

$$[(U-V)(X-U)(X-V)]^{\frac{1}{2}} = (X-U)$$

(6) Gumbel Copula when  $\alpha=1$

$$C_{\alpha}^2(U, V) = \exp \left\{ - \left[ (-\log U)^{\alpha} + (-\log V)^{\alpha} \right]^{\frac{1}{\alpha}} \right\}$$

$$= \exp \left\{ - \left[ (-\log U)^2 + (-\log V)^2 \right]^{\frac{1}{2}} \right\}$$

$$U \sim \text{Exp}(0.01) \quad V \sim \text{Exp}(0.02)$$

(a) both will default:

~~$$F(T) = 8 \times e^{-RT} C(F_1(T), F_2(T))$$~~

$$F_1(T) = P(U \leq 1) = 1 - e^{-0.01 \times 1} = 0.9950166\%$$

$$F_2(T) = P(V \leq 1) = 1 - e^{-0.02 \times 1} = 1.980133\%$$

$$P = C(F_1(T), F_2(T)) = C(0.9950166\%, 1.980133\%)$$

$$= 0.00235139$$

~~$F(T)$~~

(b) At least one will default:

$$P = F_1(T) + F_2(T) - C(F_1(T), F_2(T))$$

$$= 0.9950166\% + 1.980133\% - 0.00235139$$

$$= 0.0274001$$

$$(7) F(T) = 8 \times e^{-RT} C(F_1(T), F_2(T))$$

$$= 1000000 \times e^{-0.01 \times 1} \times C(F_1(1), F_2(1))$$

$$= 235.9$$

4 if  $\alpha=1$

$$C_{\alpha}(U, V) = \exp \left\{ - \left[ (-\log U)^{\alpha} + (-\log V)^{\alpha} \right]^{\frac{1}{\alpha}} \right\}$$

$$\text{Thus } F(T) = 8 \times e^{-RT} C(F_1(1), F_2(1))$$

$$= 1000000 \times e^{-0.01 \times 1} \times (0.9950166\% \times 1.980133\%)$$

$$= 197.0265$$