.60000000
1 0.22072766
2 0.08120117
3 0.02987224
4 0.01098938
5 0.00404277
6 0.00148725
7 0.00054713

```

```

units: NA

```

```

# With ages and years - passing in the NAO data as numeric (1,0,1,0)
range(m3, c('minyear', 'maxyear')) <- c(2000, 2003) # set the year range
m(m3, nao=as.numeric(nao[,as.character(2000:2003)]))

```

```

An object of class "FLQuant"
An object of class "FLQuant"
, , unit = unique, season = all, area = unique

```

```

      year
age 2000    2001    2002    2003
0 0.90000000 0.60000000 0.90000000 0.60000000
1 0.33109150 0.22072766 0.33109150 0.22072766
2 0.12180175 0.08120117 0.12180175 0.08120117
3 0.04480836 0.02987224 0.04480836 0.02987224

```

```

4 0.01648407 0.01098938 0.01648407 0.01098938
5 0.00606415 0.00404277 0.00606415 0.00404277
6 0.00223088 0.00148725 0.00223088 0.00148725
7 0.00082069 0.00054713 0.00082069 0.00054713

```

```
units: NA
```

The final example show how `m()` can be used to make an `FLQuant` with uncertainty (see Figure 3). We use the `m4` object from earlier with uncertainty on the *level* and *trend* parameters.

```

range(m4, c('min', 'max')) <- c(0,7) # set the quant range
range(m4, c('minyear', 'maxyear')) <- c(2000, 2003)
flq <- m(m4, nao=as.numeric(nao[,as.character(2000:2003)]))
flq

```

```
An object of class "FLQuant"
```

```
An object of class "FLQuant"
```

```
iters: 100
```

```
, , unit = unique, season = all, area = unique
```

```

      year
age 2000      2001      2002
0 3.0079919(0.359714) 2.0389830(0.229792) 3.0079919(0.359714)
1 1.1065784(0.132331) 0.7500999(0.084536) 1.1065784(0.132331)
2 0.4070874(0.048682) 0.2759463(0.031099) 0.4070874(0.048682)
3 0.1497591(0.017909) 0.1015150(0.011441) 0.1497591(0.017909)
4 0.0550933(0.006588) 0.0373453(0.004209) 0.0550933(0.006588)
5 0.0202677(0.002424) 0.0137386(0.001548) 0.0202677(0.002424)
6 0.0074561(0.000892) 0.0050541(0.000570) 0.0074561(0.000892)
7 0.0027429(0.000328) 0.0018593(0.000210) 0.0027429(0.000328)
      year
age 2003
0 2.0389830(0.229792)
1 0.7500999(0.084536)
2 0.2759463(0.031099)
3 0.1015150(0.011441)
4 0.0373453(0.004209)
5 0.0137386(0.001548)
6 0.0050541(0.000570)
7 0.0018593(0.000210)

```

```
units: NA
```

```
dim(flq)
```

```
[1] 8 4 1 1 1 100
```

## References

Ernesto Jardim, Colin P. Millar, Iago Mosqueira, Finlay Scott, Giacomo Chato Osio, Marco Ferretti, Nekane Alzoriz, Alessandro Orio; What if stock assessment is as simple as a linear model? The a4a initiative. ICES J Mar Sci 2015; 72 (1): 232-236. doi: icesjms/fsu050

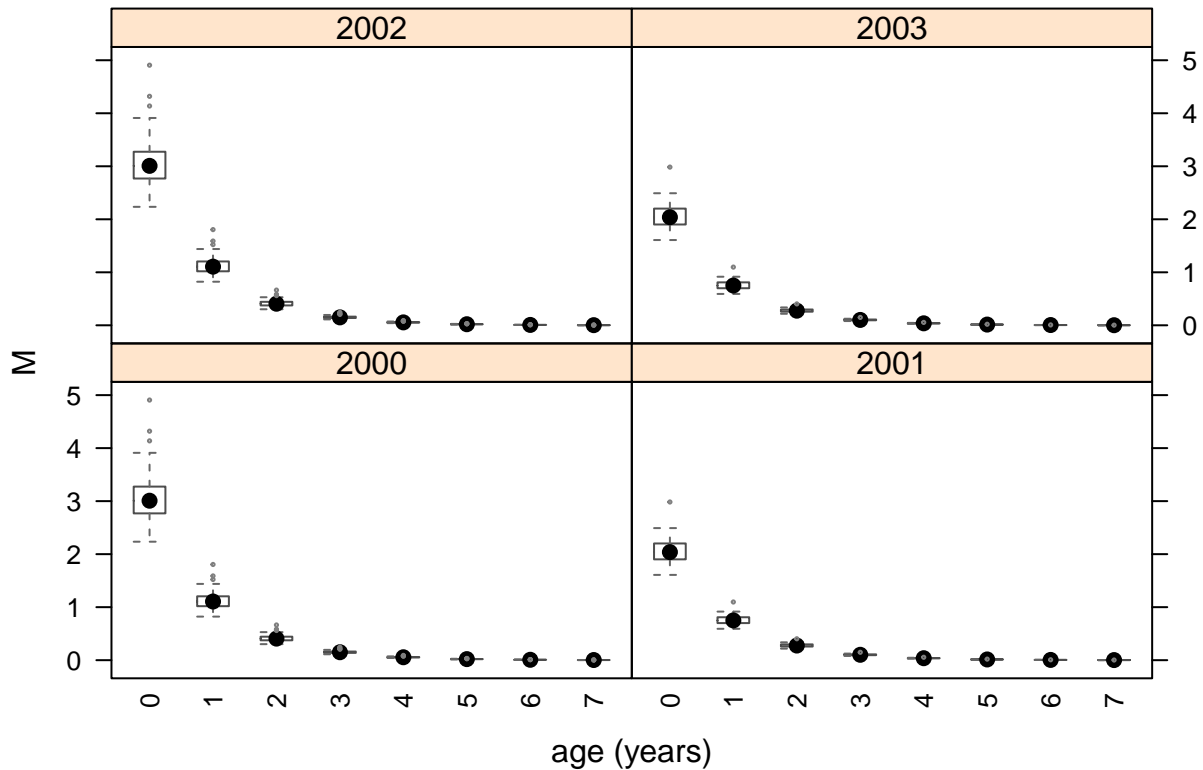


Figure 3: Natural mortality with age and year trend.

Kenchington, T. J. (2014), Natural mortality estimators for information-limited fisheries. *Fish Fish*, 15: 533-562. doi: 10.1111/faf.12027.

Colin P. Millar, Ernesto Jardim, Finlay Scott, Giacomo Chato Osio, Iago Mosqueira, Nekane Alzorritz; Model averaging to streamline the stock assessment process. *ICES J Mar Sci* 2015; 72 (1): 93-98. doi: icesjms/fsu043

Scott F, Jardim E, Millar CP, Cervino S (2016) An Applied Framework for Incorporating Multiple Sources of Uncertainty in Fisheries Stock Assessments. *PLoS ONE* 11(5): e0154922. doi: 10.1371/journal.pone.0154922

## More information

Documentation can be found at (<http://flr-project.org/FLa4a>). You are welcome to:

- Submit suggestions and bug-reports at: (<https://github.com/flr/FLa4a/issues>)
- Send a pull request on: (<https://github.com/flr/FLa4a/>)
- Compose a friendly e-mail to the maintainer, see `packageDescription('FLa4a')`

## Software Versions

- R version 3.4.1 (2017-06-30)
- FLCore: 2.6.5
- FLa4a: 1.1.3
- **Compiled:** Mon Sep 18 15:20:19 2017

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## Author information

**Ernesto Jardim.** European Commission, DG Joint Research Centre, Directorate D - Sustainable Resources, Unit D.02 Water and Marine Resources, Via E. Fermi 2749, 21027 Ispra VA, Italy. <https://ec.europa.eu/jrc/>