## Stat GR5205, Fall 2017

## Assignment #5: Due October 30

- 1. Consider a *n*-dimensional random variance X with mean covariance matrix  $\Sigma$ . Let A be a  $k \times n$  matrix. Show that the covariance matrix of Y = AX is  $A\Sigma A^{\top}$ .
- 2. Consider linear model  $y = \beta_0 + \beta_1 x_1 + ... + \beta_p x_p + \varepsilon$  and  $\varepsilon \sim N(0, \sigma)$  and hypotheses

$$H_0: \beta_1 = 0 \quad H_1: \beta_1 \neq 0.$$

Show that t-test and F-test are equivalent in the sense that the  $T^2 = F$  where T is the t-statistic and F is the F-statistic.

- 3. Chapter 6, problem 5, a. b. c. f.
- 4. Chapter 6, problem 7.
- 5. Chapter 6, problem 8.
- 6. Chapter 6, problem 25.